State of Florida Department of Transportation



EVALUATION OF CONCRETE PILE TO FOOTING OR CAP CONNECTIONS

(Project No.: BED29-977-09)

FINAL REPORT

Principal Investigator

Armin Mehrabi

Florida International University 10555 W. Flagler St., EC 3606 Miami, FL 33174 Phone: 305-348-3653 Email: <u>amehrabi@fiu.edu</u>

Project Manager

Christina Freeman

Florida Department of Transportation M.H. Ansley Structures Research Center 2007 E. Paul Dirac Dr. Tallahassee, FL 32310 Phone: 850-921-7100 Email: Christina.Freeman@dot.state.fl.us

Revised May 2024

DISCLAIMER

The opinions, findings, and conclusions expressed in this publication are those of the authors and not necessarily those of the Florida Department of Transportation

TECHNICAL REPORT DOCUMENTATION PAGE

1. Report No.	2. Go	overnment Accession N	lo.	3. Rec	ipient's Catalog No.	
4. Title and Subtitle	1			5. Rep	ort Date	
Evaluation of Concrete Pile t	o Fo	oting or Cap Co	nnections	nections		
			-	6. Per	forming Organizatio	n Code
7. Author(s)				8. Perf	orming Organization	ı Report No.
Isabella Rakestraw						
Armin Mehrabi (0000-0003-4736-850X)						
Seung Jae Lee						
9. Performing Organization Name and Add	dress			10. Wo	ork Unit No. (TRAIS)	
Florida International University						
11200 SW 8th Street			-	11. Co	ntract or Grant No.	
Miami, FL 33199				BED29	9-977-09	
12. Sponsoring Agency Name and Addres	ss			13. Ty	pe of Report and Pe	riod Covered
Phone: (850) 414-5260				Final F May 20	Report 019 to May 2024	
605 Suwannee Street Tallahassee, Florida 32399-0450				14. Sp	onsoring Agency Co	de
Email: research.center@dot.state.fl.us						
15. Supplementary Notes						
16. Abstract						
Foundations for many bridges consist of c	driven	piles embedded in pile	caps or footings whe	ereby a	ixial loads, lateral lo	ads, and moments are
transferred from the bridge to underlying transferred through the bridge. The pile-to	soil a o-cap	nd/or bedrock. The co connection is typically	nnection between the either assumed to be	e pile a e a pin	and pile cap will affe ned or a fixed conn	ection. Current design
recommendations for pinned and fixed con	nectio	ns vary in different state	s. The disconnect be	tween	current design provis	ions and past research
would suggest that many structures may h	nave a	different level of actual nection between the pi	fixity between piles a le and pile cap, to an	nd pile valvze t	caps than assumed the impact of the co	. The primary objective
structure, and to provide a better guidance	to eng	ineers. Experimental te	sting was completed	involvir	ng ten prestressed c	oncrete pile specimens
embedded into cast-in-place pile caps. Th	ne tests	s were conducted to de	termine the moment	capaci	ty of the connection	at failure. In all cases,
development length of the strands. Results	ts of th	is research showed that	t the full moment cap	bacity o	of the pile cap, which	iched with embedment
length shorter than the current guidance. D	Design	recommendations are	proposed to the curre	ent deve	elopment length equ	ations, considering the
clamping lorces and comming suesses de	svelope		a pile.			
17. Key Word			18. Distribution State	ement		
Precast-prestressed concrete pile, Pile-to-cap connections, No restrictions						
embedment length						
19. Security Classif. (of this report)		20. Security Classif. (c	of this page)		21. No. of Pages	22. Price
Unclassified		Unclassified			256	N/A

EXECUTIVE SUMMARY

Foundations for many bridges consist of driven piles embedded in pile caps or footings whereby axial loads, lateral loads, and moments are transferred from the bridge to underlying soil and/or bedrock. Piles can also be subjected to large lateral deflections in the event of an earthquake or vessel impact, which can result in high local curvature and moment demands at various locations along the pile length.

The connection between the pile and pile cap or footing will affect the way forces are transferred through the bridge. Bridge superstructures can transfer axial loads, lateral loads, and moments into substructure and foundation elements. The pile-to-cap connection is typically either assumed to be (1) a pinned connection, allowing for transfer of axial and lateral forces, but no moments, permitting some rotation to eliminate excessive moment build-up, or (2) a fixed connection, allowing transfer of axial and lateral forces and development of the full moment capacity of the pile.

Current design recommendations for pinned and fixed connections vary in different states. Previous research has shown disconnection with current recommendations suggesting that many structures may have a different level of actual fixity. A better understanding of the connection between prestressed concrete piles and cast-in-place (CIP) footings and pile caps is needed to assure designs are completed correctly and conservatively.

A pinned connection between pile and pile cap is typically required to have a positive connection between the pile and cap while still permitting some rotation to eliminate excessive moment buildup. Different states specify between a 6- and 12-inch embedment length for pinned connections. There is limited research specifically on developing a pinned connection between pile and pile cap. Rollins and Stenlund [1] experimentally investigated two connections with shallow embedment (0.5 to 1.0 times the pile diameter) with a reinforcement cage connection. They found that the shallow embedment still developed at least 40 to 60 percent of the moment capacity of the pile.

A fixed connection between the pile and pile cap provides a connection capable of developing the full moment capacity of the pile. It also ensures the connection is rigid enough so that rotation of the pile within the cap does not significantly contribute to the overall drift of the assembly. Several different researchers have previously investigated this type of connection using different types of piles, different sizes of piles, and different loading configurations. Some states require up to a 48-inch pile embedment length to achieve a full moment capacity, which is close to 3 times the pile diameter for 18-inch piles. This recommendation is based on experimental testing conducted by Issa [2] on square 30-inch prestressed concrete piles with an internal pipe void. Since this testing was completed, there have been several additional studies from which researchers have concluded that the full moment capacity of the pile can be developed in embedment lengths less than 48 inches: ranging from an embedment length equal to the pile depth to two times the pile depth. These tests were performed on different pile diameters and with either constant or variable axial loads.

The disconnect between current design provisions and past research would suggest that many structures may have a different level of actual fixity between piles and pile caps or footings than assumed. The primary objective of this research was to better understand the connection between the pile and pile cap, to analyze the impact of the connection in the overall structure, specifically

in structures that are considered sensitive to the connection between the pile and the pile cap, and to provide better guidance to engineers. These objectives were accomplished through three interdependent research efforts, which included a literature review of previous research, an analytical investigation and numerical modeling to explore possible experimental variables, and an experimental testing to evaluate the level of fixity and impact of primary variables.

Engineers currently use these assumptions to design the connection between pile and footing or pile cap, which influences the design of the rest of the structure. Recent research has shown these assumptions are unrealistic and can be unconservative under certain circumstances, e.g., a fixed connection can be achieved with a much shorter embedment length. A better understanding of the connection between prestressed concrete piles and CIP footings and pile caps is needed to ensure designs are completed correctly and conservatively.

In the experimental program, ten full-scale prestressed pile with cast-in-place caps were tested in the FDOT Structures Research Center (SRC) to better understand the pile-to-cap connection. The primary variables selected were pile size (18-inch and 30-inch piles) and embedment length (between 0.33d_{pile} to 1.5d_{pile}). Axial load and interface reinforcement were selected as secondary variables.

The experimental program focused on embedment length. For the 18-inch and 30-inch specimens, embedment lengths between 0.33 and 1.5 times the side dimension of the piles were tested. Moment-displacement results for all specimens are shown in Figure 0.1. All specimens experienced a ductile failure mechanism, where there was significant deflection after the maximum load was reached. All 18-inch pile specimens held close to the ultimate capacity while additional deflection was observed. The 30-inch pile specimens experienced a drop in capacity immediately after the ultimate load was reached. All specimens. SP-10 failed due to slipping of the prestressing strands (strand development). SP-10 failed due to a punching shear failure of the edge of the pile cap adjacent to the embedded pile.



Figure 0.1: Moment versus displacement curves for (a) 18-inch and (b) 30-inch pile specimens.

With respect to capacity, the 18-inch pile specimens with $0.33d_p$ (6-inch) and $0.5d_p$ (9-inch) embedment (SP-01 and SP-04) still developed 34% and 37% of the pile capacity, respectively. The two specimens (SP-06 and SP-09) with the current FDOT-specified embedment length for pinned connections (12-inches) each developed 48% of their respective pile capacity. These specimens had two different pile sizes (SP-06 had 18-inch piles and SP-09 had 30-inch piles), so the capacity did not correspond to the relationship between pile size and pile embedment. Both specimens had the same strand type (0.5-inch special strands), which suggests that the capacity of the connection is more dependent on the available development length of the strand.

The 18-inch pile specimens with the deepest pile embedment (SP-08 with 27-inch embedment) developed 81% of the pile capacity and the 30-inch pile specimen with 30-inch embedment (SP-10) developed 73% of the pile capacity. The smaller capacity developed by SP-10 was likely due to punching shear of the edge of the pile cap occurring before the slipping of the strands occurred. SP-10 had a lower strength concrete in the cap (8.95 ksi) than in the pile (13.82 ksi), which led to a decreased punching shear capacity. Lower concrete strengths are more representative of field conditions where the piles would likely be made with higher strength concrete than the pile cap.

The estimated transfer and development lengths were found using AASHTO LRFD Bridge Design Specification (BDS) [3] and ElBatanouny and Ziehl [4]. Both procedures conservatively estimated the strength of the specimens, on average, with the estimation procedure of ElBatanouny and Ziehl resulting in the more accurate estimation. It was concluded that the moment capacity estimated using AASHTO LRFD BDS is noticeably conservative and that the equations proposed by ElBatanouny and Ziehl provide for a more accurate estimation.

Based on the experimental results and additional numerical modeling, a modification to the strand development equation by AASHTO LRFD BDS was proposed in this study for calculating the partial moment resistance in piles embedded in pile caps or footings. The proposed modified development length equation which considers the confining stresses and clamping forces that develop around the embedded portion of the pile is shown in Equation 0.1

Required development length:
AASHTO LRFD MODIFIED
$$l_d \ge \kappa_p \left(f_{ps} - \frac{2}{3} f_{pe} \right) d_b$$
 Equation 0.1

where:

 d_b = nominal strand diameter (in)

- f_{ps} = average stress in prestressing steel at the time for which the nominal resistance of the member is required (ksi)
- f_{pe} = effective stress in the prestressing steel after losses (ksi)
- $\kappa_p = 0.6$ when finding strand development length in piles embedded into cast-in-place pile caps; included to account for confining stresses.

Additional numerical models were created for specimens with lower pile cap concrete strength to study the impact on the pile-to-cap connection. Results showed a reduction in the moment capacity of the pile-to-cap connection depending on the embedment length. This reduction in capacity is mostly due to a punching shear of the edge of the pile cap occurring before the slipping of the strands. To control the punching shear failure, additional shear reinforcement was included in the numerical analysis. The additional reinforcement increased the punching shear capacity of the pile cap and increased the capacity of the connection by approximately 10%. More importantly, adding

shear reinforcement increased the ductility of the pile-to-footing connection. Major conclusions of this study can be summarized as follows:

- Nine of the ten specimens tested failed due to slipping of the prestressing strand (strand development failure). The 18-inch specimens all held a load around the maximum capacity of the connection as the strands were slipping and pile rotating. The 30-inch pile cap with strand slipping saw a drop in strength when the strands began to slip.
- The transfer and development length equations proposed by ElBatanouny and Ziehl [4] and AASHTO LRFD BDS were used to estimate the moment capacity of the specimens that failed due to strand development. It was concluded that the moment capacity estimated using AASHTO LRFD BDS is noticeably conservative and that the equations proposed by ElBatanouny and Ziehl results in estimates that align closely with the test data.
- A modification to the current AASHTO LRFD BDS development length equation proposed in this study considers the confining stresses developed around the embedded pile. Accordingly, a pile embedment length of 42 inches for 18-inch piles and 30-inch piles would be required for full moment capacity using the proposed modification.
- A small axial compression force greatly increased the capacity of the connection; an average 107% increase in capacity of the connection was observed when $0.05A_g f'_{c,pile}$ axial compression was applied to the pile and connection.
- The specimen with the interface reinforcement (SP-03) developed a moment capacity 67% higher than the similar specimen without interface reinforcement (SP-01).
- The capacity of the connection did not appear to be dependent on the pile embedment length as a function of the pile size. The behavior of the connection appeared to be more dependent on the available strand development length provided by the pile embedment length.
- A linear relationship was observed between rotational stiffness and embedment length in 18-inch piles with 1/2" (special) strand configuration.
- The failure of one of the specimens, SP-10, resembled a punching shear failure where the side of the pile punched through the side face of the pile cap.
- Based on FEM results, lower concrete strength in the cap resulted in change of failure mode and in moment capacities significantly lower than those estimated by assuming a strand development failure. This capacity reduction ranges between 3% to 38% depending on the embedment length. This condition can be more prevalent for actual pile-to-footing connection for which the footing normally uses concrete with strength lower than that in the pile.
- Additional reinforcement bars in the pile cap, located around the embedded pile, are recommended to prevent punching shear failure, therefore allowing the connection to reach its full moment capacity.

TABLE OF CONTENTS

DISCLAIMERii
TECHNICAL REPORT DOCUMENTATION PAGEiii
EXECUTIVE SUMMARY iv
TABLE OF CONTENTS viii
LIST OF FIGURES xiii
LIST OF TABLESxxv
Chapter 1: Introduction1
1.1 Background1
1.2 Objectives
1.3 Tasks
Chapter 2: Literature Review on Pile-to-Cap Connections
2.1 Types of Precast Pile-to-Cap Connections
2.2 Pinned Connection between Pile and Cap
2.2.1 Summary of Past Research
2.3 Fixed Connection between Pile and Pile Cap7
2.3.1 Required Behavior and Mechanism7
2.3.2 Summary of Past Research
2.4 Current DOTS' Recommendations10
2.4.1 Florida Recommendation for Pinned Connections10
2.4.2 Florida Recommendations for Fixed Connections11
2.4.3 Other DOTS' Recommendations11
2.5 Resisting Mechanisms
2.5.1 Strand Development for Fixed Connections15
2.5.2 Shear Friction Capacity of Interface
2.5.3 Bearing Capacity of Interface17
2.6 Testing Details From Previous Research
2.6.1 Experimental Variables
2.6.2 Test Setups
2.6.3 Instrumentation Layouts

3: Sensitivity Structure Analysis
Bridge #1: Simple Spans with Uneven Span Lengths
1 Base Structure
2 Concrete Strength Properties
3 Cross-Section Details for Members
4 Construction Procedure
5 Fixed versus Pinned Connection
6 Boundary Conditions and Modeling Assumptions
7 Summary of Results40
Bridge #2: PT Segmental Box girder with Fixed Pier Table and Lateral Load on ructure
1 Base Structure
2 Concrete Strength
3 Cross Section Details for Members47
4 Loading
5 Boundary Conditions and Modeling Assumptions49
6 Summary of Results
Bridge #3: Straddle Bent
1 Base Structure
2 Cross-Section Details for Members
3 Loading61
4 Boundary Conditions and Modeling Assumptions
5 Summary of Results
Bridge #4: PT Segmental Box Girder with Fixed Pier Table
1 Base Structure
2 Elevation and Detail
3 Pile Layout
4 Boundary Conditions and Modeling Assumptions
5 Summary of Results
4: Preliminary Numerical Study72
Boundary Conditions and Modeling Assumptions for Pile-to-Cap Connection Models72
1 Model Geometry
2 Material Assumptions73

4.1.3	Test Setup and Boundary Conditions	74
4.1.4	Load Protocol	75
4.1.5	Finite Element Mesh	77
4.2 Nu	merical Results for Pile-To-Cap Connection Models	78
4.2.1	Pile Capacity	78
4.2.2	Effect of Embedment Length	79
4.2.3	Effect of Axial Load	84
4.2.4	Effect of Pile Concrete Strength	86
4.2.5	Effect of Pile-Cap Concrete Strength	87
4.2.6	Effect of Pile Cap Size	88
4.2.7	Effect of Reinforcement around Pile	88
4.2.8	Effect of Strand Pattern	89
4.2.9	Summary of Results of Preliminary Numerical Study	90
Chapter 5: E	xperimental Program	92
5.1 Tes	st Matrix	92
5.1.1	Primary Variables	92
5.1.2	Secondary Variables	93
5.2 Spe	ecimen Description	94
5.2.1	Pile Details	94
5.2.2	Pile Cap Details	94
5.3 Tes	st Setup	103
5.3.1	Spreader Beams	105
5.3.2	Threaded Rods	105
5.4 Exp	perimental Procedure	106
5.4.1	Without Axial Load	106
5.4.2	With Axial Load	108
5.5 Ins	trumentation Plan	109
5.5.1	Deflection Gauges	109
5.5.2	Surface Gauges	110
5.5.3	Rebar Gauges	111
5.5.4	Vibrating Wire Strain Gauges (VWSG)	112
5.5.5	Fiber Optic Sensors	113
5.6 Spe	ecimen Construction	113

5.6.1	18-inch Specimens	
5.6.2	30-inch Specimens	116
5.7 Te	est Setup and Protocol	
5.7.1	Without Axial Load Application	
5.7.2	Axial Load Application	
5.8 Pil	les Capacity	
5.8.1	Capacity of 18-inch Piles	
5.8.2	Capacity of 30-inch Piles	
5.9 Su	mmary of Results	
5.9.1	Specimen Detail Summary	
5.9.2	Material Properties	
5.9.3	Transfer Length	
5.9.4	Prestress Losses	
5.9.5	Ultimate Strength Testing Results	
5.10	Analysis of Results	
5.10.1	Observed Failure Mechanism	
5.10.2	Moment Capacity and Pile Embedment Length	
5.10.3	Effect of Interface Reinforcement	171
5.10.4	Effect of Pile Size	
Chapter 6: 1	Final Computational Analysis	
6.1 Pi	le-to-Cap Modeling Assumptions	
6.1.1	Model Geometry	
6.1.2	Material Assumptions	
6.1.3	Boundary Conditions	
6.1.4	Load Protocol	
6.1.5	Finite Element Mesh	
6.2 Nu	umerical Results for Experimental Matrix	
6.2.1	Bond-Slip Relationship of Strands	
6.2.2	Crack Pattern and Failure Modes	
6.3 Ac	ditional Numerical Analysis	
6.3.1	Embedment Length	
6.3.2	Strand Diameter	
6.3.3	Pile Cap Concrete Strength	

Chapter	7: Sun	nmary of Observations	.211
7.1	Partia	l Moment Resistance	211
7.1	.1 N	Aodified Strand Development Equation	.211
7.1	.2 N	Noment Capacity and Pile Embedment Length	.212
7.1	.3 R	Recommendation for Fixed Connection	.217
7.1	.4 R	Rotational Stiffness	.217
7.2	Servic	ceability Limit	.218
7.3	Punch	ning Shear Control	.219
Chapter	8: Sun	nmary and Conclusions	.222

LIST OF FIGURES

Figure 0.1: Moment versus displacement curves for (a) 18-inch and (b) 30-inch pile specimensv
Figure 2.1: Typical construction procedure for piles with cast-in-place pile cap
Figure 2.2: (a) Forces from the above structure assumed to be transferred to piles either through (b) pinned or (c) fixed connections
Figure 2.3: Types of pile embedment details (modified from [12] and [15])
Figure 2.4: Embedment details for Rollins and Stenlund [1] specimens; (a) with and (b) without interface steel
Figure 2.5: Embedment details for (a) Xiao [16] and (b) Harries et al. [12]6
Figure 2.6: Failure of this connection can be controlled by (a) development length of the prestressing strand, (b) shear friction capacity between the pile and pile cap, and (c) bearing between the pile and cap
Figure 2.7: (a) FDOT pinned connection details and (b) strand development10
Figure 2.8: FDOT fixed connection details11
Figure 2.9: Strand development in embedded prestressed concrete pile: (a) Available development length and plane where full moment capacity is desired; (b) shrinkage of the footing or cap will actively confine the embedded pile, and (c) bending of the pile will place compressive stresses on portions of the pile bearing against footing or cap
Figure 2.10: Test setup for pile-to-cap connection testing conducted by Rollins and Stenlund [1]
Figure 2.11: Capacity of resultant of horizontal load (V_n) dependent on bearing stress between embedded pile and cap, details for model proposed by (a) Mattock and Gaafar [42]; (b) Marcakis and Mitchell [43]
Figure 2.12: Types of connections: (a) plain embedment of the pile into the cap; (b) embedment with interface steel extending from the pile into the pile cap
Figure 2.13: Test setup used by Shahawy and Issa [20]21
Figure 2.14: Previously investigated pile cross sections: (a) square prestressed concrete pipe pile; (b) square prestressed concrete pile; (c) octagonal prestressed concrete pile; (d) steel HP piles; (e) steel pipe pile; (f) circular timber pile23
Figure 2.15: Direction of bearing stresses in (a) square; (b) octagonal piles23
Figure 2.16: Control pile cap detail for Larosche et al. [18]: (a) Elevation; (b) Section A-A; (c) Section B-B views; (d) picture of reinforcement cage for Specimen EB-1824
Figure 2.17: Modifications to pile cap design for Larosche et al. [18] for: (a) EB-26; (b) EB-2224
Figure 2.18: Cap reinforcement details from Kappes et al. [47] with single #7 U-bar in each direction
Figure 2.19: Single #4 and #5 U-bar detail from Kappes et al. [47] for: (a) CT1 exterior only; (b) CT2 exterior and interior

Figure 2.20: Test setups from previous research: (a) Harries and Petrou [12] (elevation); (b) Shahawy and Issa [20] (elevation); (c) Xiao [45] (elevation); (d) Issa [2] (plan); (e) Larosche et al. [18] (plan)
Figure 2.21: Procedure for measuring curvature in hinge region with LVDTs29
Figure 2.22: Location of VWGs at Section A-A for: (a) ElBatanouny et al. [14]; (b) Shahawy and Issa [20]
Figure 2.23: LVDTs used by Shahawy and Issa [20] to measure strand slip (a) elevation; (b) section A-A; (c) Section B-B
Figure 3.1: (a) Construction of a bridge with tall pile bents (courtesy of Corven Engineering); (b) schematic of unstable bent with assumed pinned connection
Figure 3.2: Section of interior bent for Bridge #1
Figure 3.3: Elevation of Bridge #1
Figure 3.4: FDOT design aid for Florida-I beams [49]
Figure 3.5: General properties for FIB-45 [49]
Figure 3.6: Strand layout for: (a) 100-ft span; (b) 40-ft span
Figure 3.7: Typical cross section dimensions for pier caps
Figure 3.8: Details for 18-inch square prestressed concrete pile used in Bridge #1[51]37
Figure 3.9: Assumed construction procedure for Bridge #1
Figure 3.10: Sample model for Bridge #1 with construction stages analyzed
Figure 3.11: Possible assumed connections between pile and pile cap: (a) fixed; (b) pinned; (c) pinned with rotational spring
Figure 3.12: Stiffness of rotational spring determined from: (a) M- θ ; (b) numerical results assuming kinetic rotation about a hinge at the connection
Figure 3.13: Moment versus rotation plot for 18-inch pile with 0.25d _b pile embedment from numerical analyses
Figure 3.14: Boundary conditions for Bridge #1: (a) supports; (b) soil-structure interaction40
Figure 3.15: Bridge #1 modeling assumptions: (a) elements intersecting between spans at pile caps; (b) representation of elements and links between elements at this location
Figure 3.16: Moment response for select piles in Bridge #1 at: (a) Construction Stage 1; (b) Construction Stage 2
Figure 3.17: Moment response for beams in Bridge #1 at Construction Stage #242
Figure 3.18: Moment response for select piles in Bridge #1 at: (a) CS4a; (b) CS4b42
Figure 3.19: Moment response for beams in Bridge #1 at: (a) CS4a; (b) CS4b43
Figure 3.20: Moment response in: (a) composite beam; (b) piles for Bridge #1 with continuous deck in service (Construction Stage 5)

Figure 3.21: Moment response in: (a) composite beam; (b) piles for Bridge #1 with non-continuous deck in service (Construction Stage 5)44
Figure 3.22: Wekiva River Bridge: (a) fixed pier table; (b) bridge elevation [52]44
Figure 3.23: Typical section for Bridge #2
Figure 3.24: Elevation of Bridge #2 with: (a) equal spans; (b) balanced cantilever configuration.
Figure 3.25: Pile cap location for Bridge #2: (a) at water line; (b) at soil level46
Figure 3.26: AASHTO-PCI ASBI Standard 2100-1 box beam [53]47
Figure 3.27: Details for: (a) 24-inch; (b) 30-inch square prestressed concrete piles used in Bridge #2 [51]
Figure 3.28: Pile cap details: (a) Plan view; (b) Cross-section
Figure 3.29: Pier cross-section
Figure 3.30: Bridge #2 with: (a) all equal spans; (b) balanced cantilever configuration49
Figure 3.31: Boundary conditions for half of structure (showing Pier 1) with: (a) pile cap at water level; (b) pile cap at soil level
Figure 3.32: Axial load response for Bridge #2 with all equal spans for select piles supporting the loaded pier for: (a) pile cap at water level; (b) pile cap at soil level
Figure 3.33: Moment (z direction) response for Bridge #2 with all equal spans for select piles supporting the loaded pier for: (a) pile cap at water level; (b) pile cap at soil level
Figure 3.34: Pile cap details for 4x5 grid of 30-inch piles: (a) plan view; (b) cross-section52
Figure 3.35: Axial load response for Bridge #2 4x5 grid with all equal spans for select piles supporting the loaded pier for: (a) pile cap at water level; (b) pile cap at soil level
Figure 3.36: Moment (y direction) response for Bridge #2 4x5 grid with all equal spans for select piles supporting the loaded pier for: (a) pile cap at water level; (b) pile cap at soil level
Figure 3.37: Pile cap details for 5x5 grid (a) plan view (b) cross-section
Figure 3.38: Axial load response for Bridge #2 5x5 grid with all equal spans for select piles supporting the loaded pier for: (a) pile cap at water level; (b) pile cap at soil level
Figure 3.39: Moment (z direction) response for Bridge #2 5x5 grid with all equal spans for select piles supporting the loaded pier for: (a) pile cap at water level; (b) pile cap at soil level
Figure 3.40: Maximum moment for piles supporting the loaded pier for pile cap at water and soil level
Figure 3.41: Final geometry for Bridge#2: (a) water-level pile cap; (b) soil-level pile cap57
Figure 3.42: Moment (z direction) response for Bridge #2 with all equal spans for laterally loaded piers for: (a) pile cap at water level; (b) pile cap at soil level
Figure 3.43: (a) Shear (y direction); (b) moment response for Bridge #2 with all equal spans and water-level pile caps along length of beam

Figure 3.44: Straddle bent (courtesy of Corven Engineering)
Figure 3.45: Details for Bridge #3
Figure 3.46: Pile cap details: (a) plan view; (b) cross-section60
Figure 3.47: Details for 18-inch square prestressed concrete pile used in Bridge #3 [51]60
Figure 3.48: Straddle beam cross-section
Figure 3.49: Long-term properties: (a) creep coefficient for 5.5 ksi; (b) shrinkage strain for 5.5 ksi.
Figure 3.50: Four load cases investigated for Bridge #3: (a) uniform temperature, no vertical load; (b) uniform temperature with vertical load; (c) temperature gradient, no vertical load; and (d) temperature gradient with vertical load
Figure 3.51: Boundary conditions for Bridge #3: (a) supports; (b) soil-structure interaction63
Figure 3.52. Bridge #3 model with uniform element temperature: (a) without vertical load; (b) with vertical load
Figure 3.53: Bridge #3 with temperature gradient: (a) without vertical load; (b) with vertical load.
Figure 3.54: Post-tensioned loading for Bridge#364
Figure 3.55: Axial load response for Bridge #3 piles with: (a) uniform temperature only; (b) uniform temperature with vertical applied load
Figure 3.56: Moment response for Bridge #3 piles with: (a) uniform temperature only; (b) uniform temperature with vertical applied load
Figure 3.57: (a) Axial load; (b) moment response for Bridge #3 columns with uniform temperature only
Figure 3.58: (a) Typical section for Bridge #4; (b) elevation of balanced cantilever configuration.
Figure 3.59: Post-tensioned segmental box girder bridge with fixed pier table
Figure 3.60: Imposed deflection at cut in half-bridge model
Figure 3.61: Pile layouts used for Bridge #4 with: (a) 3x4 grid of 18-inch piles; (b) 2x4 grid of 24-inch piles; (c) 2x3 grid of 30-inch piles
Figure 3.62: Bridge #4 modeling
Figure 3.63: Boundary conditions for Bridge #469
Figure 3.64: Axial load response for select piles in Bridge #4 with: (a) 3x4 grid of 18-inch piles; (b) 2x3 grid of 30-inch piles70
Figure 3.65: Moment response for select piles in Bridge #4 with: (a) 3x4 grid of 18-inch piles; (b) 2x3 grid of 30-inch piles70
Figure 3.66: (a) Axial load; (b) moment response for pier in Bridge #471

Figure 4.1: Example of: (a) AutoCAD model; (b) ATENA model used for pile-to-cap connection models
Figure 4.2: Sample of Master-Slave conditions used at interfaces between volume elements73
Figure 4.3: Reinforcement layout for typical pile-to-pile cap connection specimens73
Figure 4.4: Stress-strain curve: (a) Reinforcement; (b) tendons74
Figure 4.5: Test configuration used for modeling connection specimens: (a) without axial load application; (b) with axial load application
Figure 4.6: Boundary conditions: (a) plates; (b) restrictions75
Figure 4.7: Load Stage #1: (a) defined materials; (b) applied prestrain of -0.007 per step in prestressing strands
Figure 4.8: (a) Axial load applied during Load Stage #2; (b) lateral load applied during Load Stage #3
Figure 4.9: Sample mesh for pile-to-cap connection analyses
Figure 4.10: Moment-curvature response for: (a) 18-inch; (b) 24-inch; (c) 30-inch piles (highlighted capacities for piles with 0.5-inch strands)
Figure 4.11: Moment-axial load response for: (a) 18-inch; (b) 24-inch; (c) 30-inch piles79
Figure 4.12: Sample moment versus deflection responses for 18-inch piles: (a) without; (b) with interface reinforcement with varying embedment length
Figure 4.13: Sample moment versus embedment length responses for 18-inch piles: (a) without; (b) with interface reinforcement
Figure 4.14: Sample crack patterns for 18-inch piles without interface reinforcement with: (a) 0.25d _b ; (b) 1.5d _b embedment length
Figure 4.15: Normalized moment versus embedment length for: (a) 18-inch; (b) 24-inch; (c) 30-inch piles without interface reinforcement.(P=0, f'c, pile=6 ksi, f'c cap= 5.5 ksi)
Figure 4.16: Normalized moment versus embedment length for: (a) 18-inch; (b) 24-inch; (c) 30-inch piles with interface reinforcement. (P=0, f' _{c, pile} =6 ksi, f' _{c cap} = 5.5 ksi)
Figure 4.17: Location of interface steel layout in: (a) 18-inch; (b) 24-inch; (c) 30-inch square prestressed piles
Figure 4.18: Normalized moment versus embedment length for pile-to-cap connections: (a) without; (b) with interface reinforcement
Figure 4.19: Idea for pinned connection between pile and pile cap: (a) cross-section; (b) elevation.
Figure 4.20: Sample moment versus deflection responses for 30-inch piles with: (a) shallow (0.25d _b); (b) deep (1.5d _b) embedment with varying axial load
Figure 4.21: Sample moment versus deflection responses for 30-inch piles: (a) without; (b) with interface reinforcement with varying axial load

Figure 4.22: Sample moment versus deflection responses for 30-inch piles with: (a) shallow $(0.25d_b)$; (b) deep $(1.5d_b)$ embedment with varying pile concrete strength. (f'c, cap = 5.5 ksi)86
Figure 4.23: Sample moment versus deflection responses for 18-inch piles with: (a) shallow $(0.25d_b)$; (b) deep $(1.5d_b)$ embedment with axial compression and varying pile cap concrete strength.(f'c, pile = 6.0 ksi)
Figure 4.24: Sample moment versus deflection responses for 18-inch piles with: (a) shallow $(0.25d_b)$; (b) deep $(1.5d_b)$ embedment with axial tension and varying pile cap concrete strength. (f' _{c, pile} = 6.0 ksi)
Figure 4.25: Investigated pile cap sizes for analytical program
Figure 4.26: Sample moment versus deflection responses for 30-inch piles with: (a) shallow $(0.25d_b)$; (b) deep $(1.5d_b)$ embedment with different pile cap sizes
Figure 4.27: Sample moment versus deflection responses for 18-inch piles with: (a) shallow $(0.25d_b)$; (b) deep $(1.5d_b)$ embedment with and without confinement reinforcement around embedded pile
Figure 4.28: Sample moment versus deflection responses for 18-inch piles with: (a) shallow $(0.25d_b)$; (b) deep $(1.5d_b)$ embedment with different strand patterns
Figure 4.29: Maximum stress in prestressing strands in 24-inch piles with different embedment lengths
Figure 5.1: Details for: (a) 18-inch; (b) 30-inch pile sizes
Figure 5.2: Details of proposed interface reinforcement for testing
Figure 5.3: Typical details for: (a) 18-inch; (b) 30-inch piles94
Figure 5.4: Pile cap dimensions for 18-inch and 30-inch piles
Figure 5.5: General pile cap dimension details: (a) plan; (b) elevation views
Figure 5.6: Sample cover requirements from FDOT Structures Design Guidelines [5]97
Figure 5.7: Typical pile cap reinforcement from Larosche et al. [18]
Figure 5.8: Schematic of pile cap reinforcement scheme used by Issa [2]: (a) plan; (b) elevation views
Figure 5.9: Photograph of pile cap reinforcement used by Issa [2]
Figure 5.10: Sample pile cap reinforcement from: (a) UPRR Bridge 126.31; (b) Burnt River Bridge projects
Figure 5.11: Pile cap reinforcement: (a) primary tension; (b) vertical skin; (c) horizontal skin reinforcement
Figure 5.12: Interior pile cap reinforcement: (a) horizontal; (b) vertical; (c) embedded pile confinement reinforcement
Figure 5.13: (a) Moment demand on pile cap for piles being pushed together; (b) cross section with 18-inch pile; (c) cross section with 30-inch pile

Figure 5.14: (a) Moment demand on pile cap for piles being pushed apart; (b) cross section with 18-inch pile; (c) cross section with 30-inch pile
Figure 5.15: (a) Engagement of longitudinal reinforcement around pile; (b) cross section of typical longitudinal reinforcement; (c) cross section with possible bar bundling if reinforcement engagement does control
Figure 5.16: Investigated options for test setup: (a) rear support; (b) top support; (c) self-reacting frames
Figure 5.17: Schematic of proposed test setup: (a) elevation; (b) plan view104
Figure 5.18: Numerical analyses for test setup105
Figure 5.19: (a) Tie down point to strong floor; (b) setup for axial load application105
Figure 5.20: Threaded rods configuration106
Figure 5.21: (a) Experimental procedure without axial load; (b) numerical modeling results for shallow embedment for 18-inch piles; (c) numerical modeling results for shallow embedment for 30-inch piles
Figure 5.22: Experimental procedure with axial load: (a) application of axial load; (b) application of lateral load
Figure 5.23: Deflection gauges (LVDT) and load cells (top view)
Figure 5.24: Plastic hinge zone observation assumptions110
Figure 5.25: CDT in the plastic hinge zone
Figure 5.26: ATENA modeling for specimens: (a) shallow embedment; (b) deep embedment. 111
Figure 5.27: Concrete surface gauges: (a) side view; (b) front view111
Figure 5.28: Stress in rebars: (a) N6 bars; (b) N5 bars; (c) N9 bars
Figure 5.29: Rebar strain gauges: (a) side view; (b) front view
Figure 5.30: Vibrating wire strain gauges
Figure 5.31: Proposed location for the fiber optic sensors
Figure 5.32: 18-inch specimen construction: (a) pile casting; (b) pile cap casting
Figure 5.33: Construction of the 30-inch specimens: (a) pile casting at CDS; (b) pile cap casting at FDOT SRC
Figure 5.34: Standard slump flow test for SP-10: (a) inverted mold; (b) slump of 25 inches118
Figure 5.35: Temperature readings: (a) SP-09; (b) SP-10119
Figure 5.36: Temperature gradient: (a) SP-09; (b) SP-10119
Figure 5.37: Finished 30-inch specimens: (a) SP-09; (b) SP- 10
Figure 5.38: Test setup for specimens without axial load application120
Figure 5.39: Test setup for specimens with axial load application121
Figure 5.40: Axial load application: (a) tensioning of west pile; (b) tensioning east pile

Figure 5.41: Flexure test pile setup123
Figure 5.42: (a) Load versus displacement; (b) moment versus displacement curves for Pile 1 and Pile 2
Figure 5.43: Average measured strain profile in constant moment region for: (a) Pile 1; (b) Pile 2
Figure 5.44: Measured and estimated moment versus curvature response for Pile 1 and Pile 2.125
Figure 5.45: Estimated moment versus curvature for 30-inch piles using RESPONSE2000125
Figure 5.46: 95% average maximum strain (AMS) method for determining transfer length from Russell and Burns [61]
Figure 5.47: Sample of data processing steps taken: (a) removing extraneous points; (b) zeroing based on first relevant point; (c) smoothing data and determining AMS; (d) determining transfer length
Figure 5.48: Location of applied lateral load134
Figure 5.49: Moment versus displacement curves for: (a) 18-inch; (b) 30-inch pile specimens.136
Figure 5.50: Expected failure mechanisms of the pile-to-cap connection: (a) development length of prestressing strand; (b) shear friction capacity between the pile and pile cap; (c) bearing between the pile and cap
Figure 5.51: Photographs after failure for: (a) SP-04; (b) SP-03 with observed strand development failure
Figure 5.52: SP-09 strand development failure: (a) SP-09 failure; (b) after removing spalled concrete in the cap
Figure 5.53: SP-09 failure: (a) pile slipping out of pile cap; (b) damage in pile cap
Figure 5.54: SP-10 failure: (a) pile slipping out of pile cap; (b) punching shear failure139
Figure 5.55: SP-10 rebar strain data for N5 bars140
Figure 5.56: Punching shear cracking observed in: (a) SP-06; (b) SP-08; (c) SP-09140
Figure 5.57: Load versus rebar strain for pile cap reinforcement around the west embedded pile for: (a) SP-06; (b) SP-08
Figure 5.58: Load versus rebar strain for pile cap reinforcement around the west embedded pile for SP-09
Figure 5.59: Assumed rigid body rotation of pile during testing with typical damage at failure highlighted
Figure 5.60: Examples of spalling of concrete on compression face of pile for: (a) SP-04; (b) SP-05; SP-08 during failure
Figure 5.61: Sample displacement versus distance from cap for: (a) SP-01; (b) SP-04143
Figure 5.62: Moment versus rotation responses for: (a) 18-inch; (b) 30-inch pile specimens143
Figure 5.63: Moment-displacement curves for the 18-inch specimens

Figure 5.64: Moment versus curvature response for 18-inch specimens1	46
Figure 5.65: Flexural cracks in piles after testing for: (a) SP-07; (b) SP-081	46
Figure 5.66: Load versus concrete strain on the edge of the pile cap for: (a) SP-01; (b) SP-08 (as have different scales)	kes 47
Figure 5.67: Load versus concrete strain on the side face of the pile cap for: (a) SP-01; (b) SP-(axes have different scales)1	.08 47
Figure 5.68: Load versus rebar strain for pile cap reinforcement around the embedded piles f (a) SP-01; (b) SP-081	or: 48
Figure 5.69: Load versus rebar strain for pile cap reinforcement around the embedded piles f (a) SP-01; (b) SP-081	or: 48
Figure 5.70: Load versus rebar strain for reinforcement along the west face of the pile cap for: SP-01; (b) SP-08	(a) 49
Figure 5.71: Maximum strains in reinforcement in west face of the pile cap for SP-081	49
Figure 5.72: Idealized relationship between strand stress and distance from free end of strand [3]. 52
Figure 5.73: Estimated strand stress versus development length for 18-inch and 30-inch piles fou using AASHTO LRFD BDS equations1	nd 52
Figure 5.74: Bilinear relationship used for strand stress for ElBatanouny and Ziehl [4]1	57
Figure 5.75: Stress in strand versus available development length plots for: (a) 18-inch; (b) 3 inch pile specimens	30- 59
Figure 5.76: Punching shear failure in pile-to-cap connections1	59
Figure 5.77: Bearing stresses proposed by Mattock and Gaafar [42]1	60
Figure 5.78: Assumed strain distribution and stress block for pile embedment1	62
Figure 5.79: Measured compression strains on outside edge of pile caps for: (a) SP-09; (b) SP-1	10. 63
Figure 5.80: Typically assumed punching shear cracking and critical shear perimeter for: interior column; (b) edge column; (c) typical punch shear theory extended to embedded pile a pile cap edge	(a) ind 64
Figure 5.81: Reinforcement in 30-inch pile caps: (a) all reinforcement; (b) Bar 2A (#9 bars) rel provided1	bar 65
Figure 5.82: Assumed 45-degree spread for punching shear failure	66
Figure 5.83: Photographs after failure of SP-021	68
Figure 5.84: Moment-displacement for specimens with axial load: (a) 6-inch embedment leng (b) 9-inch embedment length1	th; 68
Figure 5.85: Moment versus curvature plots for: (a) 18-inch; (b) 30-inch piles with different lev of applied axial load. (f' _{c, pile} = 12 ksi)1	els 69

Figure 5.86: Measured concrete strains on the west side face of the pile cap in: (a) SP-01; 02 with 6-inch pile embedment lengths.	(b) SP- 170
Figure 5.87: Measure pile cap longitudinal reinforcement strain for: (a) SP-01; (b) SP-02 inch pile embedment lengths.	with 6- 170
Figure 5.88: Details of interface reinforcement for SP-03: (a) elevation; (b) Section A-A	171
Figure 5.89: Photographs of the failure of SP-03.	172
Figure 5.90: Strains along the east side of the west pile measured by FOS for SP-03	172
Figure 5.91: Moment versus displacement curves for 18-inch pile with 6-inch embedme and without interface reinforcement .	nt with 174
Figure 5.92: Load versus rebar strain for transverse pile cap reinforcement in the connecti for: (a) SP-01; (b) SP-03.	on face
Figure 5.93: Load versus rebar strain for longitudinal pile cap reinforcement in the connecti for: (a) SP-01; (b) SP-03.	on face
Figure 5.94: Load versus rebar strain for transverse pile cap reinforcement in the west si for: (a) SP-01; (b) SP-03	de face
Figure 5.95: Moment versus curvature measured using the crack displacement transducers SP-01; (b) SP-03.	for: (a)
Figure 6.1: Numerical models geometry: (a) AutoCAD drawing; (b) ATENA model	178
Figure 6.2: Reinforcement scheme in piles and pile cap	178
Figure 6.3: Material properties: (a) solid materials; (b) 1D reinforcement	179
Figure 6.4: Stress-strain relationship: (a) reinforcing steel; (b) strands	181
Figure 6.5: Test configuration used for modeling connection specimens	183
Figure 6.6: Boundary conditions	184
Figure 6.7: Load protocol: (a) load stage #1; (b) load stage #2; (c) load stage #3	184
Figure 6.8: Finite element mesh for pile-to-cap model: (a) tetrahedra elements; (b) here elements.	xahedra 186
Figure 6.9: Size of finite element mesh for the 18-inch pile-to-cap model: (a) 1 inch; (b) 2 (c) 3 inches	inches; 186
Figure 6.10: Analytical bond stress-slip relationship by CEB-FIP model code 1990 [71]	187
Figure 6.11: CEB-FIB 1990 Model Code bond strength-slip relationship	189
Figure 6.12: SP-01 moment-displacement results with CEB-FIB 1990 bond model	190
Figure 6.13: Bond law by Bigaj (1999) [72].	190
Figure 6.14: Bigaj (1990) bond strength-slip relationship.	191
Figure 6.15: SP-01 moment-displacement results with Bigaj (1990) bond model	192
Figure 6.16: Predicted bond model by Aly et al. [75]	193

Figure 6.17: Moment-displacement results for 18-inch specimens with Modified Bond Model 1. 196
Figure 6.18: Moment-displacement results for 18-inch specimens with Modified Bond Model 2.
Figure 6.19: Modified Bond Model 1 and Modified Bond Model 2 for bond-slip relationship of strands
Figure 6.20: Cracking pattern SP-01: (a) failure mechanism; (b) numerical model
Figure 6.21: Cracking patterns SP-08: (a) failure mechanism; (b) numerical model200
Figure 6.22: Cracking pattern SP-10: (a) failure mechanism; (b) numerical model200
Figure 6.23: Relationship between moment capacity and embedment length for 18-inch specimens
Figure 6.24: Crack pattern of EMB-42
Figure 6.25: Rebar detail recommendation for punching shear
Figure 6.26: Numerical results for EMB-42 with additional shear reinforcement203
Figure 6.27: Relationship between moment capacity and embedment length for 18-inch specimens. Results for EMB-42 include additional shear reinforcement around embedded piles
Figure 6.28: FDOT Standard Plans for piles: (a) 18-inch pile cross section; (b) alternate strand patterns
Figure 6.29: Estimated moment versus curvature for 18-inch piles with 0.6-inch strands using RESPONSE2000
Figure 6.30: Stress in strand versus available development length plots for 0.6-inch strand pattern. 206
Figure 6.31: Stress in strand versus available development length plots using: (a) AASHTO LRFD BDS; (b) ElBatanouny and Ziehl [4]
Figure 6.32: Moment versus displacement curves for 18-inch models with different pile cap concrete strength
Figure 6.33: Crack pattern of specimen with 9-inch embedment length: (a) SP-04 with pile cap concrete strength 12 ksi; (b) PC-04 with pile cap concrete strength 5.5 ksi
Figure 6.34: PC-08 failure mechanism: (a) before reaching maximum load; (b) at maximum load; (c) after reaching maximum load
Figure 6.35: Numerical results for PC-08 with additional shear reinforcement: (a) moment- curvature response; (b) crack pattern
Figure 7.1: Stress in strand versus available development length plot for: (a) 18-inch piles; (b) 30-inch piles
Figure 7.2: Pile moment capacity versus embedment length using AASHTO Modified for (a) 18- inch piles with ½" (special) strands (b) 30-inch piles with ½" (special) strands

Figure 7.7: Moment versus rotation plot for 18-inch pile with 6 inches embedment length2	17
Figure 7.8: Linear relationship between rotational stiffness versus embedment length: (a) 18-in piles, (b) 30-inch piles	ch 18
Figure 7.9: Aaleti and Sritharan [76] pile cap reinforcement detail	20
Figure 7.10: Additional reinforcement detail for punching shear control2	20
Figure 7.11: Assumed 45-degree spread for punching shear failure with N6 bar: (a) elevation vie of 18-inch specimen; (b) plan view of 18-inch specimen	ew 21

LIST OF TABLES

No table of figures entries found.

Chapter 1: Introduction

1.1 BACKGROUND

Foundations for many bridges consist of driven piles embedded in pile caps or footings whereby axial loads, lateral loads, and moments are transferred from the bridge to underlying soil and/or bedrock. Piles can also be subjected to large lateral deflections in the event of an earthquake or vessel impact, which can result in high local curvature and moment demands at various locations along the pile lengths.

The connection between the pile and pile cap or footing will affect the way forces are transferred through the bridge. Bridge superstructure can transfer axial loads, lateral loads, and moments. This connection is typically either assumed to be (1) a pinned connection, allowing for transfer of axial and lateral forces but no moments, permitting some rotation to eliminate excessive moment build-up, (2) or a fixed connection, allowing transfer of axial and lateral forces and development of the full moment capacity of the pile. The assumed connection between the pile and pile cap or footing will impact the stresses in the rest of the structure.

Currently, 24 states specify a required pile embedment length into the cast-in-place (CIP) footing or pile cap. Three of these states (Florida [5], Minnesota [6], and Wisconsin [7]) specify a pile embedment length for pinned connections of 0.5 feet or 1.0 foot. Six of these states ([5], [7], [8], [9], [10], [11]) specify a pile embedment length for fixed connection between 1.0 foot and 4.0 feet with two states [9], [8] calculating required pile embedment lengths based on the plastic moment capacity of the pile about the strong axis, concrete compressive strength, and width of the pile. The other states specify a required embedment length, but do not clarify in their specification whether that embedment detail will lead to a pinned or fixed connection behavior.

Past research, [12]-[13] has shown that even short embedment lengths (0.5 times the pile diameter or less) can achieve significant moment capacity (up to 40 to 60 percent of the moment capacity). Past researches [12], [1], [14] have also found that the full moment capacity can be developed with embedment lengths much shorter than the 4-foot embedment required by some states.

Assuming a different level of fixity between pile and pile cap or footing can lead to undesirable behavior of a structure. The disconnect between current design provisions and past research would suggest that many structures may have a different level of actual fixity between piles and pile caps or footing than assumed.

Engineers currently use these assumptions to design the connection between pile and footing or pile cap, which influences the design of the rest of the structure. Recent research has shown these assumptions are unrealistic and can be unconservative under certain circumstances, e.g., a fixed connection can be achieved with a much shorter embedment length. A better understanding of the connection between prestressed concrete piles and CIP footings and pile caps is needed to ensure designs are completed correctly and conservatively.

1.2 OBJECTIVES

The primary objective of this research was to better understand the connection between the pile and pile cap or footing to provide better design guidance to engineers and allow for more informed design reviews. This primary objective required the following objectives:

- 1. Determine the required pile embedment length and detail to achieve pinned connection.
- 2. Determine the required pile embedment length and detail to achieve fixed connection.

3. Estimate the level of partial fixity for embedment lengths between pinned and fully fixed connections.

1.3 TASKS

These objectives were accomplished through the following research tasks:

- Task 1 Literature Review: An extensive literature search was conducted to understand the current state of knowledge and practice for pile-to-cap or footing connections. Previously completed research was reviewed and summarized and was used to plan appropriate analytical studies and experimental testing.
- 2. **Task 2 Matrix of Parameters to Study:** A matrix of parameters was created to study in the analytical and experimental program. This matrix was based on previous research (gathered in the literature review), an understanding of the mechanism affecting the moment capacity of the connection, state of current practice in Florida and other states, and the types of structures most sensitive to the fixity level of the connection.
- 3. Task 3 Preliminary Computational Analysis Results: The primary objective of this task was to conduct computational analysis to predict the required embedment length and details for fixed and pinned connections, to determine the primary and secondary variables impacting the behavior of the connection, and to determine the impact of pile-to-cap fixity assumptions on the design and behavior of sensitive structures.
- 4. *Task 4 Test Procedures and Instrumentation Plans:* The overall objective of the experimental testing was to determine the levels of fixity for various pile embedment lengths and the impact of any other primary variable. The primary objective of this task was to select the specimens to be experimentally tested, develop the test procedures for the experimental testing, and develop an instrumentation plan for the specimens.
- 5. *Task 5 Construction Plans and Specifications for Experimental Test Specimens:* This task involved the development of the construction plans and specifications for the experimental test specimens. Sufficient details were provided for successful construction of the test specimens.
- 6. *Task 6 Experimental Test Specimens Material Delivered:* The primary objective of this task was to have all the materials for the construction of the test specimen delivered to the FDOT SRC.
- Task 7 Experimental Test Results and Conclusions: During this task all the specimens were tested in FDOT SRC and the results were analyzed. The results of the testing were conceptually and analytically evaluated and were used to validate and calibrate the results from the numerical models. The results were also used to determine the relationship between embedment length and level of fixity.
- 8. *Task 8 Demolition and Removal of Test Specimens:* The primary objective of this task was to demolish and dispose of the test specimens.
- 9. *Task 9 Final Computational Analysis Results:* During this task the computational analyses conducted during Task 3 were refined and expanded where needed.
- 10. *Task 10 Design Guidance and Visual Aids:* Results from the computational analysis and experimental testing were used to predict the level of moment transfer for various embedment lengths.
- 11. *Task 11 Draft Final and Closeout Teleconference:* A final report was developed to summarize the work and findings from this project.

Chapter 2: Literature Review on Pile-to-Cap Connections

The foundation for many bridges in Florida consists of driven piles embedded in pile caps or footings. Piles transfer axial loads and moments from the bridge into the soil and bedrock. Piles can also be subjected to large lateral deflections in the event of an earthquake, which can result in high local curvature and moment demands at various locations along the pile length. Similar demand on the connections can occur during a barge impact. The typical construction procedure for this type of foundation is shown in Figure 2.1 and involves the following steps:

- 1. Precast piles are driven to a sufficient depth based on end bearing and side friction capacities, as shown in Figure 2.1 (a). The length that the pile needs to be driven may be different from pile to pile, which may even require pile splicing to achieve longer pile lengths.
- 2. After all the piles have been driven, the tops of the piles are cut off, so the piles all have the same length extending from the ground, shown in Figure 2.1 (b). This length is based on the connection detail between the precast piles and pile cap or footing, specifically the required embedment length.
- 3. Reinforcement is placed and formwork installed around the precast piles to construct the cast-in-place pile cap or footing, shown in Figure 2.1 (c). Some states require interface reinforcement between precast pile and pile cap or footing, which would be installed at this time.



Figure 2.1: Typical construction procedure for piles with cast-in-place pile cap.

The connection between the pile and pile cap or footing will affect the way forces are transferred through the bridge. Bridge superstructures can transfer axial loads, lateral loads, and moments, as shown in Figure 2.2 (a). This connection is typically either assumed to be a pinned connection, allowing for transfer of axial and lateral forces but no moments, or a fixed connection, allowing transfer of axial and lateral forces and development of the full moment capacity of the pile, as shown in Figure 2.2 (b) and (c) respectively. The assumed connection between the pile and pile cap or footing will impact the stresses in the rest of the structure.



Figure 2.2: (a) Forces from the above structure assumed to be transferred to piles either through (b) pinned or (c) fixed connections.

2.1 TYPES OF PRECAST PILE-TO-CAP CONNECTIONS

There are several different options for connecting precast piles to cast-in-place concrete pile caps or footings. These connections can be broken into four main categories, as shown in Figure 2.3:

- 1. *Plain embedment*: This connection consists of the pile embedded directly into the pile cap with no reinforcement connecting the pile-to-pile cap. The surface of the pile can remain untreated or can also be intentionally roughened to different magnitudes.
- 2. *Vertical or horizontal dowels*: Reinforcement can be extended from the pile into the pile cap. This reinforcement can be either vertical or horizontal and can be straight or hooked. Spiral reinforcement can also be provided around the dowels to improve their development behavior. These connections typically have shorter pile embedment lengths than plain embedment.
- 3. *Pile development with spirals*: square or round spirals can be placed around the embedded pile to improve pile development. The pile can either be untreated or have an intentionally roughened surface.
- 4. *Exposed strands*: strands from the pile can be exposed and either broomed, as shown in Figure 2.3 (d) or extended straight into the cap and enclosed with spirals, similar to what is shown in Figure 2.3 (c). This type of connection typically has a shorter embedment length.



Figure 2.3: Types of pile embedment details (modified from [12] and [15]).

2.2 PINNED CONNECTION BETWEEN PILE AND CAP

A pinned connection between pile and pile cap is typically required to have a positive connection between the pile and cap while still permitting some rotation to eliminate excessive moment build-up [15]. FDOT specifies a 12-inch design embedment for pinned connections [5], which is based on a rule of thumb. The FDOT tolerance for vertical elevation of the pile head is 4-inch, which can result in a minimum 8-inch as-built embedment. Other states typically require pinned connections to be achieved with embedment lengths between 6 and 12 inches [15].

2.2.1 Summary of Past Research

There is limited research on specifically developing a pinned connection between pile and pile cap. Rollins and Stenlund [1] experimentally investigated two connections with shallow embedment (0.5 to 1.0 times the pile diameter) with a reinforcement cage connection and two deeper embedment (1 to 2 times the pile diameter) with no reinforcement cage connection, shown in Figure 2.4. They found that the shallow embedment still developed at least 40 to 60 percent of the moment capacity of the pile.



Figure 2.4: Embedment details for Rollins and Stenlund [1] specimens; (a) with and (b) without interface steel.

Xiao [16] tested three full-scale prestressed concrete pile-to-cap connections: two with constant axial load and cyclic lateral load and one with no lateral load and cyclic axial load. These connections were all shallow embedment lengths with dowel bars extending from the pile into the pile cap, shown in Figure 2.5 (a). Xiao found that a significant moment and rotation could be achieved with the shallow embedment and reinforcement. Xiao also found that there was no degradation in behavior caused by cycling the axial load.



Figure 2.5: Embedment details for (a) Xiao [16] and (b) Harries et al. [12]

Xiao et al. [16] tested pile-to-cap connections for steel HP piles with shallow embedment lengths and diagonal dowel bars extending from the piles into the cap, shown in Figure 2.5 (b). This connection was expected to behave more like a hinge, only developing approximately 6 percent of the plastic moment capacity of the pile based on Shama et al.[13], but ended up developing between 25 and 66 percent of the plastic moment capacity of the pile.

2.3 FIXED CONNECTION BETWEEN PILE AND PILE CAP

The typical objective for the connection between the pile and pile cap is to provide a connection capable of developing the moment capacity of the pile [12]. An additional objective is to ensure the connection is rigid enough so that rotation of the pile within the cap does not significantly contribute to the overall drift of the assembly [12]. This fixed connection can be developed using any of the connection types shown above in Figure 2.3 by a combination of the below methods:

- 1. Providing sufficient embedment length,
- 2. Roughening the surface of the pile,
- 3. Providing spirals around the embedded portion of the pile, and
- 4. Using mechanical shear connectors or supplemental mild steel reinforcement. [15]

However, Joen and Park [17] found that embedding the pile into the pile cap was the easiest to construct and resulted in the least damage to the pile cap. Primarily because of its ease of construction, a plain pile embedment into a pile cap is typically used to achieve a moment connection.

2.3.1 Required Behavior and Mechanism

Several different mechanisms can control the moment capacity, as shown in Figure 2.6. Each of these failure mechanisms must be prevented to develop the moment capacity of the pile:

- 1. *Slip of prestressing strands in embedded pile*: The available development of the strands must be sufficient to fully develop the prestressing force in the strands.
- 2. *Slip between pile and pile cap*: The shear friction capacity at the cold joint between the precast pile and cast-in-place cap must be sufficient so that slip does not occur at the interface before the moment capacity of the pile is achieved.
- 3. *Bearing failure between pile and pile cap*: If the compression strength in the pile cap is not sufficient, then the concrete will crush at the interface.



Figure 2.6: Failure of this connection can be controlled by (a) development length of the prestressing strand, (b) shear friction capacity between the pile and pile cap, and (c) bearing between the pile and cap.

Each of these mechanisms will be discussed in more detail in the following sections. Note that the shear friction capacity, shown in Figure 2.6 (b), seems to become an influential factor in tension piles.

2.3.2 Summary of Past Research

Several different researchers have previously investigated this type of connection using different types of piles, different sizes of piles, and different loading configurations. A summary of the results from some of these studies is shown in Table 2.1. The current FDOT recommended embedment length to achieve the full moment capacity of prestressed concrete piles is 48 inches [5]. This is based on experimental testing conducted by Issa [2] on square 30-inch prestressed concrete piles with an internal pipe void. Issa [2] tested two pile-to-pile cap connections with the piles embedded the entire way through the 48-inch thick pile cap. They found that failure occurred in the pile just outside the connection, so the pile was able to develop its full theoretical bending strength. No axial load was applied to the piles tested in this program. Note that the 48-inch embedment is equal to 1.6 times the pile diameter/depth in this case.

Since this testing was completed, there have been several additional studies from which researchers have concluded that the full moment capacity of the pile can be developed in embedment lengths less than 48 inches: ranging from an embedment length equal to the pile depth to two times the pile depth [1], [12], [18]. These tests were performed on different pile types, diameters, and depths and with either constant or variable axial loads.

Research	Year	Recommended Embedment Length to Develop Full Moment Capacity of Pile	Type of Pile	Pile Size	Notes
Castilla et al. [19]	1984	2 x pile depth or diameter	Steel HP 14x73 and 14x117	14"	Based on results from numerical modeling
Joen and Park [17]	1990	No recommendation made, testing of 2 x pile depth or diameter provided full moment capacity	Octagonal, prestressed concrete	15.7"	Embedded pile surface was roughened; constant axial load; also tested 2 other types of pile-to-cap connections and found embedded pile connection to be best
Shahawy and Issa [20]	1992	50"	Square, prestressed concrete	14"	Added external clamping force with jacks simulating shrinkage of cap; no axial load
Issa [2]	1999	48"	Square, prestressed concrete with internal pipe void	30"	Testing referenced in FDOT Structures Design Guidelines; no axial load
Harries and Petrou [12]	2001	Width of pile; greater than 12 inches	Square, prestressed concrete	18"	Constant axial load
Rollins and Stenlund [1]	2010	Recommend embedment of 24" for their 12" diameter steel pipes (2 x pile depth or diameter)	Steel pipe	12"	Piles were driven to a depth of 40 feet into soil; no externally applied axial load
Larosche et al. [18]	2013	1.3 x pile depth or diameter	Square, prestressed concrete	18"	Variable axial load; cyclic loading

Table 2. 1: Recommended embedment lengths to develop full moment capacity of piles from previous research.

2.4 CURRENT DOTS' RECOMMENDATIONS

2.4.1 Florida Recommendation for Pinned Connections

The FDOT Structures Design Guidelines [5] currently specifies a 1-foot embedment length for a pinned connection, as shown in Figure 2.7. The strand development length is specified to be in accordance with the sections on development length of prestressing strands (§5.11.4) in the AASHTO LRFD Bridge Design Specification [3], as shown in Figure 2.7.



Figure 2.7: (a) FDOT pinned connection details and (b) strand development.

The strand stress can be determined using either Equation 1-2.1 or Equation 1-2.2, depending on if the location of interest is within the transfer length or between the transfer and development lengths.

Within transfer length:
$$f_{px} = \frac{f_{pe}l_{px}}{60d_b}$$
Equation 1-2.2AASHTO LRFD
(5.11.4.2-2)

Patwaan transfar langth	$(l_m - 60d_h)$	Equation 1-2.3
and development length: f_p	$f_{x} = f_{pe} + \left(\frac{l_{px}}{l_d - 60d_b}\right) \left(f_{ps} - f_{pe}\right)$	AASHTO LRFD (5 11 4 2-3)

where:

- f_{px} = design stress in pretensioned strand at nominal flexural strength at section of member under consideration (ksi)
- l_{px} = distance from free end of pretensioned strand to section of member under consideration (in)
- d_b = nominal strand diameter (in)
- f_{ps} = average stress in prestressing steel at the time for which the nominal resistance of the member is required
- f_{pe} = effective stress in the prestressing steel after losses (ksi)
- $l_d =$ development length of the strand required to develop f_{ps} , found using (5.11.4.2-1) (in)

The strand stress development can be used to determine how the moment develops in the pile away from the hinge location.

2.4.2 Florida Recommendations for Fixed Connections

Currently, the prestressed concrete pile embedment length is based on research conducted by Issa [2] and the FDOT Structures Research Center [5], which recommends an embedment length of 4 feet to develop the full bending capacity of the pile as shown in Figure 2.8. The pile must be solid for 8 feet from the end of the pile (i.e., for the 4-foot embedment length and for 4 feet below the bottom of the pile cap).



Figure 2.8: FDOT fixed connection details.

2.4.3 Other DOTS' Recommendations

A summary of the embedment requirements for other states is provided in Table 2.2. The embedment requirements are organized by recommendations for pinned connections and fixed
connections. Several states specify a required embedment length, but do not state whether the required embedment length is for a fixed or pinned connection.

The only states that specify a pile embedment length for pinned connections are Florida (1 foot), Minnesota (1 foot) and Wisconsin (0.5 feet).

State	Embedment Length		Notes	Source	
	Pinned	Fixed	Not specified		
Alaska	-	-	≥ 1' 6"	Only details for Steel H- piles and Steel pipe piles	[21]
Colorado	-	Equation 2.3			[9]
Connecticut	-	-	≥1'		[22]
Delaware	-	-	≥1'	Dowel bars are used for connection with precast piles; minimum embedment is for Steel H-piles	[23]
Florida	1'	4'	-		[5]
Idaho	-	-	1'or 2'	Positive means of anchorage and 1' embedment if uplift is present; 2' for stubby abutments where superstructure is integral with pile cap; 1' without anchorage for most other cases	[24]
Illinois	-	2'	-	Details for reinforcement between Steel H-piles and cap are provided to reduce embedment length	[10]
Illinois Tollway	-	-	1'		[25]

Table 2.2: Embedment details from other DOTs

State	Embedment Length		Notes	Source	
	Pinned	Fixed	Not specified		
Indiana	-	-	1.5'	5' pile embedment is required into the stem of a wall pier with a single row of piles	[26]
Iowa	-	-	2'	1.5' for continuous concrete slab pile bent cap (not monolithic with slab) and 1' when monolithic with slab	[27]
Kansas	-	-	1'	1' embedment into a footing; 2' to 3' embedment into an abutment	[28]
Michigan	-	-	0.5'	1' when a tremie seal is used	[29]
Minnesota	1'	-	-	1' for embedment into a footing; 2.33' for embedment for a low parapet abutment footing	[6]
Montana	-	-	1.58'	Embedment may be reduced by extending reinforcement into the footing	[30]
Nevada	-	-	1'	Larger of 1' and 1.0 x pile width; no roughening of pile is required	[31]
New Hampshire	-	1'	-	Typically extend 1.5' into stub abutments, 2' into integral abutments, and 1' into pier or other footings; CIP piles with reinforcement extending have minimum embedment of 0.5'	[11]

State	Embedment Length		Notes	Source	
	Pinned	Fixed	Not specified		
New York	-	-	1'		[32]
Ohio	-	-	1'	Piles supporting capped pile piers should be embedded 1.5'; substructure units on a single row of piles should be embedded 2'	[33]
Oregon	-	Equation 2.3	-	1' minimum embedment length if lateral load capacity is not needed	[8]
Pennsylvania	-	-	≥1'	1.5' for a single row of piles	[34]
Rhode Island	-	-	≥1'	Piles must be positively anchored into the footing	[35]
South Carolina	-	-	1 x pile width	No roughening of the pile is required; 1.25' minimum embedment for steel pipe pile connection	[36]
Vermont	-	-	≥1'		[37]
West Virginia	-	-	≥1'		[38]
Wisconsin	0.5'	≥2'	-		[7]

	<i>Table 2.2:</i>	Embedment	details	from	other	DOTs-	Continued
--	-------------------	-----------	---------	------	-------	-------	-----------

Washington does not allow precast, prestressed piles for permanent bridge structures. They use cast-in-place concrete piles with a specified reinforcement embedment length from the pile into the pile cap of l_d when the footing/cap connection is not a plastic hinge and $1.25l_d$ when the connection is a plastic hinge zone.

Only a few states have requirements for fixed connections. Florida has the longest requirement (4 feet). Wisconsin and Illinois DOT both require 2-foot embedment for fixed connections. New Hampshire has the shortest required connection (1 foot for piles into piers or other footings) for transferring moment, shear, and axial loads. Colorado and Oregon use a variable embedment length calculated using Equation 2.3.

$$L = \sqrt{\frac{4M_{up}}{\phi f'_c b_f}}$$

Equation 2.4

where:

L = Required pile embedment into cap (in)

 ϕ = Strength reduction factor for concrete bearing

 f'_c = 28-day compressive strength of concrete (ksi)

 M_{up} = Plastic moment capacity of pile about strong axis (kip-in)

 b_f = Pile flange width (in)

2.5 **RESISTING MECHANISMS**

2.5.1 Strand Development for Fixed Connections

The available development length for the prestressing strand in the pile can affect the ability of the pile to develop its full moment capacity at the interface with the footing or cap. The available development length is the distance from the end of the strands in the embedded pile to the point when the pile exits the footing or cap, as shown in Figure 2.9 (a).



Figure 2.9: Strand development in embedded prestressed concrete pile: (a) Available development length and plane where full moment capacity is desired; (b) shrinkage of the footing or cap will actively confine the embedded pile, and (c) bending of the pile will place compressive stresses on portions of the pile bearing against footing or cap.

In fixed connection, the strand must be fully developed for full moment capacity. The strand must be able to develop its full stress at ultimate (f_{ps}) if the connection will allow the pile to develop its full moment capacity. The specified development length (l_d) for bonded strands in AASHTO LRFD is shown in Equation 2.4. A version of this equation was first presented by Zia and Mostafa [39].

$$l_{d} \ge \kappa \left(f_{ps} - \frac{2}{3} f_{pe} \right) d_{b}$$
Equation 2.5

AASHTO LRFD

(5.9.4.3.2-1)

where:

- d_b = nominal strand diameter
- f_{ps} = average stress in prestressing steel at the time for which the nominal resistance of the member is required (ksi)
- f_{pe} = effective stress in the prestressing steel after losses (ksi)
- $\kappa = 1.0$ for piling (and other members) with a depth less than or equal to 24"
- $\kappa = 1.6$ for pretensioned members with depth greater than 24"

For typical stresses, the required development length is greater than 68 inches for 0.5-inch diameter strands and 80 inches for 0.6-inch diameter strands. As shown in Table 2.1, many researchers have found that the full moment capacity of the pile can be developed with much shorter embedment lengths than would be required by AASHTO LRFD to fully develop the strands. This is because the actual required strand development length for the pile embedded in a footing or cap can be shorter than the development length calculated using AASHTO LRFD. There are two primary reasons for this, as illustrated in Figure 2.9 (b) and (c):

- 1. Shrinkage of the cast-in-place (CIP) footing or cap create a clamping force around the embedded pile, which will decrease the required development length. [4], [14], [20], [40], [41].
- 2. Compressive stresses develop as a moment is applied on the pile and cause bearing stresses between the pile and footing or cap, which provide active confinement on the strands further decreasing the required development length. [40]

Several researchers [4], [14], [20], [40], [41] have measured the strains from shrinkage and observed the decreased required development length caused by these effects.

The shrinkage differential will only occur for CIP pile caps. The shrinkage in the CIP pile cap creates the clamping force around the precast pile, which already experienced creep and shrinkage effects. Clamping forces from shrinkage would not be expected for precast pile caps, where most shrinkage would occur prior to the cap being connected with the precast piles in the field. This behavioral difference would suggest that findings from this research project would not be applicable to precast pile caps.

Strand development failures would be expected in connections with embedment shallower than required development length for strands where slip does not occur between pile and cap.

2.5.2 Shear Friction Capacity of Interface

The shear friction capacity at the interface between the precast pile and cast-in-place footing or cap is another mechanism that can control the capacity of the connection. There are two scenarios in which the shear friction capacity controls the behavior. The first is by the moment that would result from the friction force components, as shown in Figure 2.6 (a). The second would be the friction between the pile and footing, or cap required to resist tension that may occur in the connection, as shown in Figure 2.10. Three of the four pile caps tested by Rollins and Stenlund [1] failed due to a pullout failure of the back pile, Figure 2.6 (b). Two of these had a reinforcement cage between the pile and pile cap with embedment lengths of 0.5 and 1.0 times the diameter of the steel pipe pile. The other was connected with pile embedment equal to 2 times the diameter of the steel pipe pile and no reinforcement cage between pile and pile cap. The pullout failure of the back pile between pile and pile cap. The pullout failure of the steel pipe pile and no reinforcement cage between pile and pile cap. The pullout failure of the steel pipe pile and no reinforcement cage between pile and pile cap. The pullout failure of the steel pipe pile and no reinforcement cage between pile and pile cap. The pullout failure of the steel pipe pile and no reinforcement cage between pile and pile cap. The pullout failure of the steel pipe pile and no reinforcement cage between pile and pile cap. The pullout failure of the steel pipe pile and no reinforcement cage between pile and pile cap. The pullout failure of the loading setup, as shown in Figure 2.10.



Figure 2.10: Test setup for pile-to-cap connection testing conducted by Rollins and Stenlund [1]

Castilla et al. [19] investigated three different coefficients of friction between the cap and exterior surfaces of the pile in a parametric analysis: 0.4, 0.7, and 1.4. They found that increasing the coefficient of friction did not have a significant impact on the shape of the displacement curve but did decrease the maximum displacement and maximum rotation of the pile.

This type of failure would be expected in connections with shallower embedment lengths with a smooth interface surface between pile and cap.

2.5.3 Bearing Capacity of Interface

A moment placed on the pile will also be resisted by the bearing forces between the pile and footing or cap, illustrated in Figure 2.11. Two proposed methods were developed to account for the bearing strength of the cap concrete at the interface between pile and cap: Mattock and Gaafar [42] and Marcakis and Mitchell [43]. Both models were developed for steel members embedded into concrete. They consider the capacity of the resultant load (horizontal in this case) acting on the connection to be dependent on the forces caused by bearing between the embedded member and the concrete, as shown in Figure 2.11.



Figure 2.11: Capacity of resultant of horizontal load (V_n) dependent on bearing stress between embedded pile and cap, details for model proposed by (a) Mattock and Gaafar [42]; (b) Marcakis and Mitchell [43]

Mattock and Gaafar [42] assumed a parabolic distribution of bearing stresses for C_b and a uniform stress distribution for C_f of $0.85f'_c$. The bearing stresses are distributed over the width of the

embedded pile, b. The method proposed by Mattock and Gaafar is discussed in detail in Section 4.10.2.2: Punching Shear Failure of Pile Cap Edge

The equations proposed by Marcakis and Mitchell [43] are shown in Equation 2.5 and Equation 2.6.

$$V_n = \frac{0.85f'_c bl_e}{1 + 3.6 e'/l_e}$$
Equation 2.6
$$M_{max} = V_n a + \frac{V_n^2}{1.7f'_c b}$$
Equation 2.7

where:

e = eccentricity of resultant of vertical loads from center of embedment

Marcakis and Mitchell [43] found through their experimental testing that the effective width of the connection (*b* in Equation 2.5 and Equation 2.6) measured to the outside of the reinforcement surrounding the embedded element, limited to 2.5 pile width.

Harries and Petrou [12] recommended that the embedment length in the above equations be modified to account for the possible spalling of the soffit of the pile cap. This modification results in Equation 2.7 and Equation 2.8.

$$V_{n} = 54\sqrt{f'_{c}} \left(\frac{b'}{b}\right)^{0.66} \beta_{1} b l_{e} \left(\frac{0.58 - 0.22\beta_{1}}{0.88 + a'/(l_{e} - c)}\right)$$
Equation 2.8
$$V_{n} = \frac{0.85f'_{c} b (l_{e} - c)}{1 + 3.6 e'/(l_{e} - c)}$$
Equation 2.9
(modified Equation 2.5)

where:

c = depth of concrete cover in pile cap face toward embedded pile

Both estimation procedures [42], [43] have been found to conservatively estimate the required plain embedment length of prestressed concrete piles into caps [12].

This type of failure would be expected in connections with larger embedment lengths where the concrete in the cap is weaker than the concrete in the prestressed pile.

2.6 TESTING DETAILS FROM PREVIOUS RESEARCH

2.6.1 Experimental Variables

There are several different variables that researchers have previously studied. Some of these important variables that have been previously investigated are:

- Embedment length,
- Use of interface reinforcement and type,
- Pile shape and size,
- Dimensions of pile cap, and

• Reinforcement in pile cap.

There do not appear to be any researchers that have systematically investigated the effect of pile and pile cap concrete strength on the performance of the connection, though there have been different concrete strengths tested due to the variability of concrete.

2.6.1.1 Embedment Length and Interface Reinforcement

Embedment length has been one of the primary variables that has been previously investigated. The embedment length dictates the available development length for the prestressing strands and the available interface area for bearing and shear friction interactions between the pile and the cap. Previous research efforts that have investigated multiple embedment lengths are summarized in Table 2.3.

The embedment details done by these researchers are shown in Figure 2.12 (a) and (b). The reinforcement extending from the pile into the cap consisted of either prestressing strands or reinforcement continuing out of the pile into the cap or dowel bars being grouted into the top of the pile and extended into the cap. This reinforcement was either extended straight into the cap or hooked to shorten the required length.

Harries and Petrou [12] studied two simple embedded connections of 18-inch prestressed concrete square piles without interface reinforcement under a constant axial load equal to approximately $0.1f'_{c}A_{g}$. The two lengths they selected were based on the previous embedment length recommended by the South Carolina Department of Transportation (24 inches) and the calculated embedment length required to develop the capacity of the pile (18 inches). They found that the pile with 24-inch embedment was able to develop a moment of 3,636 kip-in, while the 18-inch embedment developed 3,144 kip-in. The estimated capacity of the pile using RESPONSE2000 was 3,420 kip-in. Based on these test results, they proposed a minimum embedment length equal to the width of the pile but not less than 12 inches with no special interface reinforcement required.

Researcher	Pile Size	Embedment Lengths	Embedment lengths
ElBatanouny et al. [14]	18" square, prestressed concrete	18 in, 22 in, 26 in.	$1d_p, 1.22d_p, 1.44d_p$
Harries and Petrou [12]	18" square, prestressed concrete	18 in, 24 in.	$1d_{p}, 1.33d_{p}$
Joen and Park [17]	15.7" octagonal reinf. concrete	2 in*, 31.5 in.	$0.127d_p^*, 2d_p$
Larosche et al. [18]	18" square, prestressed concrete	2 in*, 22 in, 24 in, 26 in.	$\begin{array}{ccc} 0.11d_p^*, & 1.22d_p, \\ 1.33d_p, 1.44d_p \end{array}$

Table 2.3: Previous experimental research investigating multiple embedment lengths.

Researcher	Pile Size	Embedment Lengths	Embedment lengths
Rollins and Stenlund [1]	12" steel pipe pile	6 in*, 12 in*, 12 in, 24 in.	$0.5d_p, 1d_p^*, 1d_p, 2d_p$
Shahawy and Issa [20]	14" square, prestressed concrete	32 in, 42 in, 48 in, 60 in	$\begin{array}{cccc} 2.28d_p, & 3d_p, & 3.43d_p, \\ 4.28d_p \end{array}$
Shama et al. [44]	9" circular timber pile	9 in, 14 in.	$1d_p, 1.56d_p$

Table 2.3: Previous experimental research investigating multiple embedment lengths -Continued

*Interface reinforcement was provided between pile and cap



Figure 2.12: Types of connections: (a) plain embedment of the pile into the cap; (b) embedment with interface steel extending from the pile into the pile cap.

ElBatanouny et al. [14] studied three different embedment lengths (18, 22, and 26 inches) of 18inch square prestressed piles and found that the deeper embedment had higher moment capacities. They also determined the prestressing strand stress at time of failure to see if any slipping of the strands occurred. A summary of their test results is shown in Table 2.4. They did not report the estimated full moment capacity of the piles, only the estimated capacity accounting for insufficient development length of the prestressing strands. The measurement capacities were significantly larger than the estimated capacities including the effect of insufficient development lengths.

Specimen ID	Embedment Length	Moment Capacity	Slipping Stress
BC-18-1	18"	195.8 kip-ft.	185 ksi
BC-18-2	18"	174.2 kip-ft.	160 ksi
BC-22-1	22"	245.8 kip-ft.	270 ksi
BC-26-1	26"	230.8 kip-ft.	270 ksi

Table 2.4: Summary of test results from ElBatanouny et al. [14]

Larosche et al. [18], Rollins and Stenlund [1], and Joen and Park [17] all investigated much smaller embedment lengths (0.111 times the pile width or diameter) with interface reinforcement between the pile and pile cap. The goal was to determine the amount of moment transferred between pile and cap in an assumed pinned connection. These researchers found that it is difficult to create a true pinned connection as the short embedment lengths were still able to develop significant moment transfer (up to 30 percent higher than the estimated pile capacity). Larosche et al. [18] also investigated the behavior of plastic hinges developing adjacent to this connection and concluded that increasing the pile embedment will lead to the improvement of the plastic hinge development and the associated moment capacity.

Shama [44] studied timber piles connected to concrete pile caps. One of the specimens had an embedment length equal to the pile diameter and the other 1.5 times the diameter. Specimens were found to have satisfactory performance when the embedment length equaled the diameter of the pile, although the specimen with the larger embedment length had a higher capacity.

Shahawy and Issa [20] also investigated several different embedment lengths. They tested four different embedment lengths (36, 42, 48, and 60 inches) for 14-inch prestressed concrete square piles. They did not embed these piles into actual pile caps but used a reaction frame to imitate the clamping force provided by the pile cap, as shown in Figure 2.13. They were attempting to isolate the relationship between the embedment length and the development of the prestressing strands.



Figure 2.13: Test setup used by Shahawy and Issa [20]

Results from Shahawy and Issa [20] are summarized in Table 2.5 as the average measured and theoretical ultimate moments for all specimens with similar embedment lengths. There was no apparent strength gain as the embedment increased from 36 inches to 60 inches, although slip of prestressing strands was reported for more specimens with shorter embedment lengths. Although

Shahawy and Issa [20] had the most systematic and complete evaluation of embedment length, the range of embedment lengths investigated was above the range of interest for 14-inch prestressed concrete square piles and there are questions as to whether the clamping provided by the reaction frame accurately represents the conditions of an actual pile-to-pile cap connection.

Embedment Length (in)	# of specimens	Avg. Measured ultimate moment (kip-ft)	Avg. Theoretical ultimate moment (kip-ft)	Avg. Measured/ Theoretical	# specimens where slip was reported
36	4	140.3	124.9	1.13	2
42	6	142.3	127.3	1.12	4
48	6	139.1	128.2	1.09	1
60	3	141.0	127.9	1.10	0

Table 2.5: Summary of test results from Shahawy and Issa [20]

Embedment length for plain embedment details will be the primary variable of interest for the future experimental testing of this project.

2.6.1.2 Pile Details

No single researcher has previously isolated the effect of pile shape on the connection behavior. The pile sections that have been investigated by previous researchers are summarized in Table 2.6 and shown in Figure 2.14.

Pile Type	Dimensions	Researcher
Square prestressed concrete with internal pipe void	30"	Issa [2]
	14"	Xiao [45], Shahawy and Issa [20]
Square prestressed concrete	18"	ElBatanouny et al. [14], Harries and Petrou [12], Larosche et al. [18]
Octagonal prestressed concrete	15.7"	Joen and Park [17]
Steel HP	HP10x42	Shama et al. [13]
Steel HP	HP14x89	Xiao et al. [16]
Staal ning	8"	Stephens and McKittrick [46], Kappes et al. [47]
Sieer pipe	12"	Rollins and Stenlund [1]
Circular timber	9"	Shama and Mander [44]

Square, prestressed concrete piles have been the most tested pile type with 18-inch being the most tested size. Most of the prestressed pile tests have investigated the embedment length required to develop the full capacity of prestressing strands and thus the full capacity of the pile. Most of tests

using the steel pile types have investigated pile cap details by forcing failure of the specimens into the pile cap.



Figure 2.14: Previously investigated pile cross sections: (a) square prestressed concrete pipe pile; (b) square prestressed concrete pile; (c) octagonal prestressed concrete pile; (d) steel HP piles; (e) steel pipe pile; (f) circular timber pile.

The shape and type of pile will affect how the pile and pile cap interact. Unlike square piles, round or octagonal piles will develop bearing forces directed radially from the embedment which may result in greater deterioration of the pile cap and embedment region [12], as shown in Figure 2.15. These radially directed bearing stresses may result in tension developing in the pile cap and may result in failure in the pile cap rather than the pile.



Figure 2.15: Direction of bearing stresses in (a) square; (b) octagonal piles.

Pile shape was not a primary variable investigated experimentally in this project. Several different sizes for square prestressed concrete piles were investigated experimentally. Pile shape was investigated through numerical modeling efforts.

The surface of the embedded piles was intentionally roughened for two pile specimens in Joen and Park [17]. The surface of these two piles was roughened to a magnitude of 0.12 inches using a pneumatic hammer before the pile caps were cast. This is the surface roughness required for a Type B construction joint by the New Zealand Standard Specification for Concrete Construction, NZS 3109 [48].

2.6.1.3 Pile Cap Details

There have been several studies that have investigated the impact of pile cap dimensions and reinforcement detail on the pile-to-cap connection performance.

Larosche et al. [18] investigated several different pile cap details with 18-inch square prestressed concrete piles. Their control specimen had an 18-inch embedment (embedment equal to pile size)

and pile cap dimensions and reinforcement detail in line with the practice used at the time in South Carolina, as shown in Figure 2.16.



Figure 2.16: Control pile cap detail for Larosche et al. [18]: (a) Elevation; (b) Section A-A; (c) Section B-B views; (d) picture of reinforcement cage for Specimen EB-18

Two modifications were made by Larosche et al. [18] to the pile cap design to improve the behavior of the connection. Additional reinforcement was provided in the cap of EB-26, shown in Figure 2.17 (a). Additional distance was provided between the edge of the pile and edge of the pile cap for EB-22, shown in Figure 2.17 (b).



Figure 2.17: Modifications to pile cap design for Larosche et al. [18] for: (a) EB-26; (b) EB-22

A summary of some relevant details related to pile cap design and maximum failure moments for the moment connection tests from Larosche et al. [18] is provided in Table 2.7.

Specimen ID	Reinforcement Percent per Cap Volume	Minimum Edge Distance	Maximum Failure Moment
EB-18	1.62%	13"	1,416 kip-in*
EB-26	2.71%	13"	2,744 kip-in
EB-22	1.62%	27"	2,832 kip-in

Table 2.7: Summary of moment capacity for moment connection specimens from Larosche et al. [18]

*failure occurred in pile cap

The two modified pile cap designs moved the failure from the pile cap into the pile. Both increasing the reinforcement ratio in the pile cap and increasing the minimum edge distance in the direction of bending increased the capacity of the pile-to-cap connection enough to move the failure into the pile.

Stephens and McKittrick [46] tested five different pile cap reinforcing schemes for 8" diameter steel pipe piles with a 9-inch embedment length. Cap reinforcement was the primary variable. The control specimen had the recommended reinforcement plan in Montana at the time of testing. The four other details had a thinner pipe wall thickness and up to seven times the amount of reinforcement in the cap, as shown in Table 2.8. They found that increasing the amount of reinforcement in the cap increased the capacity in the connection and eventually caused failure in the steel pipe pile and not in the cap.

Kappes et al. [47] also investigated pile cap reinforcement for connections between 8-inch diameter concrete filled tube (CFT) piles and pile caps. One type of reinforcement that they investigated in more depth was the use of U-bars around the embedded pile, as shown in Figure 2.18.

ID	Pipe wall thickness (in)	Longitudinal steel ratio (%)	Transverse steel ratio (%)	Concrete strength (ksi)	Maximum moment at failure (kip-ft)
PC-1	0.32	0.41	0.09	4.83	82
<i>PC-2</i>	0.25	0.41	0.09	5.33	74
<i>PC-3</i>	0.25	1.09	0.24	3.15	76
РС-За	0.25	2.11	0.65	3.95	102
<i>PC-4</i>	0.25	2.83	0.70	4.68	121 (Only specimen that failed due to plastic hinging in steel pipe pile)

Table 2.8: Summary of test results from Stephens and McKittrick [46]



Figure 2.18: Cap reinforcement details from Kappes et al. [47] with single #7 U-bar in each direction.

A summary of the test results from Kappes et al. [47] is shown in Table 2.9. The pile design for VT1 was made to be consistent with previous testing done by Stephens and McKittrick [46]. The design strength of the pile was increased to exceed the pile cap strength for the remainder of the specimens.

The single #4 and #5 U-bar detail with 11.75-inch embedment, shown in Figure 2.19, was found to perform better than the single #7 U-bar detail. The single #4 and #5 U-bar detail with U-bars located both on the interior and exterior, shown in Figure 2.19 (b), was the best performing detail.

The reinforcement detail in the pile cap is currently not a primary detail for this project. The design of the pile cap will be decided on based on current Florida practice and integrating some of the research discussed in this section as appropriate.

Specimen ID	U-Bar Configuration	U-Bar Location	Pile Embedment Length	Concrete Strength	Failure Mechanism	Maximum Moment at Failure
VT1	Single #7 U-bar in each direction	Exterior only	9.0 in	6.25 ksi	Plastic hinge in steel pipe pile	119.2 kip- ft
VT2	Single #4 and #5 U- bar in each direction	Exterior only	11.75 in	3.8 ksi	Fracture of concrete pile cap	173.8 kip- ft
VT2.5	Single #7 U-bar in each direction	Exterior only	9.0 in	6.25 ksi	Fracture of concrete pile cap	138.5 kip- ft
VT3	Single #7 U-bar in each direction	Exterior only	10.375 in	4.1 ksi	Fracture of concrete pile cap	151.7 kip- ft
CT1	Single #4 and #5 U- bar in each direction	Exterior only	11.75 in	4.2 ksi	Fracture of concrete pile cap	172.4 kip- ft
CT2	Single #4 and #5 U- bar in each direction	Interior and Exterior	11.75 in	4.2 ksi	Fracture of concrete pile cap	181.8 kip- ft

Table 2.9: Summary of test results from Kappes et al. [47]



Figure 2.19: Single #4 and #5 U-bar detail from Kappes et al. [47] for: (a) CT1 exterior only; (b) CT2 exterior and interior

2.6.1.4 Compressive Strength

As previously stated, there has been no previous research systematically investigating the effect of pile and pile cap concrete compressive strengths on the behavior of the connection. The range of compressive strengths that have been achieved in previous research in the pile and pile cap are summarized in Table 2.10.

A higher quality concrete is used for the precast piles than the cast-in-place pile cap, so the strength of the pile concrete has been greater than the pile cap concrete in all previous research.

Researcher	Pile Concrete Strength Range (ksi)	Pile Cap Concrete Strength Range (ksi)	
ElBatanouny et al. [14]	7.3 to 8.3	4.3 to 5.5	
Harries and Petrou [12]	6.7	3.0 to 5.0	
Issa [2]	10.1	9.0	
Joen and Park [17]	6.3 to 7.3	3.6 to 4.8	
Larosche et al. [18]	7.3 to 8.3	5.1 to 6.4	
Shahawy and Issa [20]	5.6 to 7.8	n/a	
Xiao [45]	8.6	5.9	

Table 2.10: Previous experimental research investigating multiple concrete compressive strength.

2.6.2 Test Setups

Several different test setups have been used by past researchers to experimentally evaluate the connection between piles and pile caps, as shown in Figure 2.20. Three of the five test setups required fixture to a strong floor, Figure 2.20 (a) to (c). Two of the test setups are self-equilibrating, Figure 2.20 (d) and (e).

- 1. **Harries and Petrou** [12]: This test setup required load and support frames. The support frame was anchored to the strong floor and the pile cap to prevent displacement and rotation of the pile cap. Two load frames were required: one to apply a constant axial load to the system and one to apply the variable lateral load. Two hydraulic jacks were used at the location of the lateral load, one bearing against the strong floor and one against the load frame, to apply lateral loads in both directions.
- 2. Shahawy and Issa [20]: This test setup relied on a single reaction beam connected to the strong floor with high-strength threaded rods to provide moment restraint for the pile cap. The lateral load was applied through a hydraulic jack bearing against the strong floor. No axial load was applied to the system.
- 3. **Xiao** [45]: This test setup was the only setup with a vertically oriented pile. The pile cap was anchored directly to the strong floor to provide moment restraint. Two load frames with two hydraulic jacks were used to provide a constant axial load and variable lateral load.
- 4. **Issa** [2]: This test setup was self-equilibrating. Two piles were cast into a single pile cap. A hydraulic jack was placed between the two piles and lateral load applied to failure. Both piles were tested at the same time under this setup. No axial load was applied.
- 5. Larosche et al. [18]: This test setup was self-equilibrating. A modified W-shape steel section was chemically anchored to the side of the pile cap. A diagonally oriented hydraulic jack extended between the W-shape connected to the pile cap and a pinned connection device to the end of the pile. Using this setup, a single jack was used to apply axial load, moment, and shear to the connection. A variable compressive and tensile axial load was applied during testing.



Figure 2.20: Test setups from previous research: (a) Harries and Petrou [12] (elevation); (b) Shahawy and Issa [20] (elevation); (c) Xiao [45] (elevation); (d) Issa [2] (plan); (e) Larosche et al. [18] (plan)

Several different types of tests have been previously conducted by researchers, as shown in Table 2.11. Most of previous testing has been conducted using a constant axial load and cyclic lateral load to failure.

Axial Load	Lateral Load	References		
Constant	Cyclic to Failure	Harries and Petrou [12], Xiao [45], ElBatanouny et al. [14], Joen and Park [17]		
None	Monotonic to Failure	Shahawy and Issa [20], Issa [2]		
Cyclic to Failure None		Xiao [45]		
Variable Variable		Larosche et al. [18]		

Table 2.11: Types of tests previously conducted by researchers.

2.6.3 Instrumentation Layouts

Previous researchers have used different types of gauges and instrumentation to measure displacement, curvature, strand slip, and strain in reinforcement, prestressing strands, and concrete. Some relevant details on the types of instrumentation used by these previous researchers are organized by goal of instrumentation in the following sections.

2.6.3.1 Displacement and Load Measurement

Displacement was typically measured at the point where the lateral load was applied typically using either linear or string potentiometers. The displacement measurement point was shifted in some studies due to limited access at the point of load application. Load was typically measured using load cells at the load application points. Load cells or pressure transducers were also used to verify the constant applied axial loads.

2.6.3.2 Curvature in Plastic Hinge Region

ElBatanouny et al. [14] and Larosche et al. [18] both used four linear variable differential transducers (LVDTs) fixed in series to two opposite faces of the pile in the plastic hinge region, as shown in Figure 2.21. These LVDTs are used to measure displacement, which can be then used to determine the strain on opposite faces. Assuming strains are linear across the section, these strains can be used to determine the curvature along the length of the hinge region.



Figure 2.21: Procedure for measuring curvature in hinge region with LVDTs.

Similar instrumentation was also used by Xiao [45] to measure the curvature in the pile near the connection.

2.6.3.3 Confining stresses

ElBatanouny et al. [14] used two vibrating wire strain gauges (VWGs) embedded in the end of one of their pile specimens (BC-22-1) to measure internal concrete strains in two directions perpendicular to the pile, as shown in Figure 2.22 (a). They used these measured strains in the pile to determine the confinement provided in both directions by the bearing stresses between the pile and pile cap.

Shahawy and Issa [20] used VWGs mounted in the pile cap oriented in the x, y, and xy directions, shown in Figure 2.23 (b), at four different heights along the length of the embedment. They used these gauges to measure the shrinkage strain in the pile cap along the length of the embedment. They assumed that this shrinkage strain in the pile cap applied clamping stresses to the embedded pile, which they assumed decreased the development length of the prestressing strands.



Figure 2.22: Location of VWGs at Section A-A for: (a) ElBatanouny et al. [14]; (b) Shahawy and Issa [20]

2.6.3.4 Strand slip

Shahawy and Issa [20] used horizontal LVDTs at the free end of the pile (extending through the pile cap) to measure the slip of the prestressing strands during testing, as shown in Figure 2.23. Measurement of the strand slip using this technique was only possible because the pile extended through the entire pile cap (i.e. the pile embedment length was equal to the pile cap depth).



Figure 2.23: LVDTs used by Shahawy and Issa [20] to measure strand slip (a) elevation; (b) section A-A; (c) Section B-B

ElBatanouny et al. [14] stated that they used two LVDTs mounted on the top and bottom strands of each pile within the bent cap to measure strand slip. The pile embedment does not equal the pile cap depth though, so it is not clear how these gauges were installed.

2.6.3.5 Prestress Losses

Joen and Park [17] used demountable mechanical (Demec) strain gauges on the piles to measure the concrete strains immediately after transfer and periodically up until testing. These strains were used to determine the prestress losses due to creep and shrinkage. Internally mounted, longitudinally oriented VWGs could also be used to monitor prestress losses in the pile up to the time of testing.

2.6.3.6 Engagement of reinforcement

Joen and Park [17] used typical resistance strain gauges on spiral reinforcement in the pile and pile cap and also on some of the longitudinal non-prestressed steel in the piles. Xiao [45] also used resistance strain gauges mounted on some of the reinforcement in the pile cap, although the specific location of the instrumentation was not specified by the author. ElBatanouny et al. [14] used five strain gauges on some of the longitudinal reinforcement within the bent cap, although the specific location of gauges was not specified.

Chapter 3: Sensitivity Structure Analysis

A numerical analysis was performed using a nonlinear finite element analysis software (FEA) MIDAS Civil to determine the impact of pile-to-cap fixity assumptions on the design and behavior of sensitive structures.

The sensitive structures analysis focused on the analysis of the following primary types of structures:

- 1. Simple spans with uneven span lengths with piles embedded in pier cap,
- 2. PT segmental box girder bridge with fixed pier table subjected to lateral load,
- 3. Straddle bent with pile cap subjected to temperature effects,
- 4. PT segmental box girder bridge with fixed pier table and forced displacement at end of span.

3.1 BRIDGE #1: SIMPLE SPANS WITH UNEVEN SPAN LENGTHS

The stability of substructures can be dependent on the degree of pile fixity in the cap. One example of a substructure dependent on the pile fixity is the construction of tall pile bents using relatively small embedment lengths into the bent cap, shown in Figure 3.1 (a). The bearings for down-station and up-station girders are placed on the bent cap offset from the centerline of the pier, as shown in Figure 3.1 (b). A hinge assumption would result in an unstable linkage across the depth of the bent cap. This detail works because of the consideration of some degree of fixity between the pile and pile cap.



Figure 3.1: (a) Construction of a bridge with tall pile bents (courtesy of Corven Engineering); (b) schematic of unstable bent with assumed pinned connection.

The first structure considered was a simple-span bridge with piles directly embedded in the pier cap, similar to that shown in Figure 3.1. The analysis of this structure investigated the moment developed at the pile-to-cap connection at different construction stages. Analyzing at different construction stages allowed for investigating any in-service impact of the pile-to-cap connection fixity. The fixity of the connection was also varied using a rotational spring connection.

3.1.1 Base Structure

The base structure had five girder lines spaced at eight feet on center, as shown in Figure 3.2 and specified in Table 3.1. The number of girders was decided to equal to the number of piles, and

girders were located directly over the piles. The bridge layout was based on sample drawings provided by FDOT, although the properties were not the same as the provided drawings.



Figure 3.2: Section of interior bent for Bridge #1

The base structure was a three-span bridge with simply supported, non-continuous girders in each span. The middle span had a much longer span length than the first and third spans, as shown in Figure 3.3.



Figure 3.3: Elevation of Bridge #1

The values used in the base structure are summarized in Table 3.1. Note that several of the variables are interdependent, e.g., beam spacing, and span length will control the beam cross section design. The parameters selected for this base structure were determined to represent the general behavior of this type of structure.

Variable		Base Case	
Pile spacing	Spile	8'	
Driven pile depth	l_{p1}	40'	
Exposed pile length	<i>l_{p2}</i> 15'		
Pile width	d_{pile}	18"	
Number of piles at each pier	<i>n_{piles}</i>	5	
Number of girders	n girders	5	
Beam spacing	Sbeam	8'	
Bridge width	Wbd	40'	
Overhang length	Loh	4'	
Bridge length	Lbridge	176'	
Shorter span length	L_{s1}, L_{s3}	40'	
Longer span length	L_{s2}	100'	
Beam cross section		FIB 45	
Deck thickness	t_d	8"	

Table 3.1: Variable values for Bridge #1

3.1.2 Concrete Strength Properties

The concrete strength used in each structural element is summarized in Table 3.2.

Component	Concrete Strength	
Deck	Class IV	
Piles	Class V (Special)	
Pile Cap	Class IV	
Girders	Class IV	
Piers	Class IV	

Table 3.2: Concrete strength properties for Bridge#1

3.1.3 Cross-Section Details for Members

3.1.3.1 Prestressed Beam Details

The 45-inch deep Florida I-Beam (FIB-45) was selected as the cross section for this base bridge, as it is the appropriate cross section for the longer 100-foot span length with 8-foot beam spacing, as shown in Figure 3.4. The general cross section geometry and properties for the FIB-45 are shown in Figure 3.5.



Figure 3.4: FDOT design aid for Florida-I beams [49]



Figure 3.5: General properties for FIB-45 [49]

The FDOT design software "Prestressed Beam" [50] was used to design the beams. Strand layouts determined for the longer and shorter span lengths are shown in Figure 3.6. The section properties and strand location and strand properties are all inputs in the software being used for this study.



Figure 3.6: Strand layout for: (a) 100-ft span; (b) 40-ft span.

3.1.3.2 End and Interior Bents

The cross-section dimensions for the end and interior bents were based on the sample drawings provided by FDOT. No reinforcement details are required in the input for the analyses.



Figure 3.7: Typical cross section dimensions for pier caps.

3.1.3.3 Piles

Pile designs were based on FDOT standard plans for prestressed concrete piles [51]. Square prestressed concrete piles with 18-inch width and height were used for Bridge #1; details for 18-inch piles are shown in Figure 3.8. The pile section and concrete properties are provided as inputs in the software used for this study. Details for the prestressing strands are not inputs in the analysis software.



Figure 3.8: Details for 18-inch square prestressed concrete pile used in Bridge #1[51].

3.1.4 Construction Procedure

This bridge was modeled using construction stages to investigate the impact of placement of each girder and the final stage. The construction procedure for girder placement included the stages shown in Figure 3.9. All the girders in a span were placed at the same time for these analyses. Effects of the weight of the deck during construction were analyzed in Construction Stages 4a through 4c. Results are presented for Construction Stages 1, 2, 4a, 4c, and 5 (completed structure).



5. Completed structure under service loading

Figure 3.9: Assumed construction procedure for Bridge #1

The placement of the second span girders (Construction Stage 2) causes the maximum moment on the pile-to-cap connection of the right interior support. This construction procedure (i.e., with the

Span 2 girders placed after the Span 1 girders) was selected as it resulted in the maximum moment in the connection.

The construction stages for Bridge #1 investigated through numerical modeling are shown in Figure 3.10. Construction Stage 3 and 4c were found to not control, so they were not modeled.



Figure 3.10: Sample model for Bridge #1 with construction stages analyzed.

The weight of the deck during construction stage 4 was added using a distributed load with a magnitude of 0.8 kip/ft. This distributed load was determined based on an 8-inch thick deck, 8-foot beam spacing, and normal weight concrete (150 pcf). The distributed load was applied to each girder individually in the model.

3.1.5 Fixed versus Pinned Connection

Several different connections can be assumed between the pile and pile cap, as shown in Figure 3.11. A fixed connection between pile and pile cap, Figure 3.11 (a), assumes full moment transfer between the pile and pile cap with a rotational stiffness equal to that of the pile. A pinned connection, Figure 3.11 (b), results in an unstable system as there is no moment restraint between pile and pile cap to resist the moment caused by the off-center loading from the adjacent span. A rotational spring, Figure 3.11 (c), can also be used at the connection between pile and pile cap to allow for moment transfer between the elements with a smaller rotational stiffness than the fixed connection.



Figure 3.11: Possible assumed connections between pile and pile cap: (a) fixed; (b) pinned; (c) pinned with rotational spring.

The stiffness of the rotational spring was determined from numerical modeling results based on different embedment lengths. The rotational stiffness was determined by plotting the moment versus rotation assuming rigid body kinetic rotation about the connection between pile and pile cap, as shown in Figure 3.12. The rotational stiffness was then found based on the slope of the moment-rotation plot in the linear elastic region. The rotational stiffness was determined from one shallow embedment ($0.25d_{pile}$) and used as the connection input in the Midas model.



Figure 3.12: Stiffness of rotational spring determined from: (a) M- θ ; (b) numerical results assuming kinetic rotation about a hinge at the connection.

The moment versus rotation plot for the 18-inch piles with $0.25d_b$ pile embedment is shown in Figure 3.13. The $0.25d_p$ embedment would not meet current FDOT specifications; it was chosen to simulate a pinned connection. As shown the rotational stiffness was determined based on two points from the elastic response.



Figure 3.13: Moment versus rotation plot for 18-inch pile with $0.25d_b$ pile embedment from numerical analyses.

3.1.6 Boundary Conditions and Modeling Assumptions

The piles, piers, beams, and deck were modeled as general beam elements. The pile caps were modeled as plate elements with a section thickness corresponding to the cap depth. The boundary conditions at the end of the beams were modeled as pinned connections. The piles were modeled assuming a pinned connection at the tip of the pile, Figure 3.14 (a), and point springs along the length of the embedded pile to model the soil-structure interaction, Figure 3.14 (b). FDOT Structure Design Guidelines [5] specifies that the modulus of subgrade reaction should be obtained

from the geotechnical engineer. For purposes of this project, a modulus of subgrade reaction of 0.23 kips/in³ in the K_x and K_y direction was selected, which corresponds to a dense soil [5].



Figure 3.14: Boundary conditions for Bridge #1: (a) supports; (b) soil-structure interaction.

The beam element for the pile comes into a shared node with the pile cap. This creates a fixed connection unless a beam end release is applied to the node, in which case a pinned connection is realized. A beam end release with the corresponding rotational stiffness was used to simulate the pinned connection. Elastic links (simulating bearing pads) were used to connect the beam elements for beams to the pile caps at one point at the ends of the beams. The stiffness of bearing pads is manufacturer. The elastic links in this model were specified to have a horizontal stiffness of 8.3 kips/inch and vertical stiffness of 7,686 kips/inch, common values for bearing pads with 7-inch thickness. In the last construction stage, the beams were modeled as composite sections with the deck. The full bridge (Construction Stage 5) was modeled in two different ways: one with a continuous deck (SDCL) and one with a joint over the supports.



Figure 3.15: Bridge #1 modeling assumptions: (a) elements intersecting between spans at pile caps; (b) representation of elements and links between elements at this location.

3.1.7 Summary of Results

A summary of all results from these analyses on Bridge #1 is presented in Section 7. A summary of some of the major findings is presented below.

The moment responses for the piles in Bridge #1 at Construction Stages 1 and 2 are shown in Figure 3.16 (a) and (b), respectively. The moment at the pile-to-cap interface was not influenced

by the type of connection, as this moment is dictated by the eccentricity and magnitude of the loads provided from the two spans. The moment magnitude at the soil level was not influenced by the type of connection. All moments were minor in comparison to the pile and pile-to-cap connection capacities (about 10 percent of the full moment capacity of the 18-inch piles).



Figure 3.16: Moment response for select piles in Bridge #1 at: (a) Construction Stage 1; (b) Construction Stage 2

The moments in the beams for Construction Stage 1 and 2 were unaffected by the type of connection between the pile and cap, as shown in Figure 3.17.



Figure 3.17: Moment response for beams in Bridge #1 at Construction Stage #2

The moment responses for the piles in Bridge #1 at Construction Stages 4a and 4b are shown in Figure 3.18, respectively.



Figure 3.18: Moment response for select piles in Bridge #1 at: (a) CS4a; (b) CS4b.

The moments in the beams for Construction Stage 4a and 4b were unaffected by the type of connection between the pile and cap, as shown in Figure 3.19.



Figure 3.19: Moment response for beams in Bridge #1 at: (a) CS4a; (b) CS4b.

The moment response in the composite beams with a continuous deck from live load and piles is shown in Figure 3.20 (a) and (b), respectively. There was no observed difference in the moment in the composite beams between the fixed and rotational spring connections, but there was a slight difference in the moments in the piles with the rotational springs resulting in slightly smaller moments at the pile-to-cap connection.



Figure 3.20: Moment response in: (a) composite beam; (b) piles for Bridge #1 with continuous deck in service (Construction Stage 5).

The moment response in the composite beams with a non-continuous deck from live load and piles is shown in Figure 3.21 (a) and (b), respectively. There was again no observed difference in the moment in the composite beams between the fixed and rotational spring connections, but a slight difference in the pile moments. There was a slightly smaller moment at the pile-to-cap connection and a slightly larger moment at the ground level.



Figure 3.21: Moment response in: (a) composite beam; (b) piles for Bridge #1 with non-continuous deck in service (Construction Stage 5).

The type of joint had no impact on the axial load in any of the piles for any of the construction stages.

3.2 BRIDGE #2: PT SEGMENTAL BOX GIRDER WITH FIXED PIER TABLE AND LATERAL LOAD ON SUBSTRUCTURE

Structures that are designed to resist large lateral loads (e.g., ship impact or seismic loads) are sensitive to the assumed fixity between the pile and pile cap or footing. Bridges in Florida that are located over navigable waters must be designed including consideration for possible vessel impact (e.g. from barges or ocean). The second base structure analyzed was a segmental box girder with a fixed pier table with pile cap and pier, similar to the structure shown in Figure 3.22. This structure was used to analyze the effect of pile fixity on the structural response of vessel impacts [5].



Figure 3.22: Wekiva River Bridge: (a) fixed pier table; (b) bridge elevation [52]

3.2.1 Base Structure

The base structure was a one-cell segmental box girder fixed to a pier with a constant depth D, as shown in Figure 3.23, with three spans, as shown in Figure 3.24.



Figure 3.23: Typical section for Bridge #2

The primary variables selected for the analysis are summarized in Table 3.3. The cap width and length were based on the pile size and pile configuration.

Variable		Base Case	
Pile spacing	Spile	$3.0d_p$	
Pile length	l_p	40'/55'	
Pier height	l _{pier}	65'/85'	
Pile width	d_{pile}	24" and 30"	
Pier width	d_{pier}	10'	
Cap depth	d_{cap}	4'	
Number of piles at each pier	n piles	12	
Bridge width	Wbd	35'	
Bridge length	Lbridge	435'	

 Table 3.3: Variable values for Bridge #2

The span length was determined based on whether the structure had three equal spans, Figure 3.24 (a), or was constructed using a balanced cantilever approach, Figure 3.24 (b). The bridge length was kept the same for both cases. For the equal span length configuration, all spans were 145 feet.

The spans for the balanced cantilever were selected such that the outside span lengths were 0.6 times the main span length, giving span lengths of 118, 199, and 118 feet for the three spans.



Figure 3.24: Elevation of Bridge #2 with: (a) equal spans; (b) balanced cantilever configuration.

The pile cap in this type of structure can either be located at the water line, which is most typical, or at the soil level under the water, both shown in Figure 3.25. The location of the lateral load will be at the water level, so it will be applied at mid-height of the pier for the soil-level pile cap and directly to the pile cap when the pile cap is at the water line. When the pile cap is at soil level, the entire pile (40 feet) will have soil-structure interaction and the pier will have a height of 85 feet. When the pile cap is at the water level, 40 feet of the pile is embedded in soil and 15 feet of the pile will not have soil-structure interaction, which is the distance from the bottom of the pile cap to the soil. The piers in this case will extend 65 feet above the water line, which is typical for navigation clearance.



Figure 3.25: Pile cap location for Bridge #2: (a) at water line; (b) at soil level.

3.2.2 Concrete Strength

The concrete strengths used in each structural element are summarized in Table 3.4.

Component	Concrete Strength	
Box girder	Class IV	
Piles	Class V (Special)	
Pile Cap	Class IV	
Piers	Class IV	

Table 3.4: Concrete strength properties for Bridge #2

3.2.3 Cross Section Details for Members

3.2.3.1 Segmental Box Girder

The AASHTO-PCI-ASBI Standard box girder 2100-1 with a deck width of 34.5 feet (10,500 mm) was selected for this bridge. The AASHTO general cross section is shown in Figure 3.26 and properties summarized in Table 3.5.



Figure 3.26: AASHTO-PCI ASBI Standard 2100-1 box beam [53]

Table 3.5: Section properties for AASHTO-PCI ASBE Standard 2100-1 box beam [53]

Deck Width (in)	A (in)	Area (in ²)	Wt. (kip/ft)	I _x (in ⁴)	y _t (in)
414	41.3	8,353	8.86	7.621 x 10 ⁹	29.1

3.2.3.2 Piles

Pile designs were based on FDOT standard plans for prestressed concrete piles [51]. Square prestressed concrete piles with 24-inch width and height were used for the initial pile configuration for Bridge #2; details for 24-inch piles are shown in Figure 3.27 (a). The pile size was later increased to 30-inch piles, Figure 3.27 (b), and pile configuration modified to reduce the demand on individual piles. The pile section and concrete properties are provided as inputs in the software used for this task. Details for the prestressing strands are not inputs in the analysis software.


Figure 3.27: Details for: (a) 24-inch; (b) 30-inch square prestressed concrete piles used in Bridge #2 [51]

3.2.3.3 Pile Cap

Details for the base pile cap configuration are shown in Figure 3.28. The preliminary pile cap investigated had a pile grid of 3 by 4 piles, which was thought to be typical for the bridge configuration and lateral load applied. Additional pile grids were investigated as described below to decrease the demand on individual piles. The spacing of the piles was based on a minimum center-to-center spacing of $3d_b$ [5].



Figure 3.28: Pile cap details: (a) Plan view; (b) Cross-section.

3.2.3.4 Piers

Square concrete columns with 10-ft width and height were used for Bridge #2. The cross section of the pier is shown in Figure 3.29.



Figure 3.29: Pier cross-section.

3.2.4 Loading

FDOT Structures Design Guidelines [5] specifies that the design of all bridges over navigable waters must include consideration of vessel impact. To analyze the bridge response under extreme events, a lateral force representing the vessel collision was applied. A 2,000-kip lateral force was applied to Pier 1 to represent the vessel impact on the bridge. The analysis was performed under the load combination "Extreme Event II" as shown in Equation 3.1.

$$1.00 DC + 0.50LL + 1.00CV$$
 Equation 3.10

3.2.5 Boundary Conditions and Modeling Assumptions

The models for Bridge #2 are shown in Figure 3.30 for all equal spans and the balanced cantilever configuration. The global x-y-z coordinate system is shown; this coordinate system is referenced in many of the results figures to help with orientation.



Figure 3.30: Bridge #2 with: (a) all equal spans; (b) balanced cantilever configuration.

The piles, piers, and box beams were all modeled as general beam elements. The pile caps were modeled as plate elements with a section thickness corresponding to the cap depth. An elastic link was provided between the top of the pier and the box segment on top of the pier, like those described for Bridge #1. The structure was modeled as a three-span continuous structure. Like Bridge #1, the piles were modeled assuming a pinned connection at the bottom tip of the pile and point springs along the length of the embedded pile, simulating soil-structure interaction. A beam end release was defined between the pile and pile cap to simulate a pinned connection; otherwise, the connection behaves as fully fixed. A rotational spring was not used for pinned connections between pile and cap (like in Bridge #1) in these models as all models were stable with fully pinned connections. Modeling these extremes also enveloped all possible results between a pinned and fixed connection.

When the pile cap was located at the water level, the lateral load was applied to the pile cap and soil structure interaction (i.e., point springs) in the pile was initiated at 15 feet below the pile cap, as shown in Figure 3.31 (a). The soil structure interaction was included along the entire length of the pile for the case of the pile cap at soil level, as shown in Figure 3.31 (b).



Figure 3.31: Boundary conditions for half of structure (showing Pier 1) with: (a) pile cap at water level; (b) pile cap at soil level.

3.2.6 Summary of Results

A summary of some of the major findings is presented below. Note that similar results were observed for equal span length and balanced cantilever analyses.

The axial load in the piles of the pier with the lateral load are shown in Figure 3.32. In the waterline pile cap, an axial tension force (maximum of 285 kips tension) was observed for some of the piles with pinned pile-to-cap connections while almost no axial tension (maximum of 40 kips tension) was observed in the piles with fixed pile-to-cap connections. Larger axial compression was also observed in the piles with pinned pile-to-cap connections (maximum of 574 kips compression compared to a maximum of 285 kips for piles with fixed pile-to-cap connections).

In the soil-level pile cap, axial tension was present in some piles with pinned (maximum of 325 kips tension) and fixed (maximum of 388 kips tension) pile-to-cap connections, a difference of about 16%. There was also a smaller difference between the maximum axial compression in piles with pinned (600 kips compression) and fixed (664 kips compression) pile-to-cap connections, a difference of about 10%.



Figure 3.32: Axial load response for Bridge #2 with all equal spans for select piles supporting the loaded pier for: (a) pile cap at water level; (b) pile cap at soil level.

The moment demand in the piles of the pier with the lateral load (caused by the lateral load) is shown in Figure 3.33. A pinned connection resulted in a slightly higher maximum moment (1,774 kip-ft) in the pile compared to the fixed connection (1,713 kip-ft) for water-level pile cap location (3% increase). For soil-level pile cap, a fixed connection resulted in a higher maximum moment (420 kip-ft) compared to a pinned connection (251 kip-ft) which corresponds to a 40% difference. The location of the maximum moment also changes based on connection fixity, between the embedded portion of the pile for pinned connection to the connection between pile and cap for the fixed connection.

The pinned connection produced the maximum axial tension and compression forces in the piles for the water-level pile cap, while the fixed connection had larger axial tension and compression forces in the piles for the soil-line pile cap. The lateral force produced much higher moments in general for the waterline pile caps compared to the soil-level pile caps; an 85% increase for pinned connections and 75% increase for fixed connections.

The analysis results showed that the ultimate capacity of the 24-inch piles (681 kip-ft) was not sufficient for the water-level pile cap. Several other pile grids were investigated to decrease the demand on the piles.



Figure 3.33: Moment (z direction) response for Bridge #2 with all equal spans for select piles supporting the loaded pier for: (a) pile cap at water level; (b) pile cap at soil level.

The next pile grid and pile size that was investigated was a 4 by 5 pile grid of 30-inch piles, as shown in Figure 3.34. The pile spacing was still $3d_{pile}$ and pile cap geometry was $11d_{pile}$ by $14d_{pile}$.



Figure 3.34: Pile cap details for 4x5 grid of 30-inch piles: (a) plan view; (b) cross-section.

The axial load in the piles of the pier with the lateral load is shown in Figure 3.35. Increasing the number of piles and pile size significantly decreased the overall demand on the individual piles and changed the way pile-to-cap fixity affected the pile response, compared to the 4 by 3 grid of 24-inch piles. For the water-level pile cap, the maximum tension was observed in the piles with

fixed pile-to-cap connections (maximum of 137 kips tension compared to a maximum of 19 kips tension for pinned pile-to-cap connections). The maximum compression was still in the piles with pinned pile-to-cap connections (329 kips compression compared to 261 kips for fixed pile-to-cap connections).

For the soil-level pile cap, there was a smaller difference in the maximum axial tension between pile-to-cap fixities (142 kips tension for fixed and 104 kips tension for pinned) and no difference in the maximum axial compression (507 kips compression for pinned and 507 kips compression for fixed).



Figure 3.35: Axial load response for Bridge #2 4x5 grid with all equal spans for select piles supporting the loaded pier for: (a) pile cap at water level; (b) pile cap at soil level.

The moment caused by the lateral load in the piles of the pier with lateral load is shown in Figure 3.36. In the water-level pile cap, there was little difference in the maximum moment for fixed and pinned connection (1,466 kip-ft for fixed compared to 1,403 kip-ft for pinned). For soil-level pile cap, a fixed connection resulted in a higher maximum moment (392 kip-ft) compared to a pinned connection (187 kip-ft) which corresponds to a 52% increase.

The moment demand was less for the soil-level pile cap than the water-level pile cap for both pinned and fixed pile-to-cap connections.

The moments obtained for the new pile cap configuration with 30-inch piles are smaller compared to the moments with twelve 24-inch piles, but still greater than the ultimate capacity of the 30-inch piles (1,098 kip-ft).



Figure 3.36: Moment (y direction) response for Bridge #2 4x5 grid with all equal spans for select piles supporting the loaded pier for: (a) pile cap at water level; (b) pile cap at soil level.

The next pile grid and pile size that was investigated was a 5 by 5 pile grid of 30-inch piles, as shown in Figure 3.37. The pile spacing was still $3d_{pile}$ and pile cap geometry was $14d_{pile}$ by $14d_{pile}$.



Figure 3.37: Pile cap details for 5x5 grid (a) plan view (b) cross-section.

The axial load and moment in the piles of the pier with lateral load are shown in Figure 3.38 and Figure 3.39, respectively. The maximum axial compression, axial tension, and maximum moment

(absolute value) are summarized in Table 3.6. Adding the five additional piles to the pile configuration further decreased the demand on the individual piles. Also, in general, there was less of a difference in the pile behavior between pinned and fixed pile-to-cap connections (similar maximum axial compression for both, axial tension for soil level, and maximum moment for water-level pile caps). Fixed pile-to-cap connections resulted in higher axial tension with water-level pile caps (64% increase) and higher maximum moment with soil-level pile caps (71% increase).

Table 3.6: Summary axial load and moment	(z direction) f	for pile cap	at water	level and	l pile cap	at soil
	level					



Figure 3.38: Axial load response for Bridge #2 5x5 grid with all equal spans for select piles supporting the loaded pier for: (a) pile cap at water level; (b) pile cap at soil level.



Figure 3.39: Moment (z direction) response for Bridge #2 5x5 grid with all equal spans for select piles supporting the loaded pier for: (a) pile cap at water level; (b) pile cap at soil level.

The moments obtained for the grid with twenty-five, 30-inch piles are smaller compared to the moments with twenty 30-inch piles. As previously mentioned, the ultimate capacity of the 30-inch pile is 1,098 kip-ft, which satisfies the demand for all the piles in the soil-level and water-level pile cap, as shown in Figure 3.40.



Figure 3.40: Maximum moment for piles supporting the loaded pier for pile cap at water and soil level.

After different iterations, the final geometry of the segmental box girder bridge that satisfies the moment demands, consists of twenty-five 30-inch piles in each pile cap, as shown in Figure 3.41.

The results obtained showed that higher moments were obtained with the water-level pile cap, but the structure was more sensitive to the connection (pinned or fixed) for the soil-level pile cap.



Figure 3.41: Final geometry for Bridge#2: (a) water-level pile cap; (b) soil-level pile cap.

The axial load in the piers was unaffected by the type of connection between pile cap and the location of pile cap and applied lateral load.

The moment in the piers was unaffected by the pile-to-cap connection for the soil-level pile cap as shown in Figure 3.42. On the contrary, the pier where the lateral load is applied, is highly affected by the type of connection in the water-level pile cap.



Figure 3.42: Moment (z direction) response for Bridge #2 with all equal spans for laterally loaded piers for: (a) pile cap at water level; (b) pile cap at soil level.

The response of the box beam was unaffected by whether a fixed or pinned connection in the soillevel pile cap. On the water-level pile cap case a higher shear response and moment in the z direction was obtained for the pinned connection, as shown in Figure 3.43.



Figure 3.43: (a) Shear (y direction); (b) moment response for Bridge #2 with all equal spans and water-level pile caps along length of beam.

3.3 BRIDGE #3: STRADDLE BENT

The assumed fixity between pile and cap can also impact the design of bridges where the stiffness of the substructure can impact the behavior of the superstructure. These bridges include segmental box girder bridges with fixed pier tables, and straddle bents, although it is not necessarily a feature of structures with integral superstructures. Foundation stiffness for short piers was closely considered to capture the change in forces for time-dependent creep and shrinkage, support settlement, transit breaking loads, etc.

The third base structure to be evaluated was a straddle bent, similar to the one shown in Figure 3.44, considering temperature effects and approximate loading from the superstructure.



Figure 3.44: Straddle bent (courtesy of Corven Engineering).

3.3.1 Base Structure

The details for the straddle bent are shown in Figure 3.45 and Table 3.7.



Figure 3.45: Details for Bridge #3.

Variable		Base Case
Pile spacing	Spile	5'
Driven pile depth	l_{p1}	40'
Pier height	l_{p2}	20'
Pile width	d_{pile}	18"
Pier width	d_{pier}	5'
Number of piles at each pile cap	<i>n</i> _{piles}	4
Beam length	lbeam	40'
Beam depth	d_{beam}	6'
Beam width	Wbeam	5'
Cap depth	d_{cap}	5'

Table 3.7: Variable values for Bridge #3

3.3.2 Cross-Section Details for Members

3.3.2.1 Pile Cap

Details for the pile cap are shown in Figure 3.46. The preliminary pile cap investigated has a pile grid of 2 by 2 piles, which is typical for this bridge configuration. The spacing of the piles is based on a minimum center-to-center spacing of $3d_b$ [5].



Figure 3.46: Pile cap details: (a) plan view; (b) cross-section.

3.3.2.2 Pile

Pile designs were based on FDOT standard plans for prestressed concrete piles [51]. Square prestressed concrete piles with 18-inch width and height were used for Bridge #3; details for 18-inch piles are shown in Figure 3.47. The pile section and concrete properties are provided as inputs in the software used for this task. Details for the prestressing strands are not inputs in the analysis software.



Figure 3.47: Details for 18-inch square prestressed concrete pile used in Bridge #3 [51].

3.3.2.3 Straddle Bent

Details for the straddle beam are shown in Figure 3.48. The section investigated consists of six 6inch ducts with twelve 0.6-inch strands in each duct. The strand pattern was based on a Midas tutorial: Straddle Beam Design using Midas Civil [54].



Figure 3.48: Straddle beam cross-section.

3.3.3 Loading

Two loading-related variables were investigated for Bridge #3: temperature effects and superstructure loading. A uniform temperature profile and temperature gradient were both investigated on Bridge #3. Temperature effects are considered a force effect due to superimposed deformation [5]. The temperature range selected for the uniform temperature range was based on Table 2.7.1-1 in the FDOT Structures Design Guidelines [5]; for concrete-only structures, temperature varies from 35°F to 105°F.

The temperature gradient for concrete superstructures was determined based on AASHTO LRFD [3]. Florida is in Solar Radiation Zone 3, which has a $T_1 = 41^{\circ}$ F and $T_2 = 11^{\circ}$ F. These values were used as input in the computer software. SDG [5] specifies that the effects of temperature gradient need only be taken into account for continuous concrete superstructures. A temperature gradient was investigated for this substructure element to mimic the influence of post-tensioning that is common in these bent caps.

The effect of applying a vertical load from the superstructure was also investigated. The maximum vertical load applied from the superstructure was determined from the axial load in the piers from the Bridge #2 model (considering only dead and live loads); this force was found to be 1,200 kips (factored). A point load was applied at midspan of the bent cap for some of the load cases to see the effect of the vertical load with uniform temperature and temperature gradient effects.

The post-tensioning described above was applied to all the different load cases. Long-term effects were included in the analysis by considering long-term material properties for creep and shrinkage and concrete compressive strength.

The creep coefficient and shrinkage strain were automatically calculated by Midas using the AASHTO LRFD Bridge Design Specification [3], considering the volume-to-surface ratio and the compressive strength of concrete at age of 28 days. Two long-term properties were created: one for the concrete strength of 5.5 ksi and for 6.0 ksi. Results for the creep coefficient and shrinkage strain for 5.5 ksi are shown in Figure 3.49.



Figure 3.49: Long-term properties: (a) creep coefficient for 5.5 ksi; (b) shrinkage strain for 5.5 ksi.

A time-dependent material property was defined for the compressive strength of the concrete to reflect the variation of the modulus of elasticity with time. Midas calculates the development of concrete compressive strength and stiffness using equations found ACI 209R-08 [55] considering the concrete strength at 28 days and the concrete strength factors (A and B). Typical values for the concrete strength factors were used (A = 4 and B = 0.85).

Four different load cases were applied to Bridge #3:

- 1. Uniform temperature, no vertical load, PT
- 2. Uniform temperature, vertical load, PT
- 3. Temperature gradient, no vertical load, PT
- 4. Temperature gradient, vertical load, PT

A schematic of these different load cases is shown in Figure 3.50.



Figure 3.50: Four load cases investigated for Bridge #3: (a) uniform temperature, no vertical load; (b) uniform temperature with vertical load; (c) temperature gradient, no vertical load; and (d) temperature gradient with vertical load.

3.3.4 Boundary Conditions and Modeling Assumptions

The base model for Bridge #3 is shown in Figure 3.51. The piles, columns, and bent cap were all modeled as general beam elements. The pile caps were modeled as plate elements with a section thickness corresponding to the cap depth. An elastic link with infinite stiffness was provided between the columns and bent cap to provide a moment connection between these elements. Like Bridges #1 and #2, the piles were modeled assuming a pinned connection at the tip of the pile and point springs along the length of the embedded pile, simulating soil-structure interaction. Like

Bridge #2, a beam release was defined between pile and pile cap to simulate a pinned connection; otherwise, the connection behaves as fully fixed.



Figure 3.51: Boundary conditions for Bridge #3: (a) supports; (b) soil-structure interaction.

Element temperature was modeled in MIDAS by defining the initial and final temperature of the element. The two models analyzed with uniform temperature changes are shown in Figure 3.52 (a) without vertical load and (b) with vertical load.



Figure 3.52. Bridge #3 model with uniform element temperature: (a) without vertical load; (b) with vertical load.

As mentioned, a temperature gradient of $T_1 - T_2 = -30^{\circ}$ F was also applied to the structure. The two models with gradient are shown in Figure 3.53.



Figure 3.53: Bridge #3 with temperature gradient: (a) without vertical load; (b) with vertical load.

Post-tensioning was included in the straddle bent, as shown in Figure 3.54. All strands were stressed to 202 ksi. The effects of the post-tensioning were included in all analyses.



Figure 3.54: Post-tensioned loading for Bridge#3.

3.3.5 Summary of Results

The axial load in the piles remained in compression in all four load cases for pinned and fixed connections between pile and pile cap. The axial load was not significantly affected for the cases without vertical applied load as shown in Figure 3.55 (a). The most significant difference was seen for the load cases with vertical applied load shown in Figure 3.55 (b), where the fixed connection resulted in an increased axial compression of about 10%.



Figure 3.55: Axial load response for Bridge #3 piles with: (a) uniform temperature only; (b) uniform temperature with vertical applied load.

The maximum moment in the piles was found to be larger for bridges with a fixed pile-to-cap connection in all load cases. The maximum moment was between 35% and 60% larger with a fixed pile-to-cap connection compared to a pinned connection. An example of the difference between fixed and pinned connection is shown in Figure 3.56.



Figure 3.56: Moment response for Bridge #3 piles with: (a) uniform temperature only; (b) uniform temperature with vertical applied load.

Little to no difference in column or bent cap behavior was observed between bridges with fixed and pinned pile-to-cap connections for all four load cases. A sample response for the axial load and moment response in the piers is shown in Figure 3.57.



Figure 3.57: (a) Axial load; (b) moment response for Bridge #3 columns with uniform temperature only.

3.4 BRIDGE #4: PT SEGMENTAL BOX GIRDER WITH FIXED PIER TABLE

The last structure that was analyzed was a segmental box girder bridge with fixed pier tables, similar to Bridge #2, except with an applied displacement in the middle of the span to simulate erection tolerances at the closure pour between the cantilevered spans. The difference in elevation at this point is typically taken care of by using steel strong back system with jacks to force the tips of the two cantilevered spans to align. The closure pour is then cast, the continuity tendons stressed along the top and bottom of the section, and then the strong back was released, which locks in the stresses in the structure. These locked-in stresses need to be considered in the superstructure and substructure designs and the assumed fixity of the pile-to-cap connection will affect how these stresses are handled.

3.4.1 Base Structure

The same base structure as Bridge #2 was used with a balanced cantilever configuration and pile caps at soil level, as shown in Figure 3.58. Variables and parameters used in this model are presented in Table 3.3 and previous sections.



Figure 3.58: (a) Typical section for Bridge #4; (b) elevation of balanced cantilever configuration.

3.4.2 Elevation and Detail

FDOT Structures Design Guideline [5] requirements for cantilever bridges with fixed pier tables specify an erection tolerance of L/1000 (where L is the cantilever length from the center of the pier to the cantilever tip), as shown in Figure 3.59. For a main span of 199 feet (corresponding to the main span length of the balanced cantilever configuration), the cantilever length is 99.5 feet, and the corresponding tolerance is 1.19 inches.



Figure 3.59: Post-tensioned segmental box girder bridge with fixed pier table.

Half of the structure will be modeled with this applied displacement of 1.19 inches at the location where the forced displacement would be locked in, as shown in Figure 3.60.



Figure 3.60: Imposed deflection at cut in half-bridge model.

3.4.3 Pile Layout

Three different pile orientations were investigated for Bridge #4:

- 3x4 grid of 18-inch piles
- 2x4 grid of 24-inch piles
- 2x3 grid of 30-inch piles

The investigated pile layouts are also shown in Figure 3.61.



Figure 3.61: Pile layouts used for Bridge #4 with: (a) 3x4 grid of 18-inch piles; (b) 2x4 grid of 24-inch piles; (c) 2x3 grid of 30-inch piles.

3.4.4 Boundary Conditions and Modeling Assumptions

The base model for Bridge #4 with the three different pile layouts is shown in Figure 3.62.



Figure 3.62: Bridge #4 modeling.

The piles, piers, and box beams were all modeled as general beam elements. The pile caps were modeled as plate elements with a section thickness corresponding to the cap depth. An elastic link was provided between the top of the pier and the box segment on top of the pier with infinite stiffness. The structure was modeled such that the beam was continuous over the interior pier. The piles were modeled assuming a pinned connection at the tip of the pile and point springs along the length of the embedded pile, simulating soil-structure interaction. A beam release was defined between pile and pile cap to simulate a pinned connection; otherwise, the connection behaves as fully fixed. The applied soil-structure interaction and applied settlement of 1.19 inches are shown in Figure 3.63.



Figure 3.63: Boundary conditions for Bridge #4.

3.4.5 Summary of Results

A summary of the major findings is presented below.

There was not a significant difference in axial load in the piles between bridges with fixed and pinned pile-to-cap connections, as shown in Figure 3.64.



Figure 3.64: Axial load response for select piles in Bridge #4 with: (a) 3x4 grid of 18-inch piles; (b) 2x3 grid of 30-inch piles.

The observed moment in the piles for the 3x4 and 2x3 pile configurations is shown in Figure 3.65. No moment was experienced in piles for bridges with pinned pile-to-cap connections. Only minor moment was seen in the piles for bridges with fixed pile-to-cap connections. The moment per pile does increase as the number of piles decreases and pile size increases.



Figure 3.65: Moment response for select piles in Bridge #4 with: (a) 3x4 grid of 18-inch piles; (b) 2x3 grid of 30-inch piles.

There was little to no difference in the behavior of the beam or pier based on whether a pinned or fixed pile-to-cap connection was used. An example of the similar behavior is shown in Figure 3.66 for the axial load and moment response of the pier.



Figure 3.66: (a) Axial load; (b) moment response for pier in Bridge #4.

Chapter 4: Preliminary Numerical Study

A preliminary numerical analysis was performed using a nonlinear finite element analysis software ATENA [56] to investigate the variables impacting the behavior of the connection and the required embedment lengths for fixed and pinned connections. Results for this preliminary study helped to determine the primary and secondary variables tested in the experimental program.

4.1 BOUNDARY CONDITIONS AND MODELING ASSUMPTIONS FOR PILE-TO-CAP CONNECTION MODELS

ATENA is a FEA software specifically designed for reinforced concrete structures. It was used to study the failure mechanisms of over 100 different specimens with different connection details. The program has detailed bond-slip models that will be capable of capturing the slip of the prestressing strands, detailed interface material models, detailed concrete material models, and detailed crack patterns.

The prestressed pile and cast-in-place pile cap will be modeled considering its construction sequence. First, the strands in the pile are going to be prestressed to the desired stress and the pile cast; after this, the pile cap will be cast and an axial load will be applied to the pile; finally, a lateral load will be applied to the pile and reactions at this point will be recorded.

ATENA provides the possibility of modeling the construction stages of different structures. Three different intervals, with the steps described above, were created, and analyzed. Details of the analysis are presented in subsequent sections.

4.1.1 Model Geometry

The geometry was first drawn in AutoCAD 3D. Typical models consisted of six 3D volume components (pile cap, pile, and plates) and 1D lines representing the reinforcing steel, see Figure 4.1 (a). After defining the geometry in AutoCAD 3D, each section was imported into ATENA, as shown in Figure 4.1 (b).



Figure 4.1: Example of: (a) AutoCAD model; (b) ATENA model used for pile-to-cap connection models.

Interfaces were defined between volume elements with different material properties that shared common surfaces. As an example, a fixed contact (Master-Slave) connection was defined between the concrete pile and an elastic plate where load was applied and between the pile cap and two elastic plates where boundary conditions were applied, as shown in Figure 4.2.



Figure 4.2: Sample of Master-Slave conditions used at interfaces between volume elements.

The reinforcement scheme used in the typical pile-to-pile cap connection specimens is shown in Figure 4.3. The prestressing strands were either 0.5-inch or 0.6-inch diameter strands. Conventional reinforcement (#5, #6, #9, and W3.4 wire) was used in the piles and pile caps.



Figure 4.3: Reinforcement layout for typical pile-to-pile cap connection specimens.

4.1.2 Material Assumptions

Three different materials were used for the analysis: (1) a solid concrete material for the pile and pile cap, (2) an elastic solid material for the plates, and (3) 1D reinforcement for the reinforcing bars and prestressing strands.

The SOLID Concrete material was used for the pile and pile cap. Concrete models were created for all the investigated concrete strengths, parameters for three example concrete types are shown in Table 4.1. Two of the concrete models shown were used for modeling the pile cap during testing (Concrete6000 and Concrete5500). The third concrete model shown was used to model the pile cap during the prestressing of the pile, so that the pile cap did not restrain the pile during the prestressing process (Concrete Soft).

Material Parameter	Concrete6000	Concrete5500	Concrete Soft
Young's modulus (ksi)	4415.2	4227.2	1.45
Poisson's ratio	0.2	0.2	0.2
Compressive strength (ksi)	-6.0	-5.5	-6.5

 Table 4.1: Sample material parameters of concrete

The material used for the steel plates was generated using the Solid Elastic option with the properties shown in Table 4.2. Similar to the concrete, a soft elastic material with no stiffness was used for the steel plates during the prestressing of the piles.

Material Parameter	Steel Plate	Steel Plate Soft	
Young's modulus (ksi)	29000	1.45	
Poisson's ratio	0.3	0.3	

Table 4.2: Material parameters of steel plates

The reinforcing steel in the pile cap (#5, #6, and #9 bars) and the W3.4 wires confining the strands in the piles were all modeled as 1D reinforcement with a yield strength (f_1) of 60 ksi, yield strain (ε_1) of 0.00207, an ultimate strength (f_2) of 90 ksi and a strain at ultimate strength (ε_2) of 0.025 with a stress-strain relationship similar to that shown in Figure 4.4 (a).



Figure 4.4: Stress-strain curve: (a) Reinforcement; (b) tendons.

The prestressing strands were also created using the 1D reinforcement option, but with a tendon type option. The stress-strain relationship used for the prestressing strands is shown in Figure 4.4 (b). The critical values used for this curve are the following: yield strength (f_1) of 204 ksi, yield strain (ε_1) of 0.007, second critical stress (f_2) of 243 ksi, second critical strain (ε_2) of 0.011, ultimate strength (f_3) of 270 ksi and strain at ultimate strength (ε_3) of 0.043. These values were roughly based on the Ramberg-Osgood stress-strain relationship. A prestrain was applied to the prestressing strands in 10 load steps to model the initial stress in the strands.

4.1.3 Test Setup and Boundary Conditions

The pile-to-pile cap connection was tested as a cantilever beam in the horizontal position fixed to a strong floor, as shown in Figure 4.5 (a). A lateral load was applied and increased until failure occurred in the specimens; the deflection at the location of the lateral load was measured using a point monitor. When axial load was applied, spreader beams at the back of the pile cap were added and a load was applied and kept constant throughout the model, as shown in Figure 4.5 (b).



Figure 4.5: Test configuration used for modeling connection specimens: (a) without axial load application; (b) with axial load application.

Two plates were used to create a fixed condition for the pile cap, as shown in Figure 4.6 (a). A plate with a constraint in the z direction was placed on the back of the pile cap (opposite the pile); a plate with x and y constraints was placed on the bottom of the pile (on a face adjacent to the face with the pile), both shown in Figure 4.6 (b). These boundary conditions created a moment restrain in the pile cap similar to what would be expected in the laboratory, with the bottom of the pile cap resting on the strong floor and the back fixed to a reaction frame like in Figure 4.5.



Figure 4.6: Boundary conditions: (a) plates; (b) restrictions.

4.1.4 Load Protocol

A construction process was required to properly apply the prestressing and axial load in the piles before the lateral load was applied to fail the specimens. Three different loading stages were used, which are similar to how the specimens would be loaded in the laboratory and in the field.

- *Load Stage #1*: prestrain applied to the prestressing strands,
- *Load Stage #2*: axial load applied to the piles,
- *Load Stage #3*: lateral load applied to piles until failure of system.

4.1.4.1 Load Stage #1

The purpose of Load Stage #1 was to prestress the strands in the piles. The pile concrete strength was defined with typical stiffness. The pile cap concrete was specified with a stiffness close to zero, so the pile cap did not restrain the pile during prestressing, as shown in Figure 4.7. The total desired prestrain was applied to the piles in 10 steps.



Figure 4.7: Load Stage #1: (a) defined materials; (b) applied prestrain of -0.007 per step in prestressing strands.

The prestrain was locked in and kept constant at the end of this load stage.

4.1.4.2 Load Stage #2

The purpose of Load Stage #2 was to apply the axial load to the pile in the complete system. The "soft" materials were redefined with the material properties desired for the final test, as shown in Table 4.3.

Old Material	New Material
Concrete5500 (Soft)	Concrete5500
SteelPlate (Soft)	SteelPlate

Table 4.3: New material definitions for Load Stage #2

An axial load was applied to the end of the pile, as shown in Figure 4.8 (a) in 10 separate steps. The axial load was then kept constant on the pile at the end of this load stage.



Figure 4.8: (a) Axial load applied during Load Stage #2; (b) lateral load applied during Load Stage #3. 4.1.4.3 Load Stage #3

The purpose of Load Stage #3 was to determine the moment capacity of the pile-to-cap connection by applying a lateral load until failure of the pile or connection. The prestrain in the pile prestressing strands and axial load in the pile were both kept constant during this load stage. Lateral load was applied, as shown in Figure 4.8 (b), by applying an additional small displacement for 90 steps. The maximum observed load was recorded as the failure load. The load significantly decreased after the failure load in all cases.

4.1.5 Finite Element Mesh

The finite element mesh quality has an important influence on the quality of the analysis results and speed [57], [58]. Meshing was selected such that all volumes would have at least four elements per thickness (e.g., 4.5-inch mesh for 18-inch piles). Linear elements were used for the 1D reinforcement and tetrahedra elements for all 3D volumes, as shown in Figure 4.9. This mesh size was selected to allow for all the desired models to be run in a reasonable time. This mesh was also previously shown to produce reasonable results when compared to previous experimental results.



Figure 4.9: Sample mesh for pile-to-cap connection analyses.

4.2 NUMERICAL RESULTS FOR PILE-TO-CAP CONNECTION MODELS

4.2.1 Pile Capacity

The capacities of the piles with two different strand configurations were determined using a sectional analysis program, RESPONSE 2000. The fundamental assumptions using RESPONSE2000 include: 1) perfect bond between concrete and prestressing strands; 2) concrete spalls in compression and cracks in tension based on its stress-strain behavior. The moment-curvature responses are shown in Figure 4.10 and maximum moment capacities shown in Table 4.4. There is minimal difference in the moment-curvature behavior of piles with different strand patterns.



Figure 4.10: Moment-curvature response for: (a) 18-inch; (b) 24-inch; (c) 30-inch piles (highlighted capacities for piles with 0.5-inch strands).

Pile Size:	18-inch	24-inch	30-inch
M_n (0.5-inch strands):	308.9 kip-ft.	681.4 kip-ft.	1,098 kip-ft.
M_n (0.6-inch strands):	315.7 kip-ft.	653.7 kip-ft.	1,102 kip-ft.

Table 4.4: Maximum moment capacities for piles

The axial load versus moment response for all pile sizes is shown in Figure 4.11.



Figure 4.11: Moment-axial load response for: (a) 18-inch; (b) 24-inch; (c) 30-inch piles.

4.2.2 Effect of Embedment Length

The first primary variable investigated through the pile-to-cap connection modeling was the effect of embedment length. Specimens with six to eight different embedment lengths were investigated for each pile diameter where there was no interface reinforcement between the pile and cap. Five to seven different embedment lengths were investigated for each pile diameter where there was interface reinforcement between the pile and cap. The $1.5d_b$ pile embedment specimens were not modeled with interface reinforcement because there was not sufficient room available in the pile cap for the interface reinforcement. Sample moment versus deflection curves for the 18-inch piles with different embedment lengths are shown in Figure 4.12.



Figure 4.12: Sample moment versus deflection responses for 18-inch piles: (a) without; (b) with interface reinforcement with varying embedment length.

The maximum moment was determined from the moment-deflection plots and plotted versus the embedment length in Figure 4.13. The maximum moment determined from RESPONSE2000 is also shown in this plot.



Figure 4.13: Sample moment versus embedment length responses for 18-inch piles: (a) without; (b) with interface reinforcement.

Cracking patterns were obtained for the models to determine the mode of failure controlling the failure of the specimens. Two of the primary failure mechanisms are shown in Figure 4.14. Shallow pile embedment resulted in failure of the cap, as shown in Figure 4.14 (a). Deeper embedment resulted in failure of the pile, as shown in Figure 4.14 (b).



Figure 4.14: Sample crack patterns for 18-inch piles without interface reinforcement with: (a) $0.25d_b$; (b) 1.5d_b embedment length.

The moment response for the 18-inch, 24-inch and 30-inch piles was normalized based on the estimated pile capacity from the layered-section analysis (RESPONSE 2000) shown in Table 4.4. The normalized moment versus embedment length (normalized by the pile size) is shown in Figure 4.15 for specimens without interface reinforcement, Figure 4.16 for specimens with interface reinforcement.

The embedment length required to reach the capacity of the pile was estimated using layer-section analysis and the embedment length required for transition of failure mechanism from connection to pile are highlighted in Figure 4.15 and Figure 4.16. This transition occurred around 1.25 times the capacity of the pile. The pile-to-cap connection could have developed higher capacity than the pile due to the confining stresses and clamping forces that developed around the embedded pile, which were not considered in the layered-section analysis. The embedment length required to reach the moment capacity of the pile and transition failure from connection into pile are relatively consistent between the different embedment lengths when no interface reinforcement is present.



Figure 4.15: Normalized moment versus embedment length for: (a) 18-inch; (b) 24-inch; (c) 30-inch piles without interface reinforcement. ($P=0, f'_{c, pile}=6 \text{ ksi}, f'_{c cap}=5.5 \text{ ksi}$)

The presence of the interface reinforcement slightly decreases the required embedment to develop the moment capacity of the pile but has minimal effect on the embedment length required to transition failure from the connection to the pile.



Figure 4.16: Normalized moment versus embedment length for: (a) 18-inch; (b) 24-inch; (c) 30-inch piles with interface reinforcement. (P=0, $f'_{c, pile}=6$ ksi, $f'_{c cap}=5.5$ ksi)

The interface reinforcement has more of an effect on the behavior of the 18-inch piles compared to the 24 and 30-inch piles. This is because the location of the interface reinforcement has a larger relative lever arm compared to the location of the prestressing strands, as shown in Figure 4.17.



Figure 4.17: Location of interface steel layout in: (a) 18-inch; (b) 24-inch; (c) 30-inch square prestressed piles.

The response of the system with all three pile sizes with and without interface reinforcement are shown in Figure 4.18. Preliminary numerical results showed a linear relationship between embedment length and connection capacity until the capacity of the pile begins to control. The following two equations can be used to reasonably approximate the relationship between embedment and connection capacity without considering any other variables other than embedment length.

Without interface reinforcement:

$$\binom{M_c}{M_{pile}} = 2.0 \binom{L_e}{d_p} + 0.2 \le 1.0$$
 Equation 4.11

With interface reinforcement:

$$\binom{M_c}{M_{pile}} = 1.8 \binom{L_e}{d_p} + 0.4 \le 1.0$$
 Equation 4.12

Equation 4.1 and Equation 4.2 are included with the normalized moment versus embedment length plots in Figure 4.18. There is reasonable agreement between the numerical results and the estimates from the embedment length equations. Results in this section are based on preliminary numerical results and could be contradictory with experimental test results presented in other sections.



Figure 4.18: Normalized moment versus embedment length for pile-to-cap connections: (a) without; (b) with interface reinforcement.

Embedment length clearly influences the behavior of the connections. Embedment length should be one of the primary variables investigated during the experimental testing program. The numerical results from these preliminary models suggest that even shallow pile embedment transfer moment. Interface steel should be investigated for the shallower pile embedment lengths with an alternate detail to try and develop a pinned response. One idea for a pinned connection is shown in Figure 4.19.


Figure 4.19: Idea for pinned connection between pile and pile cap: (a) cross-section; (b) elevation.

4.2.3 Effect of Axial Load

The next variable investigated was the applied axial load to the pile. The effect of axial load on the behavior of the pile-to-cap connection was investigated for one shallow and one deep embedment, shown in Figure 4.20. This practice was repeated for all the secondary variables to investigate the effect of this variable on the connection capacity when the connection controlled the failure and when the flexural strength of the pile controlled the failure. The axial load generally had two effects on the behavior of the system:

- 1. Axial compression would improve the performance of the connection, as shown in Figure 4.20 (a). The axial load was found to have the largest impact on the 30-inch diameter piles, where going from an axial compression load of $0.1A_gf'_c$ to $0.2A_gf'_c$ increased the capacity of the system by about 33%. The 18-inch and 24-inch pile systems saw a smaller increase in capacity of about 10%.
- 2. Axial compression generally increased the capacity of the pile itself, as shown in Figure 4.20 (b). The 30-inch pile saw an increase in capacity of about 4% when going from an axial compression load of $0.1A_g f'_c$ to $0.2A_g f'_c$.



Figure 4.20: Sample moment versus deflection responses for 30-inch piles with: (a) shallow (0.25d_b); (b) deep (1.5d_b) embedment with varying axial load.(c) normalized moment versus axial load for shallow embedment, and (d) normalized moment versus axial load for deep embedment

An additional series of models were analyzed to evaluate the effect of interface reinforcement on the behavior of the system under various axial loads. The moment-deflection responses for 30-inch piles with and without interface reinforcement subjected to various constant axial loads are shown in Figure 4.21. The presence of interface reinforcement increased the capacity of the connection and decreased the impact of axial load on the behavior of the connection.



Figure 4.21: Sample moment versus deflection responses for 30-inch piles: (a) without; (b) with interface reinforcement with varying axial load.

4.2.4 Effect of Pile Concrete Strength

The moment versus deflection responses for systems with 30-inch piles and different pile concrete strengths are shown in Figure 4.22. The pile concrete strength did not significantly impact the behavior of the system when the failure of the system occurred at the connection, see Figure 4.22 (a). This is due to the failure of the connection occurring due to a failure in the cap. Increasing the strength of concrete in the pile did tend to increase the capacity of systems with larger pile embedment; this is because the strength of these systems was controlled by the pile capacity.



Figure 4.22: Sample moment versus deflection responses for 30-inch piles with: (a) shallow $(0.25d_b)$; (b) deep $(1.5d_b)$ embedment with varying pile concrete strength. (f'_{c, cap} = 5.5 ksi)

4.2.5 Effect of Pile-Cap Concrete Strength

The influence of the pile-cap concrete strength on the behavior of the system was investigated with $0.1A_g f'_c$ (axial compression) and $-0.1A_g f'_c$ (axial tension), shown in Figure 4.23 and Figure 4.24, respectively. In both cases, the concrete strength only affected the strength of the system when the connection failed before the pile, as in Figure 4.23 (a) and Figure 4.24 (a). Because increasing the pile-cap concrete strength increased the strength of the system, the system is likely controlled by the crushing of the pile-cap concrete next to the embedded pile. The strength of the system was unaffected by an increase in pile cap concrete strength when failure occurred in the pile.



Figure 4.23: Sample moment versus deflection responses for 18-inch piles with: (a) shallow $(0.25d_b)$; (b) deep $(1.5d_b)$ embedment with axial compression and varying pile cap concrete strength. ($f'_{c, pile} = 6.0 \text{ ksi}$)



Figure 4.24: Sample moment versus deflection responses for 18-inch piles with: (a) shallow $(0.25d_b)$; (b) deep $(1.5d_b)$ embedment with axial tension and varying pile cap concrete strength. ($f'_{c, pile} = 6.0 \text{ ksi}$)

4.2.6 Effect of Pile Cap Size

Five different pile cap sizes were investigated, shown Figure 4.25. AASHTO LRFD requires a minimum distance from the side of any pile to the nearest edge of the pile cap to be more than 9-inch, including casting and placement tolerances. A PC1* was created only for the 18-inch specimen, with a smaller width dimension, to simulate the behavior if this requirement is not met.



Figure 4.25: Investigated pile cap sizes for analytical program.

The size of the pile cap generally did not affect the behavior of the connection. Sample moment versus deflection responses for the systems with 30-inch piles are shown in Figure 4.26 for shallow and deep pile embedment. The capacity of the system with the shallow embedment was only affected by the pile cap size with a $2d_p$ length, Figure 4.26 (a). The pile cap size has no influence on the system performance when failure was controlled by the pile, Figure 4.26 (b).



Figure 4.26: Sample moment versus deflection responses for 30-inch piles with: (a) shallow $(0.25d_b)$; (b) deep $(1.5d_b)$ embedment with different pile cap sizes.

4.2.7 Effect of Reinforcement around Pile

Confinement reinforcement around the pile did not have a significant effect on the performance of the system regardless of embedment length, as shown in Figure 4.27. This would suggest that the

cap (without the additional confinement reinforcement) already had enough reinforcement close enough to the embedded pile to sufficiently confine the concrete bearing against the pile.



Figure 4.27: Sample moment versus deflection responses for 18-inch piles with: (a) shallow $(0.25d_b)$; (b) deep $(1.5d_b)$ embedment with and without confinement reinforcement around embedded pile.

4.2.8 Effect of Strand Pattern

The effect of the strand pattern on the behavior of the system is shown in Figure 4.28.



Figure 4.28: Sample moment versus deflection responses for 18-inch piles with: (a) shallow $(0.25d_b)$; (b) deep $(1.5d_b)$ embedment with different strand patterns.

The strand type and pattern had minimal effect on the behavior of the system. A monitor was placed in all the strands for the 24-inch specimens to measure the maximum stress in the strand along the length. As shown in Figure 4.29, the strands were not able to fully develop in shorter embedment lengths. The length required to develop the strand is significantly shorter than the required development length from AASHTO LRFD [3]. This may be due to the large compression

stresses adjacent to the strands caused by the compression block in the pile bearing against the pile cap as bending of the pile takes place. This should be further investigated during the experimental testing program to see if the development lengths are truly this short. Experimental results from 0.5-inch diameter strands should indicate how 0.6-inch strands will behave (and vice versa), so strand diameter is not thought to be a variable that should be investigated in the experimental program.



Figure 4.29: Maximum stress in prestressing strands in 24-inch piles with different embedment lengths.

4.2.9 Summary of Results of Preliminary Numerical Study

One of the primary goals of the preliminary computational analyses of the pile-to-cap connection was to determine the variables that should be investigated in the experimental program. The following conclusions were made from these analyses:

- 1. Embedment length appears to be linearly related to the moment capacity of the connection until the capacity of the pile is reached. The embedment length was selected as the primary variable investigated in the experimental program. The development of the prestressing strands likely controls the failure of shallower embedment lengths, so instrumentation was designed in the experimental program to measure developed stresses and factors that affect development length.
- 2. Shallow pile embedment still developed significant moment, so it is not likely that a shallow embedment alone can provide an adequate pin connection. Interface reinforcement between the pile and pile cap provides shorter embedment lengths to develop higher moments than those without interface reinforcement. An alternate detail, with interface reinforcement between the pile and the pile cap was during the experimental program.
- 3. There appears to be a similar ratio between the normalized moment and normalized embedment length for 18-inch, 24-inch, and 30-inch piles. Only two different pile sizes were selected to test in the experimental program (18-inch and 30-inch piles).
- 4. Additional axial compression improves the performance of the connection and increases the moment capacity in the pile. Specimens with no axial load were included in the experimental matrix, in addition to the specimens with $0.1A_g f'_c$ axial compression, to get more conservative values for shallow embedment.
- 5. Pile concrete strength did not impact the performance of the shallow embedment in the models.
- 6. Pile-cap concrete strength did affect the performance of the connection, as it appears that concrete crushing in the pile cap adjacent to the embedded pile controlled failure.

- 7. The size of the pile cap did not seem to have a significant effect on the performance of the connection. Confinement reinforcement around the pile also did not have a significant effect. Both observations are likely a result of there being enough reinforcement in the cap to confine the embedded pile and prevent splitting of the cap before concrete crushes next to the pile. A reinforcement detail that closely resembles current practice was selected, but these were not variables investigated in the experimental program.
- 8. There was little difference observed between the connection performance for piles with 0.5-inch and 0.6-inch diameter prestressing strands. There was a significantly shorter development length observed from the numerical analysis results. Strand stress was monitored near the location of the edge of the pile in the experimental program, but only one size of strand was selected.

Chapter 5: Experimental Program

The selection of the specimens to be tested was based on results from preliminary computational analyses. The primary variables selected for the initial specimens were pile size and embedment length. Axial load, interface reinforcement, and pile cap concrete strength were selected as secondary variables.

5.1 TEST MATRIX

The primary goal of the preliminary numerical analysis was to determine the variables that should be investigated in the experimental program. These preliminary analyses suggested that variables such embedment length, pile size, interface reinforcement, and axial load had more impact on the connection performance than pile concrete strength, size of the pile cap, and strand pattern. These results were used to develop the experimental test matrix. The experimental matrix is shown in Table 5.1.

Specimen No.	Pile Size	Embedment	Length	Interface Reinforcement		Axial Load	Pile Cap f'c
1	18"	$0.33 d_{pile}$	6.0"	w/o reinforcement	interface	$0A_g f'_c$	Class IV
2	18"	$0.33 d_{pile}$	6.0"	w/o reinforcement	interface	$0.1A_g f'_c$	Class IV
3	18"	$0.33 d_{pile}$	6.0"	w/interface reinforcement		$0A_gf'_c$	Class IV
4	18"	$0.5d_{pile}$	9.0"	w/o reinforcement	interface	$0A_gf'_c$	Class IV
5	18"	$0.5 d_{pile}$	9.0"	w/o reinforcement	interface	$0.1A_g f'_c$	Class IV
6	18"	$0.67 d_{pile}$	12.0"	w/o reinforcement	interface	$0A_gf'_c$	Class IV
7	18"	1.0 <i>d</i> _{pile}	18.0"	w/o reinforcement	interface	$0A_gf'_c$	Class IV
8	18"	$1.5d_{pile}$	27.0"	w/o reinforcement	interface	$0A_gf'_c$	Class IV
9	30"	$0.4d_{pile}$	12.0"	w/o reinforcement	interface	$0A_gf'_c$	Class IV
10	30"	$1.0d_{pile}$	30.0"	w/o reinforcement	interface	$0A_gf'_c$	Class IV

Table 5.1: Proposed experimental matrix.

5.1.1 Primary Variables

5.1.1.1 Pile Size

The ratio between normalized moment and normalized embedment length for 18-inch, 24-inch and 30-inch appears to be similar (from the numerical study results). Therefore, only two different pile sizes (18-inch and 30-inch) were tested, as shown in Figure 5.1. The interface reinforcement is shown in Figure 5.1, but this was only included in one specimen.



Figure 5.1: Details for: (a) 18-inch; (b) 30-inch pile sizes.

5.1.1.2 Embedment Length

The embedment length had the largest impact on the strength and behavior of the pile-to-cap connection in the numerical study. There appeared to be a linear relationship between the embedment length and the moment capacity of the connection. The full moment capacity of the pile was achieved at approximately $1.0d_{pile}$, which is consistent with what was found in previous experimental testing. Four different embedment lengths were tested between partial and full moment connections and one longer embedment length $(1.5d_{pile})$ to ensure that a test is conducted where the full moment capacity can be developed.

5.1.2 Secondary Variables

5.1.2.1 Axial Load

From the numerical analysis results, axial load was found to improve the performance of the connection and increase the capacity of the pile itself. Two of the shallow embedment lengths (6" and 9") were tested with an axial load of $0.1A_g f'_c$, which is a typical axial compression range, to better understand how axial load improves connection performance.

5.1.2.2 Interface Reinforcement

An interface reinforcement detail based on Larosche et al. [18] was implemented for one of the specimen in the experimental program, as shown in Figure 5.1 and Figure 5.2. The presence of interface reinforcement was found in the numerical analyses to slightly decrease the embedment length required to develop the full moment capacity of the pile and increase the rotation capacity of the connection. The interface reinforcement had more of an effect on the behavior of the 18-inch piles compared to the 24 and 30-inch piles.



Figure 5.2: Details of proposed interface reinforcement for testing.

5.2 SPECIMEN DESCRIPTION

5.2.1 Pile Details

The pile details are based on the FDOT Standard Plans [51], as shown in Figure 5.3. All piles had a length of 18 feet. The load point will be kept consistent, so the distance from the load point to the end of the pile will vary with different pile embedment lengths.



Figure 5.3: Typical details for: (a) 18-inch; (b) 30-inch piles.

5.2.2 Pile Cap Details

The pile cap reinforcement scheme was selected considering previous research and select projects and following the FDOT Structures Detailing Manual [5].

5.2.2.1 Pile Cap Dimensions

The basic dimensions for the pile caps used in the experimental program are shown in Figure 5.4.



Pile Cap Sizes

(Width x Length x Height) $(3.0d_p \ge 5.0d_p \ge 2.0d_p^*)$ PC1 (18" piles) – 4.5' $\ge 7.5' \ge 3.0'$ PC2 (30" piles) – 7.5' $\ge 12.5' \ge 4.0'$ *PC2 only has a 1.8 d_p height due to demolition limitations

Figure 5.4: Pile cap dimensions for 18-inch and 30-inch piles.

The length of the pile caps was selected considering center-to-center pile spacing and edge distance requirements, as shown in Figure 5.5. FDOT Structures Detailing Manual [5] (§ 3.5.4) specifies that center-to-center pile spacing should not be less than $3.0d_{pile}$, and AASHTO LRFD [3] (§10.7.1.2) specifies the minimum edge distance as 9-inch. In common practice, the edge distance varies with pile size; it is typical practice to use a minimum edge distance of $0.5d_{pile}$, which is equal to the 9-inch minimum requirement for 18-inch piles and is 15 inches for 30-inch piles. The width of the pile caps was selected to have a $1.5d_{pile}$ distance between the center of the pile and edge of the pile cap, which is equal to half of the minimum center-to-center pile spacing. The height of the pile caps was selected to be $2.0d_{pile}$ for the 18-inch specimens. For the 30-inch pile cap the height was fixed to 54-inch because of weight limits of the specimen.



Figure 5.5: General pile cap dimension details: (a) plan; (b) elevation views.

5.2.2.2 Reinforcement Specifications

• Minimum Spacing of Bars

For cast-in-place (CIP) concrete, AASHTO LRFD [3] (§5.10.3.1.1) specifies that the distance between parallel bars in a layer should not be less than the largest of the following:

- 1.5 times the nominal diameter of the bars
- 1.5 times the maximum size of the coarse aggregate
- 1.5 inches

The minimum spacing of bars was checked for all reinforcement, but specifically for the longitudinal reinforcement in the top and bottom of the pile cap.

• Maximum Spacing of Bars

FDOT Structures Detailing Manual [5] §4.3.1 specified maximum bar spacing according to AASHTO LRFD [3] §5.10.6. The area of reinforcement per foot on each face and in each direction should satisfy the following equation:

$$A_s \ge \frac{1.30bh}{2(b+h)f_y}$$
 AASHTO LRFD 2017
(5.10.6-1)
0.11 $\le A_s \le 0.60$ (5.10.6-2)

where:

- A_s = area of reinforcement in each direction and each face (in²/ft)
- b = least width of component section (in)
- h = least thickness of component section (in)
- f_y = specified minimum yield strength of reinforcement \leq 75 ksi

The spacing of the reinforcement shall not exceed 12 inches for walls and footings greater than 18 inches thick.

The required reinforcement for the 18-inch and 30-inch pile cap specimens are summarized in Table 5.2.

<i>d_{pile}</i> (in)	<i>b</i> (in)	<i>h</i> (in)	f_y (ksi)	A _{s,req} (in ² /ft)
18	54	36	60	0.234
30	90	54	60	0.366

Table 5.2: Minimum required reinforcement on each face of pile cap

The skin reinforcement in the pile caps was designed to meet these minimum area and maximum spacing requirements.

• Minimum Concrete Cover

The requirements for concrete cover are listed in the FDOT Structures Design Guidelines [5] §1.4.2. For external surfaces cast against earth and surfaces in contact with water the recommended cover is 4 inches; and for exterior formed surfaces, columns, and tops of footing not in contact with water is 3 inches, for slightly and moderately aggressive environments. A sample detail for a pile cap is shown in Figure 5.6.



Figure 5.6: Sample cover requirements from FDOT Structures Design Guidelines [5].

A slightly aggressive (S) or moderately aggressive (M) exposure condition was assumed for the developed details.

• Maximum Reinforcing Steel Bar Sizes

FDOT Structures Detailing Manual [5] §4.3.11 specifies a maximum reinforcing steel bar size of #11 bars for footings. The maximum bar size used in the pile caps is #9 bars for the longitudinal steel.

5.2.2.3 Basis for Pile Cap Reinforcement Scheme

The reinforcement scheme used for the pile caps was based primarily on two research projects (Larosche et al. [18] and Issa [2]) and contract plans obtained for two constructed bridges (from the ABC Project Database [59]). An initial pile cap reinforcement scheme was developed and then refined based on discussions with FDOT and Corven Engineering, Inc.

Larosche et al. [18] investigated several different pile cap details with 18-inch square prestressed concrete piles. Their control specimen had an 18-inch embedment (embedment equal to pile size) and pile cap dimensions and reinforcement detail in line with the practice used at the time in South Carolina, as shown in Figure 5.7. Reinforcement included five No. 9 in the top spaced evenly across the width of the cap and four No. 9 placed in the bottom. Shear reinforcement consisted of No.5 bars spaced at 6-inch. And four No.6 bars as skin reinforcement, spaced evenly between top and bottom.



Figure 5.7: Typical pile cap reinforcement from Larosche et al. [18].

Issa [2] tested two 30-inch square prestressed piles with 48-inch embedment into a single pile cap. A schematic of the reinforcement scheme for this testing is shown in Figure 5.8 and a photograph of the reinforcement shown in Figure 5.9. A significant amount of reinforcement was provided in this cap.



Figure 5.8: Schematic of pile cap reinforcement scheme used by Issa [2]: (a) plan; (b) elevation views.



Figure 5.9: Photograph of pile cap reinforcement used by Issa [2].

Two sample contract plans were obtained from the ABC Project Database [59]; these are shown in Figure 5.10.



Figure 5.10: Sample pile cap reinforcement from: (a) UPRR Bridge 126.31; (b) Burnt River Bridge projects.

These sample reinforcement schemes were used as a starting point for the proposed pile cap reinforcement. The reinforcement scheme was further refined through discussion with FDOT engineers and amongst the project team.

5.2.2.4 Types of Pile Cap Reinforcement

The specimens with 18-inch and 30-inch piles had similar reinforcement schemes, except the amount of steel increases for the 30-inch pile cap. There are six different types of reinforcement that were considered for the pile cap reinforcement, as shown in Figure 5.11 and Figure 5.12. The longitudinal reinforcement, #9 bars spaced at 6.0 inches in Figure 5.11 (a), resists the flexural stresses that develop in the pile cap from bending of the piles. The vertical skin reinforcement, #5 bars at 5.5 inches in Figure 5.11 (b), and horizontal skin reinforcement, #6 bars at 6.0 inches in Figure 5.11 (b), helps to limit cracking of the pile cap and are consistent with what has been used in previous research and the sample contract plans. This reinforcement is typical for this type of pile cap.



Figure 5.11: Pile cap reinforcement: (a) primary tension; (b) vertical skin; (c) horizontal skin reinforcement.

The additional reinforcement that is not typical for this type of pile cap are shown in Figure 5.12. The interior horizontal reinforcement, Figure 5.12 (a), was used by Issa [2] and in the Burnt River Bridge project [59] and may help prevent splitting of the pile cap; this reinforcement is not typically provided. The interior vertical reinforcement, Figure 5.12 (b), is used when additional shear strength is needed. These members are typically designed to not require shear reinforcement for strength though, so this vertical reinforcement is typically not required. The confinement reinforcement around the pocket, Figure 5.12 (c), can be provided to help confine the pile, which is thought to decrease the development length of the prestressing strand in the pile. This confinement reinforcement is not typically provided though. The reinforcement shown in Figure 5.12 was not selected for the test specimens as it is not typical in pile caps.



Figure 5.12: Interior pile cap reinforcement: (a) horizontal; (b) vertical; (c) embedded pile confinement reinforcement.

5.2.2.5 Nominal Flexural Strength of Pile Cap

Loading of the piles in the proposed test setup will result in a large moment developing in the pile cap between the piles. The flexural strength of the pile cap must be greater than the demand with a sufficient factor of safety to prevent failure of the pile cap in flexure. The longitudinal reinforcement (#9 bars) will resist the tension developed by this moment. The moment demand on the pile caps when the piles are pushed together is shown in Figure 5.13.



Figure 5.13: (a) Moment demand on pile cap for piles being pushed together; (b) cross section with 18-inch pile; (c) cross section with 30-inch pile.

The moment demand will be opposite if the piles are pushed apart, as shown in Figure 5.14. There is less tensile reinforcement that will be available in this scenario because there is not longitudinal reinforcement extending the length of the pile cap at the location of the embedded piles.



Figure 5.14: (a) Moment demand on pile cap for piles being pushed apart; (b) cross section with 18-inch pile; (c) cross section with 30-inch pile.

The nominal moment can be found using rectangular stress block assumptions and equilibrium, shown in Equation 5.1 and Equation 5.2.

Nominal Moment:
$$M_n = A_s f_y \left(d - \frac{\beta_1 c}{2} \right)$$
Equation 5.13Stress block: $c = \frac{A_s f_y}{0.85 f'_c \beta_1 b}$ Equation 5.14

The nominal flexural strength for the pile caps compared to the moment demand in each case are summarized in Table 5.3, where PC18-1 is 18-inch pile with piles being pushed together and PC 18-2 is the 18-inch pile with piles being pushed apart for testing.

	PC18-1	PC18-2	PC30-1	PC30-2
<i>h</i> (in)	36	36	54	54
<i>d</i> (in)	32	32	50	50
<i>b</i> (in)	54	54	90	90
A_s (in ²)	9.0	6.0	15.0	10.0
f_{y} (ksi)	60	60	60	60
f'_c (ksi)	6.0	6.0	6.0	6.0
β_I	0.75	0.75	0.75	0.75
<i>c</i> (in)	2.61	1.74	2.61	1.74
\mathcal{E}_{S}	0.0337	0.0521	0.0544	0.0831
M_n (kip-in)	16,751	11,285	44,118	29,608
M_u (kip-in)	3,708	3,708	13,176	13,176
M_n/M_u	4.52	3.04	3.35	2.25

Table 5.3: Pile cap flexural capacity between piles

The pile cap had sufficient flexural capacity between the piles in all cases as long as all the longitudinal reinforcement is engaged.

5.2.2.6 Engagement of Longitudinal Reinforcement

One question that arose during the development of the pile cap reinforcement scheme is what longitudinal reinforcement will be engaged when there is a small distance provided between the edge of the pile and edge of the pile cap, as shown in Figure 5.15. Some designers select the distance between the pile and edge of the pile cap based on the size of the longitudinal reinforcement and bend diameter of this reinforcement. Common practice is to ensure that the standard hook dimension ends before the edge of the pile, as shown in Figure 5.15 (a). There is no specification on this, but this can lead to a larger edge distance than the minimum 9 inches allowed by AASHTO LRFD.



Figure 5.15: (a) Engagement of longitudinal reinforcement around pile; (b) cross section of typical longitudinal reinforcement; (c) cross section with possible bar bundling if reinforcement engagement does control.

The development length of the longitudinal reinforcement (#9 bars) was found using AASHTO LRFD [3] §5.10.8.2.4.a

Development length:

 $l_{dh} = l_{hb} \left(\frac{\lambda_{rc} \lambda_{cw} \lambda_{er}}{\lambda} \right)$ Equation 5.15 $\lambda_{rc} = \lambda_{cw} = \lambda_{er} = \lambda = 1.0$

Equation 5.4

Not epoxy coated, normal - weight concrete:

Basic development length:

Development length:

$$l_{dh} = l_{hb} = \frac{38(1.128")}{60.0} \left(\frac{60ksi}{\sqrt{5.5ksi}}\right) = 18.3"$$

 $l_{hb} = \frac{38d_b}{60.0} \left(\frac{f_y}{\sqrt{f'c}}\right)$

where:

 l_{dh} = development length (in)

 l_{hb} = basic development length (in)

 λ_{rc} = reinforcement confinement factor

 λ_{cw} = coating factor

 λ_{er} = excess reinforcement factor

- d_b = nominal diameter of reinforcing bar or wire (in)
- f'_c = compressive strength of concrete for use in design not to be taken greater than 15.0 ksi for normal weight concrete and 10.0 ksi for lightweight concrete (ksi)
- f_y = specified minimum yield strength of reinforcement (ksi)
- λ = concrete density modification factor as specified in AASHTO LRFD Article 5.4.2.8

The available development is the distance from the back of the hook to the point where the full moment demand is required, which is assumed to be at the mid-depth of the embedded pile, as shown in Figure 5.15. The required development length (18.3 in) is less than the available development length (20.5 in), so the yield stress can be developed in this reinforcement.

The pile cap reinforcement is proposed to have typical distributed bars with strain gauges to measure which bars are engaged during testing.

An additional bar will be provided inside the bend on one side of the pile cap, as shown in Figure 5.15 (a), to see how this improves the engagement of reinforcement and if it improves the behavior of the connection.

5.3 TEST SETUP

Three different test setups were considered for testing of these specimens, as shown in Figure 5.16. Each of the test frames was evaluated based on the impact of support conditions on the connection behavior (using numerical analyses) and available steel beams in FDOT's Structures Research Center (SRC).



Figure 5.16: Investigated options for test setup: (a) rear support; (b) top support; (c) self-reacting frames.

The selected test setup was a self-reacting frame system with two piles, as shown in Figure 5.17. The self-reacting frame was decided to have the least impact on the connection behavior and the simplest setup in the lab.



Figure 5.17: Schematic of proposed test setup: (a) elevation; (b) plan view.

Loading the piles from the outside (pushing pile ends together) and from the inside (pushing pile ends apart) were also both evaluated using numerical modeling. One of the primary objectives of the testing was to evaluate the connection based on the minimum possible edge distance. Loading the piles from the inside was found to lead to higher stresses at the edges of the pile caps than loading from the outside. A sample of the numerical results is provided in Figure 5.18 for a shallow embedment of $0.25d_p$ where the pile reached a moment of 253.5 kip-ft, which is approximately 82% of their moment capacity.



Figure 5.18: Numerical analyses for test setup.

5.3.1 Spreader Beams

The test setup did not require any spreader beams when no axial load is applied. The only connection was four threaded rods extending through the specimens and attaching the specimen to the strong floor, as shown in Figure 5.19 (a). These were not required for the boundary condition but were used to stabilize the specimens during testing.

This test set up required four spreader beams when an axial load was applied. Two at the end of the piles and two restraining the back of the pile cap, as shown in Figure 5.19(b).



Figure 5.19: (a) Tie down point to strong floor; (b) setup for axial load application.

5.3.2 Threaded Rods

Three different threaded rod lengths were required for axial load application and securing the specimens to the strong floor, as shown in Figure 5.20. The threaded rods have the following naming convention:

• Rod 1: correspond to the rods extending through the pile cap and attaching the specimen to the strong floor,

- Rod 2: correspond to the rods attached to the spreader beams at the back of the cap, extending through the pile cap, and attached to the pin connection,
- Rod 3: corresponds to the rods connected to the pin connection, extending the length of the pile, and attached to the spreader beams at the end of the piles.

Rods 2 and 3 transferred the tension applied by the hydraulic jack to the back of the pile cap to apply the constant axial load to the piles.



Figure 5.20: Threaded rods configuration.

5.4 EXPERIMENTAL PROCEDURE

5.4.1 Without Axial Load

No spreader beams were required for the specimens tested without axial load, and only the threaded rods attaching the pile cap to the strong floor were needed. The experimental procedure consisted of the application of the lateral load using a hydraulic jack pushing the piles apart until failure, as shown in Figure 5.21 (a).

Preliminary numerical models for shallow embedment showed a maximum displacement of 1.2 inch and an anticipated failure load of 19.6 kips for the 18-inch piles. For 30-inch piles with shallow embedment preliminary results showed a maximum displacement of 0.5 inch and an anticipated failure load of 61.5 kips. For deeper embedment lengths $(1.5d_{pile})$, the predicted failure load for 18-inch and 30-inch piles increase approximately to 32 kips and 118 kips, respectively. Numerical results are shown in Figure 5.21 (b) and (c), where the red dashed line represents the pile capacity.



Figure 5.21: (a) Experimental procedure without axial load; (b) numerical modeling results for shallow embedment for 18-inch piles; (c) numerical modeling results for shallow embedment for 30-inch piles.

The piles were loaded incrementally until failure. The loading protocol for strength testing consisted of 5 loading steps, shown in Table 5.4. The specimens were visually inspected for cracks and photographs were taken between each of the loading stages. The first cracking load from visual observation was documented along with the location of first cracking.

	Specimen Description				Loading	Protocol		
Specimen	Pile Size	Predicted Failure Load	Load Rate	Step 1	Step 2	Step 3	Step 4	Step 5
1	18"	25 kips	0.03 kip/s	3 kips	6 kips	9 kips	15 kips (60% est. capacity)	Load to failure
3	18"	30 kips	0.03 kip/s	4 kips	8 kips	12 kips	18 kips (60% est. capacity)	Load to failure
4	18"	30 kips	0.03 kip/s	4 kips	8 kips	12 kips	18 kips (60% est. capacity)	Load to failure
6	18"	31 kips	0.03 kip/s	4 kips	8 kips	12 kips	18 kips (60% est. capacity)	Load to failure
7	18"	32 kips	0.03 kip/s	4 kips	8 kips	12 kips	18 kips (60% est. capacity)	Load to failure
8	18"	35 kips	0.03 kip/s	5 kips	10 kips	15 kips	21 kips (60% est. capacity)	Load to failure
9	30"	60 kips	0.1 kip/s	9 kips	18 kips	27 kips	36 kips (60% est. capacity)	Load to failure

Table 5.4: Loading protocol for specimens without axial load

	Specimen Description				Loading	Protocol		
Specimen	Pile Size	Predicted Failure Load	Load Rate	Step 1	Step 2	Step 3	Step 4	Step 5
10	30"	115 kips	0.1 kip/s	17 kips	34 kips	51 kips	69 kips (60% est. capacity)	Load to failure

Table 5.4: Loading protocol for specimens without axial load- Continued

5.4.2 With Axial Load

Spreaders beams at the back of the pile cap and at the end of the piles were needed for the application of the axial load. The experimental procedure consisted of two primary steps, as shown in Figure 5.22. First, the axial load was applied through two center-hole hydraulic jacks to the threaded rods, which transferred the tension to the pile cap. Two center hole hydraulic jacks with 60-ton capacity were used to tension the threaded rods (e.g., Enerpac Tall Blue) and put the piles in axial compression.

Once the desired axial load was reached it was left constant during the rest of the experimental procedure. Finally, a lateral load was applied using hydraulic jacks pushing the piles apart until failure of the specimens occurred.



Figure 5.22: Experimental procedure with axial load: (a) application of axial load; (b) application of lateral load.

The piles were loaded incrementally until failure. The loading protocol for strength testing consisted of 5 loading steps, shown in Table 5.5. The specimens were visually inspected for cracks and photographs were taken between each of the loading stages. The first cracking load from visual observation as be documented along with the location of first cracking.

	Specimen Description				Loading	Protocol		
Specimen	Pile Size	Predicted Failure Load	Load Rate	Step 1	Step 2	Step 3	Step 4	Step 5
2	18"	25 kips	0.03 kips/s	3 kips	6 kips	9 kips	15 kips (60% est. capacity)	Load to failure
5	18"	30 kips	0.03 kips/s	4 kips	8 kips	12 kips	18 kips (60% est. capacity)	Load to failure

Table 5.5: Loading protocol for specimens with axial load

5.5 INSTRUMENTATION PLAN

A general overview of the instrumentation is provided in this section.

5.5.1 Deflection Gauges

Load cells were located next to the hydraulic jack to measure the load that was being applied to the piles. Fourteen laser displacement transducers (LDTs) were placed across the length of the piles and cap, to measure deflection. Additionally, two LDTs were place on top of the piles to measure out-of-plane displacement. Figure 5.23 shows details of these gauges.

The length of the plastic hinge zone is 2.5 feet which was estimated based on visual observations of damage in the numerical models, as shown in Figure 5.24. To measure curvature in the plastic hinge region of the piles, sixteen (16) crack displacement transducers were placed along both sides of the piles, as shown in Figure 5.25 These CDTs measured the curvature and rotation of the pile in the plastic hinge zone.



Figure 5.23: Deflection gauges (LVDT) and load cells (top view).



Figure 5.24: Plastic hinge zone observation assumptions.



Figure 5.25: CDT in the plastic hinge zone.

5.5.2 Surface Gauges

Preliminary numerical analyses were performed using a shallow and deep pile embedment, as shown in Figure 5.26. Cracking patterns were obtained for the models to determine the mode of failure controlling the specimens. Shallow embedment resulted in failure of the cap, as shown in Figure 5.26 (a). Deeper embedment resulted in failure of the piles, as shown in Figure 5.26 (b).



Figure 5.26: ATENA modeling for specimens: (a) shallow embedment; (b) deep embedment.

These cracking patterns were used to determine the location of the concrete surface gauges. For a shallow and deep embedment, the pile cap is showing failure in the front face between the piles and in the edges. Cracking is also happening in the lateral faces of the cap. A total of 25 concrete surface gauges (CSGs) were used, 19 located on the front view of the pile cap, and three on each lateral face, as shown in Figure 5.27. CSGs perpendicular to the load application measured the splitting stresses that develop in the pile cap. CSGs parallel to load application measured the compressive stress developing from the pile bearing on the pile cap (on the outside) and the tensile stresses developing from flexure on the pile cap (between the piles).



Figure 5.27: Concrete surface gauges: (a) side view; (b) front view.

5.5.3 Rebar Gauges

The stress in the rebars in the numerical analyzes are shown in Figure 5.28. The longitudinal reinforcement resisting the flexural stresses in the pile caps was heavily engaged, as shown in Figure 5.28 (c). The transverse reinforcement on the face of the pile cap where the piles extend from are also engaged, as shown in Figure 5.28 (a) and (b).



Figure 5.28: Stress in rebars: (a) N6 bars; (b) N5 bars; (c) N9 bars.

Rebar strain gauges (RSGs) were used to measure the strain in the reinforcement with the highest observed stresses from the numerical analyses. The RSG layout is shown in Figure 5.29 with a total of 36 RSGs per specimen.



Figure 5.29: Rebar strain gauges: (a) side view; (b) front view.

5.5.4 Vibrating Wire Strain Gauges (VWSG)

Vibrating wire strain gauges (VWSGs) were used to measure the confining stresses in the pile caps around the embedded piles, as shown in Figure 5.30. Two VWSGs were also placed in the precast piles to measure the prestress losses and shrinkage strains that occur in the piles before being cast in the pile caps.



Figure 5.30: Vibrating wire strain gauges.

5.5.5 Fiber Optic Sensors

Fiber optic sensors were used to measure the behavior of the embedded portion of the pile and the rotation in the plastic hinge zone to determine the exact point at which fixity occurs in the embedded portion of the pile. The fiber optic sensors were attached to a #3 GFRP bar for internal embedment, as shown in Figure 5.31. The fiber optic gauges extended 72 inches from the end of the pile for all specimens (18-inch and 30-inch piles of all embedment lengths).



Figure 5.31: Proposed location for the fiber optic sensors.

5.6 SPECIMEN CONSTRUCTION

The 18-inch specimens (18-inch piles and caps with embedded piles) and 30-inch piles were constructed by CDS Manufacturing in Tallahassee, FL. A total of 20 piles and eight pile caps were cast at CDS Manufacturing. The 30-inch pile caps for Specimen 9 and Specimen 10 were constructed by Florida Department of Transportation at the SRC with concrete delivered from Smyrna Ready Mix (SRM). A summary of casting and testing dates is provided in Table 5.6. Construction drawings for all piles and pile cap specimens are provided in Appendix.

Specimen	Pile Cast Date (West)	Pile Cast Date (East)	Cap Cast Date	Test Date	West Pile Age (days)	East Pile Age (days)	Cap Age (days)
SP-01	4/21/2021	4/21/2021	8/25/2021	4/18/22	362	362	236
SP-02	4/13/2021	4/13/2021	8/19/2021	8/4/22	478	478	350
SP-03	4/13/2021	4/13/2021	8/26/2021	4/22/22	374	374	239
SP-04	4/21/2021	4/13/2021	8/27/2021	5/9/22	383	391	255
SP-05	4/21/2021	4/21/2021	8/30/2021	8/1/22	467	467	336
SP-06	4/13/2021	4/21/2021	9/1/2021	5/12/22	394	386	253
SP-07	4/13/2021	4/21/2021	10/12/2021	5/31/22	413	405	231
SP-08	4/13/2021	4/21/2021	10/14/2021	6/3/22	416	408	232
SP-09	1/7/2021	1/7/2021	12/20/2022	1/19/23	742	742	30
SP-10	1/7/2021	1/7/2021	3/13/2023	4/3/23	816	816	21

Table 5.6: Summary of casting and testing dates

5.6.1 18-inch Specimens

A total of sixteen (16) 18-inch piles and eight pile caps were constructed at CDS Manufacturing between April 2021 and October 2021. The construction process is shown in Figure 5.32.



Figure 5.32: 18-inch specimen construction: (a) pile casting; (b) pile cap casting.

The piles were cast with a Class VI FDOT mixture [5] with a specified concrete compressive strength of 8.5 ksi. CDS Manufacturing uses a Class VI FDOT mixture for all members cast at their facility. The 18-inch piles had a strand configuration of (12) ½-in special strands stressed at 34 kips. The first casting phase for the piles started 4/13/2021 with detensioning on 4/14/2021. The second phase started 4/20/2021 with detensioning on 4/21/2021. A summary of the piles

casting dates and instrumentation are shown in Table 5.7. No vibrating wire strain gauges were installed in pile P9 through P16. A different labeling system was used by CDS Manufacturing and FDOT, as shown in Table 5.7.

Pile FDOT label	Pile CDS label	Casting Date	Fiber Optic Sensors	Vibrating Strain Gauges
P1	FIU-18-001	4/13/2021	FOS 01 FOS 09	VWSG-P1-1E VWSG-P1-2E VWSG-P1-3E
P2	FIU-18-002	4/13/2021	FOS 02 FOS 10	VWSG-P2-1E VWSG-P2-2E VWSG-P2-3E
Р3	FIU-18-003	4/13/2021	FOS 03 FOS 11	VWSG-P3-1E VWSG-P3-2E VWSG-P3-3E
P4	FIU-18-004	4/13/2021	FOS 04 FOS 12	VWSG-P4-1E VWSG-P4-2E VWSG-P4-3E
P5	FIU-18-010	4/21/2021	FOS 17 FOS 25	VWSG-P5-1E VWSG-P5-2E VWSG-P5-3E
P6	FIU-18-012	4/21/2021	FOS 18 FOS 26	VWSG-P6-1E VWSG-P6-2E VWSG-P6-3E
Р7	FIU-18-014	4/21/2021	FOS 19 FOS 27	VWSG-P7-1E VWSG-P7-2E VWSG-P7-3E
Р8	FIU-18-016	4/21/2021	FOS 20 FOS 28	VWSG-P8-1E VWSG-P8-2E VWSG-P8-3E
Р9	FIU-18-008	4/13/2021	FOS 05 FOS 13	-
P10	FIU-18-007	4/13/2021	FOS 06 FOS 14	-
P11	FIU-18-006	4/13/2021	FOS 07 FOS 15	-
P12	FIU-18-005	4/13/2021	FOS 08 FOS 16	-
P13	FIU-18-009	4/21/2021	FOS 21 FOS 29	-
P14	FIU-18-011	4/21/2021	FOS 22 FOS 30	_
P15	FIU-18-013	4/21/2021	FOS 23 FOS 31	-
P16	FIU-18-015	4/21/2021	FOS 24 FOS 32	-

Table 5.7: Summary of 18-inch piles

The 18-inch pile caps were constructed between $\frac{8}{2}/2021$ and $\frac{10}{14}/2021$. A summary of casting dates and description of each specimen is shown in Table 5.8.

Specimen	Casting Date	Target Embedment	East Pile	West Pile
SP-01	8/25/2021	$0.33 d_{pile}$ (6")	FIU-18-016	FIU-18-008
SP-02	8/19/2021	$0.33 d_{pile}$ (6")	FIU-18-002	FIU-18-001
SP-03	8/26/2021	$0.33 d_{pile}$ (6")	FIU-18-010	FIU-18-009
SP-04	8/27/2021	0.5 <i>d</i> _{pile} (9")	FIU-18-013	FIU-18-011
SP-05	8/30/2021	$0.5 d_{pile} (9")$	FIU-18-014	FIU-18-015
SP-06	9/1/2021	0.67 <i>d</i> _{pile} (12")	FIU-18-012	FIU-18-006
SP-07	10/12/2021	1.0 <i>d</i> _{pile} (18")	FIU-18-004	FIU-18-005
SP-08	10/14/2021	1.5 <i>d</i> _{pile} (27")	FIU-18-003	FIU-18-007

Table 5.8: Summary of 18-inch specimens

5.6.2 30-inch Specimens

A total of four 30-inch piles were cast at CDS Manufacturing and two pile caps at FDOT SRC. The construction process for the 30-inch specimens is shown in Figure 5.33.



Figure 5.33: Construction of the 30-inch specimens: (a) pile casting at CDS; (b) pile cap casting at FDOT SRC.

The piles were cast with a Class VI FDOT mixture [5] with a specified concrete compressive strength of 8.5 ksi. The 30-inch piles had a strand configuration of (24) $\frac{1}{2}$ -in special strands stressed to 34 kips. The casting date for the 30-inch piles was $\frac{1}{7}/2021$ with detensioning of strands on $\frac{1}{8}/2021$. A summary of the casting date and instrumentation is shown in Table 5.9.

Pile FDOT label	Pile CDS label	Casting Date	Fiber Optic Sensors	Vibrating Strain Gauges
P1	FIU-30-1	1/7/2021	FOS-P1-1E FOS-P1-1W	VWSG-P1-1E VWSG-P1-2E VWSG-P1-3E
P1	FIU-30-2	1/7/2021	FOS-P1-2E FOS-P1-2W	-
P2	FIU-30-3	1/7/2021	FOS-P2-1E FOS-P2-1W	VWSG-P2-1E VWSG-P2-2E VWSG-P2-3E
Р2	FIU-30-4	1/7/2021	FOS-P2-2E FOS-P2-2W	-

Table 5.9: Summary of 30-inch piles

The 30-inch pile caps were constructed at FDOT Research lab. A summary of the casting dates and description of each specimen is shown in Table 5.10.

Specimen	Casting Date	Target Embedment	East Pile	West Pile
SP-09	12/20/2022	0.33 d _{pile} (12")	FIU-30-1	FIU-30-2
SP-10	3/13/2022	$1.0 d_{pile}(30")$	FIU-30-3	FIU-30-4

Table 5.10: Summary of 30-inch specimens

Due to the large pile cap dimensions (7.5-ft. by 4.0-ft. by 12.5-ft.), the 30-inch pile caps were cast with a mass concrete mix. The mass concrete mix was developed in discussion with FDOT State Materials Office (SMO). A mass concrete mix is used when the element being constructed will likely exceed the maximum allowable temperature or temperature differential (between the center of mass and the surface of the element) during curing [5]. Too large of a temperature differential can lead to cracking of the concrete due to differential volume change (relative thermal expansion). According the FDOT Structures Design Guidelines [5] §1.4.4, the concrete element should be considered mass concrete if:

- The "least dimension" is more than 3 ft. and
- The volume-to-surface area (V/S) is greater than 1 ft.

The least dimension (LD) and volume-to-surface area (V/S) for the pile caps for the 30-inch piles are shown below.

Least dimension:
$$LD = 4.0 \text{ ft} > 3.0 \text{ ft}$$

V/S
$$\frac{V}{S} = \frac{375 \text{ ft}^3}{347.5 \text{ ft}^2} = 1.079 \text{ ft} > 1.0\text{ft}$$

where:

 $V = \text{pile cap volume (ft}^3)$

S = pile cap surface area (ft²)

The concrete mix recommended for the 30-inch pile caps by the mass concrete specialist at SRM in consultation with the FDOT SMO was a Class IV concrete mix design with 30% to 50% replacement of Portland Cement with Class F fly ash and total CM of 700 lb/yd³ or less. Superplastizers were added to the concrete mix to make it self-consolidating (SCC). Upon arrival of the concrete the Standard Slump Flow Test (ASTM C1611) was performed, as shown in Figure 5.34. The target slump flow for the SCC mix was between 23-30 inches.



Figure 5.34: Standard slump flow test for SP-10: (a) inverted mold; (b) slump of 25 inches. A summary of the results is shown in Table 5.11.

Table 5 11.	Ctan daud aluman	flow toat woonlta	for 20 in oh	mila agen gal	fannalidating	comonato min
ranie s rr:	Manaara suumb	now lest results	10r 30 - lncn	nne can sei	<i>i-consoliaating</i>	concrete mix
	Station of Station	<i>Jeon rest</i> . estats	<i>Jo. 20</i>	price emp seg	,	

Specimen	Batch	d1 (in)	d2 (in)	Slump flow (in)
SP-09	1	25	25	25
	2	15	15	15
SP-10	1	19	19	19
	2	25	24	24.5

FDOT Standard Specification for Road and Bridge Construction [60], Section 346-4.2, specifies that the concrete core temperature for any mass concrete element does not exceed the maximum allowable temperature of 180 °F and that the differential temperatures between the element core and surface do not exceed the maximum allowable temperature differential of 35 °F.

Temperature recordings were taking at the top, north side, west side, and core of the pile cap. For SP-09 readings were taken every minute the first day, and then every 30 minutes in the second and

third day. For SP-10 readings were taken every 30 minutes for 7 days. Temperature readings for Specimen 9 and Specimen 10 are shown in Figure 5.35.



Figure 5.35: Temperature readings: (a) SP-09; (b) SP-10.

Temperature gradients were calculated by finding the temperature difference at the top, north and west sides of the pile cap with the core temperature. Temperature gradients for Specimen 9 and Specimen 10 are shown in Figure 5.36



Figure 5.36: Temperature gradient: (a) SP-09; (b) SP-10.
After monitoring the temperature, the formwork was removed. No temperature or shrinkage cracks were observed on Specimen 9. Cracks developed on Specimen 10 at mid-height. Specimens 9 and 10 are shown in Figure 5.37.



(a)

(b)

Figure 5.37: Finished 30-inch specimens: (a) SP-09; (b) SP-10.

5.7 TEST SETUPAND PROTOCOL

5.7.1 Without Axial Load Application

A self-reacting frame system was used for specimens without axial load application, as shown in Figure 5.38. This frame was determined to be the simplest setup to be used in SRC and have the least impact on the pile-to-cap connection behavior. Four threaded rods were extended through the pile caps and attached to the strong floor to provide additional stability to the specimen during testing. Specimen 10 was not fixed to the strong floor to simplify demolition. Wood supports were constructed and located at ends of the piles with Teflon installed between the pile and support to minimize friction between elements.



Figure 5.38: Test setup for specimens without axial load application.

The piles were loaded from the inside using a hydraulic jack located between 6 ft. and 12 ft. from the pile-to-cap interface. The piles were loaded incrementally until failure. The loading protocol for strength testing consisted of different loading steps, which were pre-determined based on numerical modeling results. The specimens were visually inspected for cracks, and photographs were taken between each of the loading stages.

5.7.2 Axial Load Application

A self-reacting frame with spreader beams was used for specimens with axial load application, as shown in Figure 5.39. A total of four spreader beams was installed, two at the end of the piles and two restraining the back of the pile cap. Threaded rods extended from the spreader beam bearing against the back of the pile cap to steel hinges and clevises located at the face of the cap. Additional threaded rods extended from the clevis to the spreader beam on the end of the piles. These rods were used to transfer the tension applied to the piles by the hydraulic jack to the back of the pile cap. The hinge and clevis located at the face of the cap and base of the pile allowed for rotation of the pile during testing.



Figure 5.39: Test setup for specimens with axial load application.

A total of 193.8 kips was applied to each pile, which corresponded to $0.052A_g f'_{c,pile}$ (using the measured concrete strength). The applied axial load was less than the $0.1A_g f'_{c,pile}$ initially planned due to a higher measured concrete strength (11.5 ksi) than the design value (6.5 ksi). The axial load application apparatus (e.g., rods, hinge, spreader beams) were designed for the axial load of 194 kips.

The elongation of the threaded rod was estimated using Equation 5.4, to provide a validation to the pressure being read during the tensioning of the threaded rods.

 $\Delta_{rod} = \frac{FL}{AE}$

Equation 5.16

where:

- F = applied force
- L =length of the threaded rod
- A = area of the threaded rod
- E =modulus of elasticity

During tensioning, measures of the actual elongation were recorded in the four threaded rods (top and bottom of the east pile, and top and bottom of the west pile). A summary of the estimated and actual elongation for Specimen 2 and Specimen 5 are in Table 5.12.

	Estimated		Actual	Elongation	
Specimen	elongation (in)	Top East (in) Bottom East (in)		Top West (in)	Bottom West (in)
SP-02	0.411	0.879	0.699	0.709	0.787
SP-05	0.407			0.470	0.506

Table 5.12: Estimated and actual elongation for SP-02 and SP-05

The process to apply the axial load included the following steps:

- Blocks and jacks were positioned on the pile, as shown in Figure 5.40 (a).
- Pressure was applied manually to each rod in steps. Stops were set at 400 psi, 2,000 psi, 4,000 psi and 7,600 psi, which corresponds to 5%, 25%, 50%, 100% required for settlement support. Elongations reading was taken at each step and nuts were tightening.
- Blocks and jacks were removed after reaching 7,600 psi.

This process was followed to tension the west and east pile.



Figure 5.40: Axial load application: (a) tensioning of west pile; (b) tensioning east pile.

A similar process was followed for de-tensioning of the piles after testing.

5.8 PILES CAPACITY

5.8.1 Capacity of 18-inch Piles

Two 18-inch piles were cut from Specimen 2 after failure of the interface and tested for flexure in the FDOT SRC. The test setup consisted of a simply supported beam with two point loads, as shown in Figure 5.41.



(a)

(b)

Figure 5.41: Flexure test pile setup.

Both piles were cast on 4/13/2021 and had an age of 525 days on the day of testing (9/20/2022). The measured concrete strength on the day of testing was 11.45 ksi for both piles. A summary of the measured failure load, displacement at failure load, and moment capacity calculated from the measured failure load is shown in Table 5.13.

Pile	Failure Load (kips)	Displacement at Failure Load (in)	Moment Capacity (kip- ft)
P1	105.4	2.16	329.5
P2	106.4	2.06	332.5

Table 5.13: Summary of results flexure test

Displacements were recorded along the length of the piles through 10 laser displacement transducers (LDTs). Load versus displacement and moment versus displacement curves at midspan for both piles are shown in Figure 5.42. The maximum load reached by Pile 1 was 105.4 kips, which corresponds to a moment capacity of 329.5 kip-ft. Pile 2 reached a maximum load of 106.4 kips, with a moment capacity of 332.5 kip-ft. The average moment capacity for the 18-inch pile is 331 kip-ft.



Figure 5.42: (a) Load versus displacement; (b) moment versus displacement curves for Pile 1 and Pile 2.

Fiber optic sensors (FOS) were located at the west side of the pile to measure strains at two depths, which allows for curvature to be calculated. One FOS was located 4 inches from the top face of the pile and one FOS 6 inches from the bottom face of the pile. The average strain in the constant moment region was used; a strain of $10,000\mu\epsilon$ was used when the sensor exceeded this strain at a location. The strain profile at midspan for both piles is shown in Figure 5.43, assuming a linear strain profile between the two measured strains. The measurements by the FOS in the bottom of Pile 2 were not consistent with the observed behavior and expected readings in the sensor at loads above 70 kips. There may have been an issue with failure of the epoxy for the sensor at higher loads for this sensor in Pile 2.



Figure 5.43: Average measured strain profile in constant moment region for: (a) Pile 1; (b) Pile 2.

The curvature was determined from the measured strains in the FOS and the distance between the sensors. The moment-curvature response for both piles is shown in Figure 5.44. The moment capacity of the 18-inch determined using RESPONSE2000 was 325 kip-ft. There was good

agreement between the measured response for Pile 1 and the estimated response using RESPONSE2000.



Figure 5.44: Measured and estimated moment versus curvature response for Pile 1 and Pile 2.

5.8.2 Capacity of 30-inch Piles

The capacity of the 30-inch piles could not be tested experimentally because of limited time, the demolition required for the pile caps, and the length of the pile not being sufficient for a flexure test. There was good agreement between the measured results and estimated behavior from RESPONSE2000, so RESPONSE2000 was used to determine the baseline pile capacity for the 30-inch piles. The capacity of the 30-inch piles was found using the concrete strength on test day to be 1,188 kip-ft with the moment versus curvature response shown in Figure 5.45. The fundamental assumptions using the section analysis program RESPONSE2000 are as follows: 1) perfect bond between concrete and prestressing strands; 2) concrete spalls in compression and cracks in tension based on its stress-strain behavior.



Figure 5.45: Estimated moment versus curvature for 30-inch piles using RESPONSE2000.

5.9 SUMMARY OF RESULTS

Results of the experimental testing are summarized in this section. The results for each individual test, including graphs for all gauges, are provided in Appendix.

5.9.1 Specimen Detail Summary

A total of 10 specimens were tested at the FDOT Structures Research Center (SRC). The primary experimental variable was the embedment length, which varied from 0.33 to 1.5 times the diameter of the pile (d_p) . Two of the 18-inch specimens (SP-02 and SP-05) had an applied axial load, and one 18-inch specimen had interface reinforcement between the pile and the pile cap (SP-03). A summary of the experimental program is provided in Table 5.14.

The applied axial load was less than the $0.1A_g f'_{c,pile}$ initially planned due to a higher concrete strength (11.5 ksi) than the design value (6.5 ksi). A total of 193.8 kips was applied to each pile, which corresponded to $0.052A_g f'_{c,pile}$. The axial load application apparatus (e.g., rods, hinge, spreader beams) were designed for the axial load of 194 kips. A summary of the applied axial load is provided in Table 5.15.

Specimen	Pile Size (in)	A_g (in ²)	Embedment (in)	Embedment (<i>d</i> _p)	Axial Load (approx.)	Interface Reinforcement
SP-01	18	324	6	$0.33d_p$		
SP-02	18	324	6	$0.33d_p$	0.1Agfc	
SP-03	18	324	6	$0.33d_p$		(4) - #6 bars
SP-04	18	324	9	$0.50d_p$		
SP-05	18	324	9	$0.50d_p$	$0.1 A_{g} f_{c}$	
SP-06	18	324	12	$0.67d_p$		
SP-07	18	324	18	$1.00d_p$		
SP-08	18	324	27	$1.50d_p$		
SP-09	30	900	12	$0.40d_p$		
SP-10	30	900	30	$1.00d_p$		

Table 5.14: Experimental matrix for full-scale experimental test program

Specimen	Initial Axial Load	Applied Axial Load (kips)	Axial Load / Ag*f ^r c,pile
SP-01		0.0	0.000
SP-02	$0.1 A_{g} f_{c}$	193.8	0.052
SP-03		0.0	0.000
SP-04		0.0	0.000
SP-05	$0.1 A_{g} f_{c}$	194.0	0.050
SP-06		0.0	0.000
SP-07		0.0	0.000
SP-08		0.0	0.000
SP-09		0.0	0.000
SP-10		0.0	0.000

Table 5.15: Axial load applied to piles in each specimen.

5.9.2 Material Properties

Cylinders (4-inches diameter with 8-inches length) were cast with the same batch of concrete during casting of the piles and pile caps. These were used to determine the compressive strength at the time of testing. The measured compressive strength for the for piles and pile caps the day of testing are provided in Table 5.16. Initially, the pile cap concrete strength for the 18-inch specimens was selected per Structure Design Guidance to have specified concrete compressive strength of 5.5 ksi . Higher concrete strengths were obtained due to CDS Manufacturing using Class VI FDOT mixture for all members cast at their facility.

Specimen	f'c,pile,west (ksi)	f'c,pile,east (ksi)	f' _{c,cap} (ksi)
SP-01	11.90	11.90	12.48
SP-02	11.45	11.45	12.36
SP-03	11.58	11.58	12.70
SP-04	11.90	11.58	11.93
SP-05	12.02	12.02	13.26
SP-06	11.58	11.90	11.40
SP-07	11.58	11.90	10.32
SP-08	11.58	11.90	12.57
SP-09	13.13	13.13	9.37
SP-10	13.82	13.82	8.95

Table 5.16: Measured compressive strength on test day for concrete in piles and pile caps.

5.9.3 Transfer Length

5.9.3.1 Method for Determining Transfer Length

Transfer lengths were determined based on the 95% Average Maximum Strain (AMS) method developed by Russell and Burns [61] and used by Al-Kaimakchi and Rambo-Roddenberry [62]. In this method, the transfer length is determined to be the point where the strain curve intersects 95% of the average maximum strain, as shown in Figure 5.46.



Figure 5.46: 95% average maximum strain (AMS) method for determining transfer length from Russell and Burns [61].

The strains were measured using fiber optic sensors (FOS) for 10 to 15 minutes after detensioning of the last prestressing strands, which was about 25 minutes after the start of detensioning. The final readings at approximately 25 minutes were used. Strain measurements were taken every 0.25

inches starting at 1.0 inch from the end of the pile. Each pile had two FOS. Only one FOS was monitored during the detensioning process for the 18-inch piles. Both FOS sensors were monitored in each pile for the 30-inch piles.

The data was post-processed by first removing any extraneous readings, highlighted in a sample of the data processing for Pile 1 in Figure 5.47 (a). The data was then zeroed based on the first reasonable reading, highlighted in Figure 5.47 (b). The data was then smoothed using the same procedure as Russell and Burns and used by Al-Kaimakchi and Rambo-Roddenberry, as shown in Equation 5.5.

$$\varepsilon_i = \frac{\varepsilon_{i-1} + \varepsilon_i + \varepsilon_{i+1}}{3}$$
 Equation 5.17

The smoothed data in the sample for Pile 1 is shown in Figure 5.47 (c). The average maximum strain (AMS) was determined based on a range of stresses from when there was a noticeable change in slope in the strain diagram and the end of the FOS, shown in Figure 5.47 (c). The transfer length was then determined by finding the point when the measured strain reached 95% of the AMS, shown in Figure 5.47 (d).



Figure 5.47: Sample of data processing steps taken: (a) removing extraneous points; (b) zeroing based on first relevant point; (c) smoothing data and determining AMS; (d) determining transfer length.

5.9.3.2 Measured Transfer Lengths

A summary of the measured transfer lengths for 18-inch piles and 30-inch piles are shown in Table 5.17. The strand pattern in each pile was assumed to be symmetrical about both axes, so it was assumed that only axial strains would occur at release. For this reason, data was only recorded for one fiber optic sensor per pile for the 18-inch specimens. Both FOS in the 30-inch piles were monitored during release.

Specimen	Pile	Fiber Optic Sensors	Measured Transfer Length
SP-01	FIU-18-016	<i>FOS 20,</i> FOS 28	22.0"
	FIU-18-008	<i>FOS 05,</i> FOS 13	30.0"
SP-02	FIU-18-002	<i>FOS 02,</i> FOS 10	23.0"
	FIU-18-001	<i>FOS 01,</i> FOS 09	27.0"
SP-03	FIU-18-010	<i>FOS 17,</i> FOS 25	27.0"
	FIU-18-009	<i>FOS 21,</i> FOS 29	32.0"
SP-04	FIU-18-013	<i>FOS 23</i> , FOS 31	22.0"
	FIU-18-011	FOS 22, FOS 30	24.0"
SP-05	FIU-18-014	<i>FOS 19</i> , FOS 27	22.0"
	FIU-18-015	<i>FOS 24</i> , FOS 32	23.0"
SP-06	FIU-18-012	<i>FOS 18</i> , FOS 26	28.0"
	FIU-18-006	FOS 07, FOS 15	n/a
SP-07	FIU-18-004	<i>FOS 04,</i> FOS 12	25.0"
	FIU-18-005	<i>FOS 08,</i> FOS 16	30.0"
SP-08	FIU-18-003	<i>FOS 03,</i> FOS 11	28.0"
	FIU-18-007	<i>FOS 06,</i> FOS 14	25.0"
SP-09	FIU-30-001	FOS-P1-1E FOS-P1-1W	16.0" 13.0"
	FIU-30-002	FOS-P1-2E FOS-P1-2W	n/a 14.0"
SP-10	FIU-30-003	FOS-P2-1E FOS-P2-1W	17.0" 13.0"
	FIU-30-004	FOS-P2-2E FOS-P2-2W	15.0" 14.0"

Table 5.17: Measured transfer lengths for 18-inch and 30-inch piles

The average measured transfer length was 25.86 inches for the 18-inch piles and 14.57 inches for the 30-inch piles. The estimated transfer length for both piles is 31.2 inches based on AASHTO LRFD BDS [3].

5.9.4 Prestress Losses

5.9.4.1 Prestress Loss Estimates

Prestress losses estimates were found using AASHTO LRFD Bridge Design Specification (§5.9.3) [3].

In pretensioned members:
AASHTO 5.9.3.1-1
$$\Delta f_{pT} = \Delta f_{pES} + \Delta f_{pLT}$$
 Equation 5.18

where:

 $\Delta f_{pT} = \text{total loss (ksi)}$

 Δf_{pES} = sum of all losses or gain due to elastic shortening or extension at the time of application of prestress and or external loads (ksi)

$$\Delta f_{pLT}$$
 = losses due to long-term shrinkage and creep of concrete, and relaxation of the steel (ksi)

Loss due to elastic shortening in pretensioned members was estimated using Equation 5.7.

AASHTO LRFD
(C5.9.3.2.3a-1)
$$\Delta f_{pES} = \frac{A_{ps}f_{pbt}(I_g + e_m^2 A_g) - e_m M_g A_g}{A_{ps}(I_g + e_m^2 A_g) + \frac{A_g I_g E_{ci}}{E_p}}$$
Equation 5.19

The long-term prestress loss, Δf_{pLT} , due to creep of concrete, shrinkage of concrete, and relaxation of steel should be found using the approximate estimate equation, shown in Equation 5.8.

AASHTO 5.9.3.3-1
$$\Delta f_{pLT} = 10.0 \frac{f_{pi}A_{ps}}{A_g} \gamma_h \gamma_{st} + 12.0 \gamma_h \gamma_{st} + \Delta f_{pR}$$
 Equation 5.20

In which:

AASHTO 5.9.3.3-2
$$\gamma_h = 1.7 - 0.01H$$
 Equation 5.21

AASHTO 5.9.3.3-3
$$\gamma_{st} = \frac{5}{(1 + f'_{ci})}$$
 Equation 5.22

where:

 f_{pi} = prestressing steel immediately prior to transfer (ksi)

- H = average annual ambient relative humidity (percent)
- y_h = correction factor for relative humidity of the ambient air
- y_{st} = correction factor for specified concrete strength at time of prestress transfer to the concrete member

 f_{pR} = an estimate of relaxation loss taken as 2.4 ksi for low relaxation strand and in accordance with the manufacturers recommendations for other types of strands (ksi)

Estimated losses for the piles are shown in Table 5.18.

Pile Size	Elastic Shortening Loss (ksi)	Long-Term Prestress Loss (ksi)	Total Prestress Losses (ksi)	Effective Stress after all Losses (ksi)
18-inch	7.4	18.8	26.2	177.4
30-inch	5.4	16.4	21.8	181.8

Table 5.18: Estimated prestress losses and effective stress in strands for 18-inch and 30-inch piles

5.9.4.2 Measured Losses and Effective Stress in Strands

Elastic shortening and long-term losses were found using two vibrating wire strain gauges (VWSG) located in the piles in the longitudinal direction. The standard temperature correction was applied to the data to account for different coefficients of thermal expansion between concrete and the steel wire located in the VWSG, shown in Equation 5.11.

$$\varepsilon_{\Delta} = (R_1 - R_0)B + (T_1 - T_0)(C_1 - C_2)$$
 Equation 5.23

where:

 ε_{Δ} = measured change in strain

 R_0 = initial reading

 R_1 = current reading

B = batch gauge factor (input in VWSG reader or DAQ)

 T_0 = initial temperature

 T_1 = current temperature

 C_1 = coefficient of expansion of steel: 12.2 µε/°C

 C_2 = coefficient of expansion of concrete: assumed to be 10 $\mu\epsilon/^{\circ}C$

A summary of the measured losses is shown in Table 5.19. No readings were taken for SP-04, SP-05, and SP-10. SP-04 did not have any VWSG installed in the piles, due to one of the instrumented piles being installed in the wrong cap. The VWSGs installed in SP-05 and SP-10 did not appear to be working correctly and returned unreliable data. Strain measurements for the elastic shortening losses were taken before and after pile detensioning. The elastic shortening loss was recorded as the average readings of the two vibrating wire gauges. The average prestress losses due to elastic shortening was 7.2 ksi for the 18-inch piles and 5.9 for the 30-inch piles, which were within 2.2% and 8.6% of the estimated elastic shortening losses, respectively.

Long-term losses were measured by taking the difference in strain readings taken after release and immediately before testing. The average long-term loss measured for the 18-inch piles was 16.2 ksi (within 13.9% of estimated loss) and 9.8 ksi for the 30-inch piles (40.1% less than estimate).

	Strain	Readings		Elastic	Shortenin g		Long	Term	
SP	Before Release (με)	After Release (με)	Before Testing (με)	Strain Change (με)	ES Losses (ksi)	<i>∆f_{pES}</i> (ksi)	Strain Chan ge (με)	LT Losses (ksi)	∆f _{pLT} (ksi)
SP-1	0	-352.1	-900.1	352.1	10.04	9.66	547.9	15.62	15.34
	0	-325.5	-854.3	325.5	9.28		528.8	15.07	
SP-2	0	-352.5	-1153.4	352.5	10.05	10.0	800.9	22.83	22.83
	0	-349.4		349.4	9.96				
SP-3	0	-316.7	-835.4	316.7	9.03	9.02	518.8	14.78	15.57
	0	-316.1	-889.8	316.1	9.01		573.8	16.35	
SP-6	0	-323.1	-822.1	323.1	9.21	9.28	499.0	14.22	14.36
	0	-328.0	-836.9	328.0	9.35		508.9	14.50	
SP-7	0	-358.6	-793.7	358.6	10.22	9.81	435.1	12.40	12.84
	0	-330.0	-795.7	330.0	9.40		465.8	13.27	
SP-8	0	-366.6	-944.8	366.6	10.45	10.08	578.2	16.48	16.17
	0	-340.5	-897.2	340.5	9.70		556.8	15.87	
SP-9						5.88			9.85
	0	-206.3	-552.0	206.3	5.88		345.7	9.85	
SP- 10	0	-210.1		210.1	5.99	5.99			

Table 5.19: Measured elastic shortening and long-term losses using VWSG.

The measured total losses and effective stress in strands are summarized in Table 5.20.

Specimen	f_{pT} (ksi)	f _{pe} (ksi)
SP-01	25.0	178.6
SP-02	32.8	170.8
SP-03	24.6	179.0
SP-06	23.6	180.0
SP-07	22.6	180.9
SP-08	26.3	177.3
SP-09	15.7	187.9

Table 5.20: Summary of measured total losses and effective stress in strands.

5.9.5 Ultimate Strength Testing Results

Ultimate strength testing was performed at the FDOT SRC. The application of the lateral load was initially located at 12 ft. from the pile-to-cap interface. The lever arm, shown in Figure 5.48, was reduced for future tests due to not having sufficient stroke in the hydraulic jack for the 12-ft. lever arm.



Figure 5.48: Location of applied lateral load.

The test date and lever arm used for testing for each specimen are shown in Table 5.21. The 18inch pile specimens without axial load were tested first, followed by the 18-inch pile specimens with axial load, and finally the 30-inch pile specimens.

Specimen	Testing day	Lever arm (ft)	Reason for Stopping Test
SP-01	4/18/2022	12	Ran out of stroke on jack, load was maintaining
SP-02	8/4/2022	6	Ran out of stroke on jack, load was maintaining
SP-03	4/22/2022	9	Load dropping at end of test, ran out of stroke on jack
SP-04	5/9/2022	9	Ran out of stroke on jack, load was maintaining
SP-05	8/1/2022	6	Ran out of stroke on jack, load was maintaining
SP-06	5/12/2022	9	Ran out of stroke on jack, load was maintaining
SP-07	5/31/2022	6	Ran out of stroke on jack, load was maintaining
SP-08	6/3/2022	6	Ran out of stroke on jack, load was maintaining
SP-09	12/20/2022	9	Dropping in capacity, damage to pile
SP-10	4/3/2023	9	Damage to cap

Table 5.21: Test date and lever arm

A summary of the ultimate strength testing results is presented in Table 5.22. These results are analyzed in more detail in the following sections.

Specimen	Pile Size	Cracking Load (kips)	Failure Load (kips)	Failure Mechanism	Failed Pile	Moment developed (kip-ft)	Percentage of capacity of pile
SP-01	18"	6	9.5	Strand Development	West	114.1	34.5%
SP-02	18"	10	40.8	Strand Development	West	244.6	73.9%
SP-03	18"	8	21.2	Strand Development	West	190.8	57.6%
SP-04	18"	9.5	13.6	Strand Development	West	122.8	37.1%
SP-05	18"	20	41.0	Strand Development	West	246.2	74.4%
SP-06	18"	10	17.7	Strand Development	East	159.4	48.2%
SP-07	18"	20	33.6	Strand Development	West	201.4	60.8%
SP-08	18"	30	44.6	Strand Development	West	267.6	80.8%

 Table 5.22: Summary of ultimate strength testing

Specimen	Pile Size	Cracking Load (kips)	Failure Load (kips)	Failure Mechanism	Failed Pile	Moment developed (kip-ft)	Percentage of capacity of pile
SP-09	30"	32	63.8	Strand Development	West	574.6	48.3%
SP-10	30"	90	96.4	Punching Shear	West	868.1	73.0%

Table 5.22: Summary of ultimate strength testing -Continued

5.10 ANALYSIS OF RESULTS

5.10.1 Observed Failure Mechanism

All specimens experienced a ductile failure mechanism, where there was significant deflection after the maximum load was reached, as shown in Figure 5.49. All 18-inch pile specimens held close to the ultimate capacity while additional deflection was observed. The 30-inch pile specimens experienced a drop in capacity immediately after the ultimate load was reached.

Based on the literature review, three different mechanisms were expected to control the moment capacity of the connection: (1) slip of prestressing strands in embedded pile, (2) slip between pile and pile cap, and (3) bearing failure between pile and pile cap, shown in Figure 5.50.

A strand development failure was observed in the 18-inch specimens and the shallower 30-inch embedment. A punching shear failure was observed in the deeper embedment of the 30-inch specimens.



Figure 5.49: Moment versus displacement curves for: (a) 18-inch; (b) 30-inch pile specimens.



Figure 5.50: Expected failure mechanisms of the pile-to-cap connection: (a) development length of prestressing strand; (b) shear friction capacity between the pile and pile cap; (c) bearing between the pile and cap.

5.10.1.1 Strand Development Failure

A strand development failure is defined as the inability of the pile to develop its full moment capacity at the pile-to-cap interface due to insufficient available development length for the prestressing strand to develop its full stress at ultimate (f_{ps}). For pile-to-cap connections, the available development length corresponds to the pile embedment length. This type of failure is a ductile failure where the section will maintain some capacity as the strand slips. It is typically assumed that the strand slip will be accompanied by a drop in capacity when the slip initiates, but this is not always the case. This type of failure would result in a large crack at the location where the strands begin to slip.

This type of failure was observed in all the 18-inch specimens with a crack in the pile at the pileto-cap interface, as shown in Figure 5.51 (a). The moment versus deflection curves, shown in Figure 5.49, all are what would be expected for a strand development failure with the specimens holding load as the strand slip is occurring. In the case of SP-03, which included interface reinforcement between the pile and pile cap, the strand development failure was observed at the end of the interface reinforcement in the pile, as shown in Figure 5.51 (b).



Figure 5.51: Photographs after failure for: (a) SP-04; (b) SP-03 with observed strand development failure.

A strand development failure was also observed in SP-09, as shown in Figure 5.52. Failure occurred in two stages: development of a crack in the pile at the pile-to-cap interface followed by a second larger crack developing in the pile about 3 inches inside the pile cap. After testing was completed, the spalled concrete in the pile cap around the west pile was removed to inspect the damage inside the embedded pile, as shown in Figure 5.52 (b). A second pile crack was found inside the cap. The strands were in good condition but slipping of the strand was visually observed.



Figure 5.52: SP-09 strand development failure: (a) SP-09 failure; (b) after removing spalled concrete in the cap.

After cracking in the pile occurred, the pile started to slip out of the cap as the second larger crack in the pile grew, as shown in Figure 5.53 (a). Diagonal cracking was observed in the cap extending from the corners of the pile, as shown in Figure 5.53 (b). This cracking is commonly observed with punching shear failures.



(a)

(b)

Figure 5.53: SP-09 failure: (a) pile slipping out of pile cap; (b) damage in pile cap.

5.10.1.2 Punching Shear Failure in the Pile Cap

A punching shear failure of the edge of the pile cap adjacent to the embedded pile was observed in SP-10. There were no significant cracks in the pile at the pile-to-cap interface, as shown in Figure 5.54 (a). Wide shear cracks in the shape of a punching shear cone were observed at the west side of the pile cap, as shown in Figure 5.54 (b). The east side of the embedded pile pulled away from the pile cap as it punched out the west side of the cap. The cracks initiated at the corners of the pile, with an inclination angle of approximately 45 degrees, and then propagated towards the top of the pile cap, as shown in Figure 5.54 (b).



(a)

(b)

Figure 5.54: SP-10 failure: (a) pile slipping out of pile cap; (b) punching shear failure.

The N5 bars located toward the west side of the pile cap (strains measured by RSG-01 and RSG-02) began to be engaged at around 96 kips as the side of the cap punched out, as shown in Figure 5.55. The maximum measured strain in RSG-01 was 1,408 μ e when the load was removed.



Figure 5.55: SP-10 rebar strain data for N5 bars.

Minor punching shear cracking was also observed in 18-inch pile specimens with pile embedment lengths of 12 inches and greater; two examples are shown in Figure 5.56 (a) and (b). Punching shear cracks were also observed in the 30-inch pile specimen with 12-inch pile embedment, shown in Figure 5.56 (c).



Figure 5.56: Punching shear cracking observed in: (a) SP-06; (b) SP-08; (c) SP-09.

The measured rebar strain in the reinforcement in these pile caps (SP-06, SP-08, and SP-09) between the embedded pile and edge of the pile cap was significantly less than the measured strains in SP-10, see Figure 5.57 and Figure 5.58.



Figure 5.57: Load versus rebar strain for pile cap reinforcement around the west embedded pile for: (a) SP-06; (b) SP-08.



Figure 5.58: Load versus rebar strain for pile cap reinforcement around the west embedded pile for SP-09.

5.10.1.3 Rigid Body Rotation

A hinge typically developed in the pile at the large crack near the pile-to-cap interface with rigidbody rotation of the pile occurring after the strands began to slip. The hinge was accompanied by a large crack on the tension face of the pile and spalling of the concrete on the compression face, highlighted in Figure 5.59.



Figure 5.59: Assumed rigid body rotation of pile during testing with typical damage at failure highlighted.

Photographs of some of the large cracks on the tension face are shown above in Figure 5.51 through Figure 5.53. Photographs of examples of spalling of the concrete on the compression face of the pile are shown in Figure 5.60.



Figure 5.60: Examples of spalling of concrete on compression face of pile for: (a) SP-04; (b) SP-05; SP-08 during failure.

The rigid body rotation of the pile was verified through observation of the laser displacement transducers (LDTs) along the length of the pile. The displacement versus distance from cap plots for SP-01 and SP-4 are shown in Figure 5.61.



Figure 5.61: Sample displacement versus distance from cap for: (a) SP-01; (b) SP-04.

The rotation capacity and moment versus rotation diagrams can be determined using this assumption, as shown in Figure 5.59 and Equation 5.12.

$$\theta = \tan^{-1} \frac{\Delta_{load}}{L_{load}}$$
 Equation 5.24

A summary of all the moment versus rotation curves for the specimens is shown in Figure 5.62.



Figure 5.62: Moment versus rotation responses for: (a) 18-inch; (b) 30-inch pile specimens.

5.10.2 Moment Capacity and Pile Embedment Length

The primary variable studied in the experimental program was the embedment length. For the 18inch and 30-inch specimens, embedment lengths between 0.33 and 1.5 times the diameter of the piles were tested. A summary of the service moment, total moment developed and the percentage of the pile capacity for specimens without axial load or interface reinforcement is shown in Table 5.23. The observed failure mechanism for each specimen is also included in Table 5.23. All specimens except SP-10 failed due to slipping of the prestressing strands (strand development). SP-10 failed due to a punching shear failure of the edge of the pile cap adjacent to the embedded pile.

With respect to capacity, the 18-inch pile specimens with $0.33d_p$ (6-inch) and $0.5d_p$ (9-inch) embedment (SP-01 and SP-04) still developed 34% and 37% of the as-built pile capacity, respectively.

The two specimens (SP-06 and SP-09) with the current FDOT-specified embedment length for pinned connections (12-inches) each developed 48% of their respective pile capacity. These specimens had two different pile sizes (SP-06 had 18-inch piles, and SP-09 had 30-inch piles), so the capacity did not correspond to the relationship between pile size and pile embedment. Both specimens had the same strand type (0.5-inch special strands), which suggests that the capacity of the connection is more dependent on the available development length of the strand.

The 18-inch pile specimens with the deepest pile embedment (SP-08 with 27-inch embedment) developed 81% of the pile capacity while the 30-inch pile specimen with 30-inch embedment (SP-10) developed only 73% of the pile capacity. The smaller capacity developed by SP-10 was likely due to punching shear of the edge of the pile cap occurring before the slipping of the strands occurred. Different failure modes were also observed between these two specimens: SP-08 with a strand development failure and SP-10 with a punching shear failure. The different concrete strengths between the pile and the pile cap in SP-10, as shown in Table 5.16, reflected a field condition between the precast piles and the cast-in-place pile caps, which likely contributed to the punching shear failure.

During the test, the load at first cracking was recorded, the corresponding moment at first cracking was calculated, and the percentage of the moment at first cracking to the pile capacity was calculated. The service moment limit for each specimen is shown in Table 5.23.

Specimen	Pile Size	Embedment	Service Moment (kip-ft)	Failure Moment (kip-ft)	Percentage of Pile Capacity	Failure Mechanism
SP 01	18"	6"(0.33d)	72.00	11/11	3/10/2	Strand
51-01	10	$0 (0.55 a_p)$	72.00	114.1	5470	Development
SD 04	18"	" 0" (0 50 <i>d</i>)	85 50	122.8	37%	Strand
51-04	10	$9 (0.30 u_p)$	85.50	122.0		Development
SD 06	10"	12"(0.673)	00.00	150 /	100/	Strand
51-00	10	$12 (0.07a_p)$	90.00	139.4	4070	Development
SD 07 1	10"	$18"(1.00d_p)$	120.00	201.4	61%	Strand
Sr-0/	10					Development

 Table 5.23: Summary of failure moments and failure mechanisms for specimens with different embedment lengths

Specimen	Pile Size	Embedment	Service Moment (kip-ft)	Failure Moment (kip-ft)	Percentage of Pile Capacity	Failure Mechanism
SP-08	18"	27" $(1.50d_p)$	180.00	267.6	81%	Strand Development
SP-09	30"	$12"(0.40d_p)$	288.00	574.5	48%	Strand Development
SP-10	30"	$30"(1.00d_p)$	810.00	868.1	73%	Punching Shear

 Table 5.23: Summary of failure moments and failure mechanisms for specimens with different embedment lengths - Continued

The moment versus displacement curves for the five different pile embedment lengths for the 18inch pile specimens are shown in Figure 5.63.



Figure 5.63: Moment-displacement curves for the 18-inch specimens.

The moment versus curvature responses is provided for three of the specimens with different embedment lengths in Figure 5.64. These responses were determined using the fiber optic sensors (FOS) embedded in the specimens by assuming a linear strain profile between the FOS on the east and west sides of the pile that failed during testing. Maximum measured strains around interface were used to calculate curvature. The FOS sensors debonded from the GFRP at a measured strain of approximately 10,000 $\mu\epsilon$. All 18-inch pile specimens failed due to a strand development failure, which led to a large crack developing near the interface. The FOS stopped reading correct strains at the large crack at strains greater than about 10,000 $\mu\epsilon$. This affected ability to find a moment versus curvature response for the other specimens.



Figure 5.64: Moment versus curvature response for 18-inch specimens.

All specimens that failed due to strand development had one large crack develop at the base of the pile at or near the pile-to-cap interface. Only two of the 18-inch specimens (without interface reinforcement or axial load) had additional flexural cracks develop along the length of the pile, shown in Figure 5.65.



Figure 5.65: Flexural cracks in piles after testing for: (a) SP-07; (b) SP-08.

A brief comparison of some strains measured by RSGs and CSGs for the shallowest 18-inch pile embedment (6 inches for SP-01) and the deepest (27 inches for SP-08) is provided in Figure 5.66 through Figure 5.70. The scale in these figures is different between SP-01 and SP-08 since there were different failure loads and typically significantly different measured strains.

Although both SP-01 and SP-08 failed due to strand development, more cracking and larger concrete strains were observed in the pile cap in SP-08 compared to SP-01. The load versus concrete strain in the face of the pile cap with the embedded pile toward the edge of the cap is

shown in Figure 5.66. Strains in the exterior edge of the pile reached 885 $\mu\epsilon$ tension in SP-08 near failure compared with less than 40 $\mu\epsilon$ tension in SP-01.



Figure 5.66: Load versus concrete strain on the edge of the pile cap for: (a) SP-01; (b) SP-08 (axes have different scales).

Larger concrete strains were also measured on the side face of the pile caps in SP-08 compared with SP-01, as shown in Figure 5.67. Tensile strains developed at mid-width of the pile cap with compression strains developing toward the edges of the pile cap. Concrete strains in SP-08 reached -320 $\mu\epsilon$ compression and 90 $\mu\epsilon$ tension compared with less than -5 $\mu\epsilon$ compression and less than 20 $\mu\epsilon$ tension for SP-01.



Figure 5.67: Load versus concrete strain on the side face of the pile cap for: (a) SP-01; (b) SP-08 (axes have different scales).

The reinforcement parallel to the edge of the cap was not heavily engaged in either SP-01 or SP-08 with strains less than 60 μ for each, as shown in Figure 5.68.



Figure 5.68: Load versus rebar strain for pile cap reinforcement around the embedded piles for: (a) SP-01; (b) SP-08.

There were larger measured strains in the longitudinal reinforcement extending along the length of the pile caps in SP-08 than SP-01, as shown in Figure 5.69. Longitudinal rebar strains in SP-01 were less than around 50 μ e, while strains in SP-08 reached 491 μ e.



Figure 5.69: Load versus rebar strain for pile cap reinforcement around the embedded piles for: (a) SP-01; (b) SP-08.

The load versus rebar strain for the reinforcement spaced across the west face of the pile cap for SP-01 and SP-08 are shown in Figure 5.70. The rebar strains are generally higher for SP-08 than SP-01.



Figure 5.70: Load versus rebar strain for reinforcement along the west face of the pile cap for: (a) SP-01; (b) SP-08.

The largest measured strain in SP-08 were measured toward the face of the pile cap opposite the pile embedment, as shown in Figure 5.71. It is unclear why the strain in RSG-30 was the largest in this specimen. Strains were generally the largest in reinforcement closest to the pile cap face with the embedded piles, as was the case for SP-01 in Figure 5.70 (a).



Figure 5.71: Maximum strains in reinforcement in west face of the pile cap for SP-08.

5.10.2.1 Development Length and Confining Stress

The observed failure mechanism for nine of the test specimens was strand development. Different estimation procedures for development length and to account for the confinement provided by the shrinkage of the cap concrete are discussed in this section.

- Estimated Development Length

Estimated transfer and development lengths were found using AASHTO LRFD Bridge Design Specification (BDS) §5.9.4.3.2 [3]. The transfer and development lengths are found using Equation 5.14 and Equation 5.13, respectively.

Required transfer length: AASHTO LRFD §5.9.4.3.1	$l_t = 60d_b$	Equation 5.25
Required development length: AASHTO LRFD (5.9.4.3.2-1)	$l_{d} \geq \kappa \left(f_{ps} - \frac{2}{3} f_{pe} \right) d_{b}$	Equation 5.26

where:

 d_p = nominal strand diameter (in)

- f_{ps} = average stress in prestressing steel at the time for which the nominal resistance of the member is required (ksi)
- f_{pe} = effective stress in the prestressing steel after losses (ksi)
- κ = 1.0 for pretensioned panels, piling, and other pretensioned members with a depth of less than or equal to 24.0 in
- κ = 1.6 for pretensioned members with a depth greater than 24.0 in

The stress in the prestressing steel at nominal moment (f_{ps}) is found from AASHTO LRFD BDS §5.6.3.1.

AASHTO LRFD (5.6.3.1.1-1)
$$f_{ps} = f_{pu} \left(1 - k \frac{c}{d_p} \right)$$
 Equation 5.27

AASHTO LRFD (5.6.3.1.1-2)
$$k = 2\left(1.04 - \frac{f_{py}}{f_{pu}}\right)$$
Equation 5.28

AASHTO LRFD (5.6.3.1.1-4)
$$c = \frac{A_{ps}f_{pu} + A_{s}f_{s} - A'_{s}f'_{s}}{\alpha_{1}f'_{c}\beta_{1}b + kA_{ps}\frac{f_{pu}}{d_{p}}}$$
Equation 5.29

where:

- A_{ps} = area of prestressing steel (in²)
- f_{pu} = specified tensile strength of prestressing steel (ksi)
- f_{py} = yield strength of prestressing steel (ksi)
- A_s = area of nonprestressed tension reinforcement (in²)
- A'_{s} = area of compression reinforcement (in²)
- f_s = stress in the nonprestressed tension reinforcement at nominal flexural resistance (ksi)
- f'_s = stress in nonprestressed compression reinforcement at nominal flexural resistance (ksi)
- b = width of the compression face of the member (in)
- d_p = distance from extreme compression fiber to the centroid of the prestressing force (in)
- c = distance from the extreme compression fiber to the neutral axis (in)
- α_1 = stress block factor

 β_1 = stress block factor

The rectangular stress distribution factors (β_1 and α_1) can be found in AASHTO LRFD BDS §5.6.2.2.

For
$$f'_c \le 10$$
 ksi: $\alpha_1 = 0.85$ Equation 5.30For $f'_c > 10$ ksi: $\alpha_1 = 0.85 - 0.02(f'_c - 10 \text{ ksi}) \ge 0.75$ Equation 5.31

The other stress block factor is also based on the compressive strength of concrete.

For
$$f'_c \le 4$$
 ksi: $\beta_1 = 0.85$ Equation 5.32For $f'_c > 4$ ksi: $\beta_1 = 0.85 - 0.05(f'_c - 4 ksi) \ge 0.65$ Equation 5.33

The losses found in §5.9.4 were used to find the effective stress in the prestressing (f_{pe}). Some of the significant values in the transfer length and development length calculations are summarized in Table 5.24 for the 0.5-in special strands in the 18-inch and 30-inch piles.

 Table 5.24: Estimated transfer and development length for 18-inch and 30-inch piles using AASHTO

 LRFD BDS

Pile	d _b (in)	fpe (ksi)	Transfer length, <i>l_t</i> (in)	<i>c</i> (in)	f _{ps} (ksi)	к	Development length, <i>l_d</i> (in)
18-inch	0.52	177.4	31.2	2.30	256.9	1.0	72.1
30-inch	0.52	181.8	31.2	2.56	261.8	1.6	117.0

The average transfer length measured using the fiber optic sensors for the 18-inch and 30-inch piles was 25.86 and 14.57 inches, respectively.

A bilinear relationship is assumed in AASHTO LRFD BDS for determining the stress in the strands when the available development length is less than the required development length. The stress in the prestressing strand varies linearly from 0 ksi at the point where bonding starts to the effective stress after losses, f_{pe} , at the end of the transfer length, l_t . Between the end of the transfer length and the development length, l_d , the strand stress is assumed to increase linearly, reaching the stress at nominal resistance, f_{ps} , at the development length. The idealized relationship between steel stress and distance from the free end of strand per AASHTO LRFD BDS is shown in Figure 5.72.



Figure 5.72: Idealized relationship between strand stress and distance from free end of strand [3].

The stress versus available development length plots found using AASHTO LRFD BDS for the 18-inch and 30-inch piles are shown in Figure 5.73.



Figure 5.73: Estimated strand stress versus development length for 18-inch and 30-inch piles found using AASHTO LRFD BDS equations.

- Background on Transfer and Development Length Equations

In 1973, AASHTO adopted the transfer and development length equation from the ACI Building Code, which was proposed by Mattock and members of ACI Committee 423 [4], [63]. The development length equation in ACI 318-19 [64], shown in Equation 5.22, divides the development length into two parts: transfer length and flexural bond length. Mattock [63] developed this equation based on results of a study conducted by Hanson and Kaar [65], where tests were conducted on specimens not subject to confining stresses.

Required development length:
ACI 318-19 (25.4.8.1)
$$l_d = \left(\frac{f_{se}}{3000}\right)d_b + \left(\frac{f_{ps} - f_{se}}{1000}\right)d_b$$
 Equation 5.34

where:

 f_{se} = effective prestress in the prestressing steel (ksi) f_{ps} = stress in the prestressing steel at the nominal strength of the member (ksi)

The average transfer bond stress, \bar{u}_t =400 psi, was stated in the study by Hanson and Kaar [65] and adopted by Mattock [63]. For the average flexural bond stress, Mattock [63] constructed a straightline relationship by subtracting the estimated transfer length from the embedment length of the strand. The increase in strand stress due to flexure was determined to be the difference between the strand stress at the load causing slip and the effective stress due to prestressing. An average flexural bond stress of \bar{u}_{fb} =140 psi was used. The expressions created for transfer length and flexural bond length by Mattock are shown in Equation 5.23 and Equation 5.24, respectively.

Transfer length (Mattock)
$$L_t = \frac{A_{ps}f_{se}}{\sum o \bar{u}_t} = \frac{f_{se}}{7.36\bar{u}_t}d_b = \frac{f_{se}}{3000}d_b$$
Equation 5.35Flexural bond length (Mattock) $L_{fb} = \frac{f_{ps}-f_{se}}{7.36\bar{u}_{fb}}d_b = \frac{f_{ps}-f_{se}}{1000}d_b$ Equation 5.36

Where:

 $\sum o$ = perimeter of the strand (in) = $4/3\pi d_b$

$$A_{\rm ps}$$
 = cross-sectional area of the strand (in2) = 0.725 $\pi d_b^2/4$.

Based on a study conducted by Cousins et al. [66] questioning the development length of prestressing strands, the Federal Highway Administration [67] later added the application of 1.6 multiplier for pretensioned members with a depth greater than 24.0 inches.

The calibration of the ACI 318-19 and AASHTO LRFD BDS development length equations did not include specimens with confining stresses on the strands during testing, which would likely help to reduce the required development length of the strands.

Effect of Cap Confinement on Transfer and Development Length

As summarized in the literature review, many researchers have found that the full moment capacity of the piles can be developed with much shorter embedment lengths than required by AASHTO LRFD BDS to fully develop the strands. This suggests that the actual required strand development length for the pile embedded in a footing or cap is significantly shorter than the development length calculated using AASHTO LRFD BDS. It has been proposed by previous researchers [4] that the primary reason for this is the shrinkage of the cast-in-place footing or cap creating a clamping force around the embedded pile and decreasing the required development length. This compressive stress affects both the average transfer bond stress and the average flexural bond stress, which will decrease the development length required for the full capacity of the prestressing strand.

Three different mechanisms are typically assumed to contribute to the transfer bond stress: adhesion, friction, and mechanical interlock. Friction, which has the most significant effect, results from the slipping of the strand along the transfer length. For the development of frictional bond stresses, radial compressive stresses are required. Hoyer's effect and confining stress contributes to this radial compressive stress, affecting the frictional bond stress directly. The confined transfer bond stress can be found by adding the average bond stress and the average confining stress multiply by the friction coefficient between steel and concrete, as shown in Equation 5.25.

Confined transfer bond stress:
$$\bar{u}_{tc} = 400 + \mu \sigma_{cav}$$
 Equation 5.37

where:

 σ_{cav} = average confining stress (psi)

= coefficient of friction between steel and concrete μ

For the confined flexural bond stress, it was assumed that the confining stress will only affect the friction stress. The cracks that form in the flexural bond stress zone will decrease the friction forces that result from the confining stress. A ratio of $(\bar{u}_t/\bar{u}_{fb}) = 2.86$ has been used by previous researchers [4] to decrease the effect of the confining stress, as shown in Equation 5.26.

Confined flexural bond stress:
$$\bar{u}_{fbc} = 140 + \frac{\mu \sigma_{cav}}{2.86}$$
 Equation 5.38

where:

 σ_{cav} = average confining stress (psi) μ = coefficient of friction between steel and concrete

ElBatanouny and Ziehl [4] assume that confining stress is dependent on several variables, including pile stiffness, pile cap stiffness, dimensions of the pile/pile cap system, time between casting of pile and casting of pile cap, and time between casting of the pile cap and loading of specimen. They developed an equation for the estimation of the confining stress for purposes of design. The equation uses Lames equations for the calculation of stresses in thick-walled cylinders. The confining stress can be calculated using Equation 5.27.

Confining stress [4]:
$$\sigma_{c} = \frac{(D_{o})\left(\varepsilon_{sh} - \frac{(d_{o})(\sigma_{c})}{E_{p}}\right)(1 - v_{p})}{\left(\frac{d_{o}}{E_{BC}}\right)\left(\frac{D_{o}^{2} + d_{o}^{2}}{D_{o}^{2} - d_{o}^{2}} + v_{BC}\right) + \frac{d_{o}}{E_{p}}(1 - v_{p})}$$
Equation 5.39
Shrinkage strain by ACI
209R-92
$$\varepsilon_{sh} = \frac{t}{35 + t}(\varepsilon_{sh})_{u}$$
Equation 5.40

209R-92

where:

 σ_c = confining stress (psi)

 d_o = smallest dimension of pile (in)

 D_o = smallest dimension of pile cap

 ε_{sh} = shrinkage strain (in/in)

 E_p = young's modulus of pile (psi)

 v_p = poisson's ratio of the pile (0.2 for concrete)

 E_{BC} = young's modulus of pile cap (psi)

 V_{BC} = poisson's ratio of the pile cap (0.2 for concrete)

t = time between casting of the bent cap and loading of the specimen (days)

 $(\varepsilon_{sh})_{u}$ ultimate shrinkage strain (780x10⁻⁶ in/in)

This procedure was used to find the estimated confining stresses for each of the specimens, as shown in Table 5.25.

SP	D _o (in)	d _o (in)	E_p (psi)	E _{BC} (psi)	t (days)	€ _{sh} (in/in)	σ_c (psi)
SP-01	36	18	6,218,954	6,368,371	236	0.00068	2468.8
SP-02	36	18	6,099,600	6,337,558	350	0.00071	2547.0
SP-03	36	18	6,133,880	6,422,958	239	0.00068	2467.9
SP-04	36	18	6,218,954	6,225,256	255	0.00069	2462.5
SP-05	36	18	6,250,491	6,564,529	336	0.00071	2615.0
SP-06	36	18	6,133,880	6,085,758	253	0.00069	2414.9
SP-07	36	18	6,133,880	5,790,249	231	0.00068	2323.3
SP-08	36	18	6,133,880	6,390,533	232	0.00068	2451.9
SP-09	48	30	6,532,276	5,516,098	30	0.00036	834.2
SP-10	48	30	6,701,350	5,393,539	21	0.00030	676.6

Table 5.25: Estimated confining stress found using ElBatanouny and Ziehl [4]

ElBatanouny and Ziehl [4] and other researchers have developed equations to calculate the development length of the strands considering these confining stresses or clamping forces provided by the pile cap. ElBatanouny and Ziehl [4] modified the ACI development length equation (Equation 5.22) by replacing the values of \bar{u}_t and \bar{u}_{fb} , with \bar{u}_{tc} and \bar{u}_{fb} , respectively, in Equation 5.23 and Equation 5.24. This will increase the values of the average bond stress and average flexural bond stress which will lead to a decrease in the development length, as shown in Equation 5.29.

ElBatanouny [4]:
$$L_{dc} = \frac{f_{se}}{5000} * d_b + \frac{f_{ps} - f_{se}}{1800} * d_b$$
 Equation 5.41

where,

 L_{dc} = confined development length (in)

 f_{se} = effective stress of prestressing strand (psi)

 f_{ps} = nominal strength of prestressing strand (psi)

 d_b = nominal diameter of prestressing strand (in)

The transfer and development length for the 18- and 30-inch piles were found using Equation 5.29. Results are shown in Table 5.26.

Table 5.26: Estimated development length for 18-inch and 30-inch piles using ElBatanouny and Zieh	l [4]
---	-------

Pile Size	d _b (in)	fpe (ksi)	<i>f_{ps}</i> (ksi)	Development length, <i>l_d</i> (in)
18-inch	0.52	177.4	256.9	41.4
30-inch	0.52	181.8	261.8	42.0
This estimated development length is much less than the estimated development length found using AASHTO LRFD BDS, 72.1 in for 18-inch piles and 117.0 in for 30-inch piles.

An additional proposal from FDOT to AASHTO T-10 in 1993, summarized in Buckner [68], had a similar form to the recommendation from ElBatanouny and Ziehl [4], shown in Equation 5.30.

FDOT 1993 [68]:
$$L_d = \frac{\left[\frac{f_{pe}d_b}{3} + (f_{ps} - f_{pe})\right]}{k_b \mu_{ave}}$$
 Equation 5.42

where:

- k_b = dimensionless constant; 8 for piles embedded in concrete footing or pier cap, 4 for slabs and slender members, and 2 if the computed development length to member depth ratio is less than or equal to 3
- μ_{ave} = average bond stress for development length, 0.25 ksi

The transfer length would be implied to be Equation 5.31.

Implied from FDOT
1993 [68]:
$$L_t = \frac{f_{pe}d_b}{3k_b\mu_{ave}}$$
 Equation 5.43

Buckner [68] comments that Equation 5.30 results in about the same development length as the 1993 AASHTO equation for slender member, results in development lengths doubling for deep members, and results in half the development length for embedded piles.

 Table 5.27: Estimated transfer and development length for 18-inch and 30-inch piles using FDOT 1993

 from Buckner [68]

Pile Size	d _b (in)	f _{pe} (ksi)	<i>f_{ps}</i> (ksi)	Transfer length, <i>l_d</i> (in)	Development length, <i>l_d</i> (in)
18-inch	0.52	177.4	256.9	15.4	55.1
30-inch	0.52	181.8	261.8	15.8	55.8

- Measured Confining Stresses

The average confining stress was calculated for each specimen using the readings from the vibrating wire gauges in the pile cap after casting and before testing. The measured strains were multiplied by the estimated modulus of elasticity of the cap concrete to find the confining stresses; this is like what was done by previous researchers [20]. Results for several specimens are shown in Table 5.28. Accurate readings were not obtained for the other specimens.

Specimen	Age of Cap (days)	VWG-4 (με)	VWG-6 (με)	Average Strain (με)	<i>E_{PC}</i> (ksi)	σ _c (ksi)
SP-01	240	-72.8	-131.8	-102.3	6,368	-0.652
SP-03	240	-1.9	-72.6	-37.2	6,423	-0.239
SP-06	260	-39.4	-66.6	-53.0	6,086	-0.323
SP-10	20.8	-95.0	-78.5	-86.8	5,394	-0.468

Table 5.28: Observed confining stress from VWSG in pile caps.

The average measured confining stress for the pile caps with 18-inch embedded piles was 0.404 ksi and 0.468 ksi for the pile cap with 30-inch embedded pile. This is much higher than the estimated confining stresses found using Equation 4.27.

- Measured versus Estimated Strand Stress at Failure

The strand stress at failure was determined from the experimental results using RESPONSE2000. The maximum strand stress (f_{pu}) was modified in the material properties until the calculated maximum moment was equal to the measured maximum moment. The strand stress was calculated for different pile embedment lengths based on AASHTO LRFD using the equations shown in Figure 4.72. The strand stress was also found using the equation proposed by ElBatanouny and Ziehl [4] for transfer length, Equation 5.32, and development length, Equation 4.29.

TransferlengthusingElBatanouny and Ziehl [4]
$$L_{dc} = \frac{f_{se}}{5000} * d_b$$
Equation 5.44

The same bilinear relationship can be used to find the strand stress based on the available development length, shown in Figure 5.74.



Figure 5.74: Bilinear relationship used for strand stress for ElBatanouny and Ziehl [4].

The calculated strand stress for each embedment length was used to find the corresponding maximum moment using RESPONSE2000. AASHTO LRFD and ElBatanouny and Ziehl do not

consider the axial load applied to the piles. The axial load and interface reinforcement was considered while calculating the maximum moment using RESPONSE2000. The slipping stress and maximum moments from the experimental testing, AASHTO LRFD BDS, and ElBatanouny and Ziehl [4] are summarized in Table 5.29. The ratio of the measured to estimated moment is provided for AASHTO LRFD BDS and ElBatanouny and Ziehl [4] along with the average, standard deviation, and coefficient of variation. A measured-to-estimated strength ratio greater than 1.0 signifies a conservative estimate. The estimated value for SP-10 is not included in the statistical analysis, since SP-10 failed due to punching shear of the edge of the pile cap, which is not captured by the development length calculations. Both procedures conservatively estimated the strength of the specimens, on average, with the estimation procedure of ElBatanouny and Ziehl [4] resulting in the more accurate estimation.

Spec.	Experim ental			AASHTO LRFD		Elbatanou ny	and	Ziehl
	Slipping stress (ksi) ¹	Max. moment (kip-ft)	Slipping stress (ksi)	Max. moment (kip-ft) ²	Meas./ Est.	Slipping stress (ksi)	Max. moment (kip-ft) ²	Meas./ Est.
SP-01	81.0	114.1	35.2	50.5	2.26	57.7	82.4	1.38
SP-02	86.0	244.6	35.2	182.5	1.34	57.7	210.4	1.16
SP-03	80.0	190.8	35.2	140.7	1.36	57.7	163.0	1.17
SP-04	87.0	122.8	52.8	75.0	1.64	86.5	121.9	1.01
SP-05	88.0	246.2	52.8	204.8	1.20	86.5	244.9	1.01
SP-06	115.0	159.4	70.4	99.2	1.61	115.4	160.7	0.99
SP-07	148.0	201.4	105.6	146.9	1.37	173.1	232.9	0.86
SP-08	204.0	267.6	158.4	214.0	1.25	207.0	272.1	0.98
SP-09	121.0	574.6	71.7	344.3	1.67	115.4	542.6	1.06
SP-10 3	188.0	868.1	179.2	832.6	1.04 ³	220.2	1015.1	0.86 ³
				Average =	1.52		Average =	1.07
				St. Dev. =	0.31		St. Dev. =	0.14
				Co. of Var. =	0.20		Co. of Var. =	0.13

Table 5.29: Maximum moment and slipping stress (experimental, AASHTO LRFD BDS, ElBatanouny and Ziehl)

¹ Experimental slipping stress was determined using maximum moment developed by specimen into RESPONSE. ² Maximum moment was determined using value of slipping stress into RESPONSE.

³ Failure of SP-10 was due to punching shear of the edge of the pile cap, so these values were not included in statistical analysis of the estimation procedures.

The stress in the pile strands versus available development length measured through the experimental testing is plotted with the strand stress estimation equations from AASHTO LRFD BDS and ElBatanouny and Ziehl [4] in Figure 5.75. The measured results generally align well with the estimated strand stress found using ElBatanouny and Ziehl [4].



Figure 5.75: Stress in strand versus available development length plots for: (a) 18-inch; (b) 30-inch pile specimens.

The initial recommendation based on the experimental testing is to determine the required embedment length using the ElBatanouny and Ziehl [4] equations, where the punching shear capacity does not control the capacity of the connection.

5.10.2.2 Punching Shear Failure of Pile Cap Edge

One of the specimens (SP-10) failed due to a failure of the edge of the pile cap prior to a strand development or flexural failure of the pile. The cracking pattern and failure mechanism observed for SP-10 was similar to a punching (two-way) shear failure for an edge column, as shown in Figure 4.54. The "column" for this punching shear failure can be assumed to be the compression force applied from the side bearing forces of the embedded pile, as shown in Figure 5.76.



Figure 5.76: Punching shear failure in pile-to-cap connections.

- Estimated Punching Shear Demand

Mattock and Gaafar [42] assumed a parabolic distribution of bearing stresses for C_b and a uniform stress distribution for C_f of $0.85f'_c$. The bearing stresses are distributed over the width of the embedded pile, b. The equation proposed by Mattock and Gaafar:

Mattock and Gaafar:
$$V_u = 54\sqrt{f'_c} \left(\frac{b'}{b}\right)^{0.66} \beta_1 b L_e \left[\frac{0.58 - 0.22\beta_1}{0.88 + \frac{a}{L_e - c}}\right]$$
Equation 5.45

where:

- a = shear span of the pile (distance from pile cap to assumed point of zero moment) (in)
- β_1 = concrete stress block factor defined in ACI 319-99
- b' = width of the element into which the pile is embedded
- b = width of the embedded pile

Mattock and Gaafar [42] propose simplified equations for design, shown in Equation 5.34 and Equation 5.35. They found that the maximum moment in the embedded element (steel sections for their research) occurred in the embedded portion of the element.

Mattock and Gaafar,
simplified equations:
$$V_n = \frac{21\sqrt{b'/b}\sqrt{f'_c}bL_e}{(0.88 + a'/L_e)}$$
 Equation 5.46
Max. moment (inside
connection): $M_{max} = V_n \left(a + \frac{L_e}{7}\right)$ Equation 5.47

The strain and stress distribution proposed by Mattock and Gaafar [42] is shown in Figure 5.77. They suggested the shear span be increased by the concrete cover, c, to account for possible spalling of the soffit of the pile cap. The value of b' is intended to account for the spreading of the compressive stresses away from the embedment.



Figure 5.77: Bearing stresses proposed by Mattock and Gaafar [42].

The top "column" force to use for the punching shear check can be found using this strain and stress distribution as shown in Equation 5.36, assuming c of 0 in since no spalling was observed in SP-10.

$$C_t = 0.85 f'_c \left(\frac{1}{3}\right) L_e b \qquad \text{Equation 5.48}$$

This equation can be slightly modified to include the α_l factor from AASHTO LRFD BDS (§5.6.2.2) to give Equation 5.37.

Mattock and Gaafar modified	$C = \alpha f' \begin{pmatrix} 1 \\ 1 \end{pmatrix} L h$	Equation 5.40
by AASHTO LRFD BDS:	$C_t = \alpha_1 \int_c \left(\frac{1}{3}\right) L_e b$	Equation 5.49

The α_1 could be found using the concrete strength for the pile cap. The punching shear demand forces using this procedure are summarized in Table 5.30.

Specimen	Embedment length	Le (in)	<i>b</i> (in)	f'c (ksi)	α1	C _t (kips)
SP-01	6.0	6.0	18.0	12.48	0.80	359.7
SP-02	6.0	6.0	18.0	12.36	0.80	357.3
SP-03	6.0	6.0	18.0	12.70	0.80	363.9
SP-04	9.0	9.0	18.0	11.93	0.81	522.7
SP-05	9.0	9.0	18.0	13.26	0.78	562.0
SP-06	12.0	12.0	18.0	11.40	0.82	674.7
SP-07	18.0	18.0	18.0	10.32	0.84	940.2
SP-08	27.0	27.0	18.0	12.57	0.80	1626.2
SP-09	12.0	12.0	30.0	9.37	0.85	955.2
SP-10	30.0	30.0	30.0	8.95	0.85	2283.2

Table 5.30: Punching shear force found using Equation 5.37

One issue with this approach is that it assumes that the concrete next to the embedded pile crushes, which may not occur depending on the capacity of the embedded pile. An alternate approach would be to use a modified compression block like that discussed in Collins and Mitchell [69] and used by Belarbi et al. [70] that considers the stress block shape when the extreme compression fiber does not crush, shown in Equation 5.38 through Equation 5.40.

Belarbi et al. [70]:
$$\beta_1 = \frac{4 - \frac{\varepsilon_{cc}}{\varepsilon'_c}}{6 - 2\left(\frac{\varepsilon_{cc}}{\varepsilon'_c}\right)} \left(1.1 - \frac{f'_c}{50}\right) \ge 0.65$$
Equation 5.50Belarbi et al. [70]: $\alpha_1 = \left(\frac{1}{\beta_1}\right) \left(\frac{\varepsilon_{cc}}{\varepsilon'_c} - \frac{1}{3}\left(\frac{\varepsilon_{cc}}{\varepsilon'_c}\right)^2\right) \left(1 - \frac{f'_c}{60}\right)$ Equation 5.51Belarbi et al. [70]: $\varepsilon'_c = \left(1.6 + \frac{f'_c}{11}\right) * 10^{-3}$ Equation 5.52

where:

- ε_{cc} = compressive concrete strain at the flexural compressive face (face of the embedment for this connection
- ε'_c = strain corresponding to f_c
- f'_c = specified concrete strength (ksi)
- α_1 = factor taken as the ratio of equivalent concrete compressive stress to the compressive strength of concrete
- β_1 = factor relating depth of equivalent rectangular compressive stress block to neutral axis

The assumed strain distribution and stress block with these assumptions is shown in Figure 5.78.



Figure 5.78: Assumed strain distribution and stress block for pile embedment.

The assumed compression block force is shown in Equation 5.41. The compression block depth can be assumed to be the same depth as was proposed by Mattock and Gaafar [42], shown in Figure 5.77 and Equation 5.42.

Assumed Compression Block Force:	$C_t = (\alpha_1 f_c) \big(\beta_1 x_f \big) b$	Equation 5.53
Assumed Compression Block Depth:	$\beta_1 x_f = \frac{L_e}{3}$	Equation 5.54

The maximum compressive strains on the face of the pile cap were measured during testing. The maximum measured strain was used to find the compression block using the equation above. Examples of the plots used to determine the top fiber strains are shown in Figure 5.79.



Figure 5.79: Measured compression strains on outside edge of pile caps for: (a) SP-09; (b) SP-10.

The maximum measured strains for each specimen and the compression block force found using Equation 5.41 and Equation 5.42 are summarized in Table 5.31.

Table 5.31: Measured compression strains in pile cap face and associated compression block force for	r
punching shear demand estimation	

Specimen	Embed. length	f'_c (ksi)	ε _{cc} (με)	βı	α1	$\begin{array}{c} \beta_l x_f \\ \text{(in)} \end{array}$	C _t (kips)	V _c (kips)	C_t/V_c
SP-01	6.0	12.48	70	0.65	0.035	2.00	15.9	50.6	0.3
SP-02	6.0	12.36	78	0.65	0.035	2.00	15.4	50.3	0.3
SP-03	6.0	12.70	140	0.65	0.061	2.00	27.7	51.0	0.5
SP-04	9.0	11.93	22	0.65	0.010	3.00	6.5	52.3	0.1
SP-05	9.0	13.26	20	0.65	0.009	3.00	6.1	55.1	0.1
SP-06	12.0	11.40	56	0.65	0.026	4.00	21.6	97.1	0.2
SP-07	18.0	10.32	128	0.65	0.063	6.00	70.4	99.7	0.7
SP-08	27.0	12.57	95	0.65	0.042	9.00	84.8	114.3	0.7
SP-09	12.0	9.37	113	0.65	0.059	4.00	66.2	189.3	0.3
SP-10	30.0	8.95	719	0.65	0.351	10.00	943.2	211.0	4.5

The C_t force found in Table 5.31 is the assumed punching shear demand, shown in Equation 5.43.

Punching Shear Demand:

 $V_u = C_t = (\alpha_1 f_c) {L_e / 3} b$ Equation 5.55

- Estimated Punching Shear Capacity

The punching shear capacity is typically found based on the critical shear perimeter, b_0 , as shown in Figure 5.80 (a). The critical shear perimeter is based on the effective shear depth, d_{ν} , or the distance between the compression face and centroid of the tension reinforcement. For a column located along the edge of the slab, the critical shear perimeter would be found as shown in Figure 5.80 (b). The punching shear capacity of the edge of the pile cap is assumed to have a critical shear perimeter as shown in Figure 5.80 (c) based on the width of the embedded pile, the edge distance, and the height of the compression block from Mattock and Gaafar [42] shown in Figure 5.77.



Figure 5.80: Typically assumed punching shear cracking and critical shear perimeter for: (a) interior column; (b) edge column; (c) typical punch shear theory extended to embedded pile and pile cap edge.

According to AASHTO LRFD BDS §5.7.2.8, the effective shear depth, d_v , is taken as the distance, measured perpendicular to the neutral axis, between the resultants of the tensile and compressive forces due to flexure; it need not be taken to be less than the greater of $0.9d_e$ and 0.72h. This can conservatively be taken as 0.72h to be independent of the reinforcement provided in the edge of the pile cap, where *h* is equal to the edge distance.

With these assumptions, the critical shear perimeter can be found using Equation 5.44.

Assumed critical shear
perimeter:
$$b_0 = 2(0.72h) + d_{pile} + \frac{2}{3}L_e$$
 Equation 5.56

The estimated punching shear strength, of two-way action, for footings was calculated following AASHTO LRFD BDS §5.12.8.6 [3]. For two-way action for sections with transverse reinforcement, the nominal shear resistance is found using Equation 5.45 through Equation 5.47.

AASHTO 5.12.8.6.3-2
$$V_n = V_c + V_s \le 0.192\lambda \sqrt{f'_c} b_o d_v$$
 Equation 5.57

In which:

AASHTO 5.12.8.6.3-3
$$V_c = 0.0632\lambda\sqrt{f'_c}b_od_v$$
Equation 5.58AASHTO 5.12.8.6.3-4 $V_s = \frac{A_v f_y d_v}{s}$ Equation 5.59

where:

 b_o = perimeter of the critical section for shear (in)

 d_v = effective shear depth (in)

 λ = concrete density modification factor

The amount of reinforcement to include in the punching shear resistance provided by the steel, Equation 5.47, is determined based on the transverse reinforcement provided in a slab. The reinforcement provided in the 30-inch pile cap is shown in Figure 5.81. The transverse reinforcement for the punching shear cone is the #9 bars labeled Bar 2A and shown in Figure 5.81 (b).



Figure 5.81: Reinforcement in 30-inch pile caps: (a) all reinforcement; (b) Bar 2A (#9 bars) rebar provided.

It is assumed that there are two (2) #9 bars on each side of the 18-inch pile and three (3) #9 bars on each side of the 30-inch pile that engage the punching shear crack. These bars are assumed to be the transverse reinforcement provided in the punching shear cone with a width equal to the pile width plus two times the edge thickness, as shown in Figure 5.82.



Figure 5.82: Assumed 45-degree spread for punching shear failure.

The punching shear capacity can be found using Equation 5.45 through Equation 5.47. The concrete component and upper limit for the punching shear capacity for all experimental specimens are summarized in Table 5.32.

Specimen	f'c (ksi)	λ	t _{edge} (in)	d_{v} (in)	b_{θ} (in)	V _c (kips)	V _{n,upper} (kips)
SP-01	12.5	1.0	9.0	6.48	34.96	50.6	153.7
SP-02	12.4	1.0	9.0	6.48	34.96	50.3	152.9
SP-03	12.7	1.0	9.0	6.48	34.96	51.0	155.0
SP-04	11.9	1.0	9.0	6.48	36.96	52.3	158.8
SP-05	13.3	1.0	9.0	6.48	36.96	55.1	167.5
SP-06	11.4	1.0	9.0	6.48	38.96	97.1	163.7
SP-07	10.3	1.0	9.0	6.48	42.96	99.7	171.7
SP-08	12.6	1.0	9.0	6.48	48.96	114.3	226.0
SP-09	9.4	1.0	15.0	10.80	59.60	189.3	378.2
SP-10	9.0	1.0	15.0	10.80	71.60	211.0	444.3

Table 5.32: Concrete component of punching shear capacity for edge of pile cap

The steel component of punching shear resistance, nominal capacity, and demand are summarized in Table 5.33.

Specimen	$A_{\nu}(\mathrm{in}^2)$	A_{v}/s (in)	f_y (ksi)	V _s (kips)	V_n (kips)	V_u (kips)
SP-01	0.00	0.00	60.0	0.0	50.6	15.9
SP-02	0.00	0.00	60.0	0.0	50.3	15.4
SP-03	0.00	0.00	60.0	0.0	51.0	27.7
SP-04	0.00	0.00	60.0	0.0	52.3	6.5
SP-05	0.00	0.00	60.0	0.0	55.1	6.1
SP-06	4.00	0.11	60.0	43.2	97.1	21.6
SP-07	4.00	0.11	60.0	43.2	99.7	70.4
SP-08	4.00	0.11	60.0	43.2	114.3	84.8
SP-09	6.00	0.10	60.0	64.8	189.3	66.2
SP-10	6.00	0.10	60.0	64.8	211.0	943.2

Table 5.33: Steel component and nominal punching shear capacity for edge of pile cap

The only specimen where the punching shear demand exceeded the capacity is SP-10, which is consistent with the observations from experimental testing.

- Limitations with Approach

The measured top fiber concrete strain was used in the procedure previously described to determine the punching shear demand. The demand values found assuming that the concrete crushes and top fiber strain is 0.003 are shown in Table 5.30. It would seemingly be excessive to design based on these values.

5.10.3 Effect of Axial Load

Two of the specimens had applied axial load with embedment lengths of 6 inches (SP-02) and 9 inches (SP-05). The total axial load applied for each specimen was 194 kips per pile. The procedure for applying the axial load to the piles is presented in §5.7.

Failure of SP-02 and SP-05 was caused by strand development failure. Failure of SP-02 is shown in Figure 5.83; the failure of SP-02 was like that of SP-05. Damage occurred in the compression zone of the embedded piles with axial force as the hinge developed in the base of the pile near the pile cap, as shown in Figure 5.83 (b).



Figure 5.83: Photographs after failure of SP-02.

The moment versus displacement responses for the specimens with axial load (SP-02 and SP-05) and the similar specimens without axial load (SP-01 and SP-04) are shown in Figure 5.84. SP-02 which had the same embedment length as SP-01 developed a moment of 244.6 kip-ft, which corresponds to 74% of the 18-inch pile capacity. SP-05, with the same embedment length as SP-04 developed 246.2 kip-ft, around 74% of the 18-inch pile capacity. The application of the $0.05f'_cA_g$ axial load led to an increased average connection capacity of 107%.



Figure 5.84: Moment-displacement for specimens with axial load: (a) 6-inch embedment length; (b) 9-inch embedment length.

The moment-curvature plots for 18-inch and 30-inch piles with varying levels of axial force assuming the full development of the strands were found using RESPONSE2000, as shown in Figure 5.85. These curves were found using the measured compressive strength and the strand configuration used in the constructed piles. The axial load levels shown correspond to $0A_gf'_{c,pile}$, $0.05A_gf'_{c,pile}$, and $0.10A_gf'_{c,pile}$, with the $0.05A_gf'_{c,pile}$ for the 18-inch pile being equal to the actual axial load applied.



Figure 5.85: Moment versus curvature plots for: (a) 18-inch; (b) 30-inch piles with different levels of applied axial load. (f'_{c, pile} = 12 ksi)

The maximum moment and slipping stress for these specimens is summarized in Table 5.34. From RESPONSE2000 assuming fully developed strands, the increase in capacity from 0 kips to 194 kips of axial load for the 18-inch pile was 329.7 kip-ft to 422.1 kip-ft (28% increase). This is less than the average 107% increase in capacity of the connection observed through the experimental testing. The application of axial force had a much larger impact on the strength of the piles when the strands were not fully developed. The slipping stress found from the experimental results was not influenced significantly by the application of the axial force (an average 4% increase). The estimated slipping stresses using AASHTO LRFD BDS [3] and ElBatanouny and Ziehl [4] is not affected by an applied axial force.

Spec.	Experim ental			AASHT O LRFD		Elbatanouny	and	Ziehl
	Slipping stress (ksi) ¹	Max. moment (kip-ft)	Slipping stress (ksi)	Max. moment (kip-ft) ²	Meas./ Est.	Slipping stress (ksi)	Max. mome nt (kip- ft) ²	Meas./ Est.
SP-01	81.0	114.1	35.2	50.5	2.26	57.7	82.4	1.38
SP-02	86.0	244.6	35.2	182.5	1.34	57.7	210.4	1.16
SP-04	87.0	122.8	52.8	75.0	1.64	86.5	121.9	1.01
SP-05	88.0	246.2	52.8	204.8	1.20	86.5	244.9	1.01

 Table 5.34: Maximum moment and slipping stress (experimental, AASHTO LRFD BDS, ElBatanouny and Ziehl)

¹ Experimental slipping stress was determined using maximum moment developed by specimen into RESPONSE. ² Maximum moment was determined using value of slipping stress into RESPONSE. Larger transverse tensile strains were measured in the pile cap for the members with axial force, likely a result of there being a larger moment capacity of the connection. An example of the larger observed concrete strains is shown in Figure 5.86.



Figure 5.86: Measured concrete strains on the west side face of the pile cap in: (a) SP-01; (b) SP-02 with 6-inch pile embedment lengths.

Larger strains were also measured in the reinforcement in the pile cap for the specimens with axial force, also likely a result of the higher moment capacity of the connection with axial force. An example of the measured rebar strains for specimens with and without axial force and 6-inch pile embedment is shown in Figure 5.87.



Figure 5.87: Measure pile cap longitudinal reinforcement strain for: (a) SP-01; (b) SP-02 with 6-inch pile embedment lengths.

In general, a small axial compression force greatly increased the capacity of the connection; an average 107% increase in capacity of the connection was observed when $0.05A_g f'_{c,pile}$ axial compression was applied to the pile and connection.

5.10.4 Effect of Interface Reinforcement

Interface reinforcement was provided in one specimen (SP-03) with the same 6-inch embedment as SP-01 without interface reinforcement. The details for the interface reinforcement, based on Larosche et al. [18], are shown in Figure 5.88. Four #6 bars were embedded 24 inches in the ends of the piles during pile casting. The bars extended 12 inches into the pile cap with 9-inch hooks on the ends.



Figure 5.88: Details of interface reinforcement for SP-03: (a) elevation; (b) Section A-A.

Photographs from failure of SP-03 are shown in Figure 5.89. Two cracks developed in SP-03 during failure: one at the pile-to-cap connection and a second at the location where the interface reinforcement ended (24 inches from the end of the pile and 18 inches from the pile cap face). A strand development failure was defined for SP-02. Significant cracking of the pile cap was also observed in this specimen and spalling of concrete around the embedded piles.



Figure 5.89: Photographs of the failure of SP-03.

The two large cracks during failure were also observed in the fiber optic sensors, shown in Figure 5.90 with the location of the two increases in strain coinciding with the location of the pile cap face and end of the interface reinforcement.



Figure 5.90: Strains along the east side of the west pile measured by FOS for SP-03.

The available development length would be the distance between the end of the pile and the failure crack. Since there were two large cracks that developed during failure, the available development length could have been 6 inches (to the pile-to-cap interface) or 24 inches (to the end of the interface reinforcement). The estimated slipping stresses using ElBatanouny and Ziehl [4] for each of the assumed available development lengths and the corresponding moment capacity found from RESPONSE are summarized in Table 5.35. The analysis of the section at the interface (with 6-inch development length) included the interface reinforcement. The analysis of the section at the end of the interface reinforcement (with 24-inch development length) did not include the interface

reinforcement. Using an available development length of 6-inches and including the interface reinforcement resulted in a lower estimated moment capacity and one that was closer to the actual measured moment capacity of the connection. For design of connections with interface reinforcement, it is recommended to use the minimum of these two capacities to estimate the strength of the connection.

		Experim ental		Elbatanouny	and	Ziehl
Spec.	Assumed I _{d,avail.} (in)	Slipping stress (ksi) ¹	Max. moment (kip-ft)	Slipping stress (ksi)	Max. mome nt (kip- ft) ²	Meas./ Est.
SP-01	6.0	81.0	114.1	57.7	82.4	1.38
SP-03a	6.0	80.0	190.8	57.7	163.0	1.17
SP-03b ³	24.0			196.6	260.2	0.73

Table 5.35: Maximum moment and slipping stress (experimental and ElBatanouny and Ziehl)

¹ Experimental slipping stress was determined using maximum moment developed by specimen into RESPONSE. ² Maximum moment was determined using value of slipping stress into RESPONSE.

³ Analysis of this point did not include the interface reinforcement because the section being analyzed is right at the end of the reinforcement.

The moment versus displacement response for SP-01 (without interface reinforcement) and SP-03 (with interface reinforcement) is shown in Figure 5.91. The specimen with the interface reinforcement (SP-03) developed a moment capacity 67% higher than the similar specimen without interface reinforcement (SP-01), both with 6-inch pile embedment lengths. The capacity of SP-01 corresponded to 34% of the 18-inch pile capacity SP-03 with 58% of the 18-inch pile capacity. The test for SP-01 needed to be stopped due to running out of stroke in the hydraulic jack. It is not clear from testing that the presence of the interface reinforcement affected the rotational capacity of the connection.



Figure 5.91: Moment versus displacement curves for 18-inch pile with 6-inch embedment with and without interface reinforcement.

The reinforcement in the pile cap was significantly more engaged for SP-03 compared to SP-01, as shown in Figure 5.92 through Figure 5.94. The transverse reinforcement in SP-03 toward the center of the pile cap was more engaged than any other specimen and had larger strains than reinforcement toward the outside face of the pile cap, see Figure 5.92 (b).



Figure 5.92: Load versus rebar strain for transverse pile cap reinforcement in the connection face for: (a) SP-01; (b) SP-03.

The longitudinal reinforcement in the pile cap was also more engaged in SP-03 than SP-01, see Figure 5.93. The strains in SP-03 were highest in the longitudinal reinforcement immediately adjacent to the embedded pile.



Figure 5.93: Load versus rebar strain for longitudinal pile cap reinforcement in the connection face for: (a) SP-01; (b) SP-03.

The pile cap reinforcement along the west side face was also more engaged in SP-03 than SP-01, see Figure 5.94. The reinforcement strains are greater toward the face of the pile cap with the embedded pile.



Figure 5.94: Load versus rebar strain for transverse pile cap reinforcement in the west side face for: (a) SP-01; (b) SP-03

The curvature found using the crack displacement transducers (CDT) was generally minimal. This was a result of the failure crack in the specimens typically occurring at the interface, which was outside of the CDT closest to the interface. The measured moment-curvature response with CDTs for most specimens resembled the response shown for SP-01 in Figure 5.95 (a). A large crack occurred in SP-03 during failure within the range of a CDT, as shown in Figure 5.89. This led to a larger curvature being measured during testing, as shown in Figure 5.95 (a).



Figure 5.95: Moment versus curvature measured using the crack displacement transducers for: (a) SP-01; (b) SP-03.

5.10.5 Effect of Pile Size

Two pile sizes were tested in the experimental program: 18-inch and 30-inch. Six of the specimens that can be used to compare the effect of pile size are summarized in Table 5.36. The piles with a similar embedment length had developed a similar percentage of the pile capacity, compare 12-inch embedment length for 18-inch and 30-inch piles (SP-06 and SP-09). The effect of the embedment length as a proportion of pile size did not seem to have a similar effect for 18-inch and 30-inch pile embedment specimens. This supports the idea that the capacity of the connection is dependent on the available development length and not necessarily the pile size.

Specimen	Pile Size	Embedment Length	Pile Capacity (kip-ft)	Max Moment Developed (kip-ft)	% Of Pile Capacity	Failure Mechanism
SP-01	18"	$6"(0.33d_p)$	331.0	114.1	34%	Strand Development
SP-06	18"	$12"(0.67d_p)$	331.0	159.4	48%	Strand Development
SP-07	18"	$18"(1.00d_p)$	331.0	201.4	61%	Strand Development
SP-08	18"	27" $(1.50d_p)$	331.0	267.6	81%	Strand Development
SP-09	30"	$12"(0.40d_p)$	1188.5	574.6	48%	Strand Development
SP-10	30"	$30"(1.00d_p)$	1188.5	868.1	73%	Punching Shear

Table 5.36: Effect of pile size summary of results

Chapter 6: Final Computational Analysis

The final computational analysis was accomplished using a nonlinear finite element analysis (FEA) software designed for reinforced concrete structures, ATENA [56]. The geometry of the numerical models created in the preliminary numerical analysis were updated based on the final test set up used in the experimental program. Results from the experimental results were used to validate the computational analysis. The final computational study was expanded with additional numerical models to study other variables that were not tested experimentally.

6.1 PILE-TO-CAP MODELING ASSUMPTIONS

A nonlinear finite element analysis software specifically designed for reinforced concrete structures, ATENA, was used to validate the specimens in the experimental matrix presented in Table 6.1. The program has detailed bond-slip models that are capable of capturing the slip of the prestressing strands, detailed interface material models, detailed concrete material models, and detailed crack patterns.

Specimen No.	Pile Size	Embedment Length	Embedment Length	Interface Reinforcement	Axial Load
1	18"	$0.33d_{pile}$	6.0"	w/o interface reinforcement	$0A_g f'_c$
2	18"	$0.33 d_{pile}$	6.0"	w/o interface reinforcement	$0.1A_g f'_c$
3	18"	$0.33 d_{pile}$	6.0"	w/interface reinforcement	$0A_g f'_c$
4	18"	$0.5 d_{pile}$	9.0"	w/o interface reinforcement	$0A_g f'_c$
5	18"	$0.5 d_{pile}$	9.0"	w/o interface reinforcement	$0.1A_g f'_c$
6	18"	$0.67 d_{pile}$	12.0"	w/o interface reinforcement	$0A_g f'_c$
7	18"	$1.0d_{pile}$	18.0"	w/o interface reinforcement	$0A_g f'_c$
8	18"	$1.5d_{pile}$	27.0"	w/o interface reinforcement	$0A_g f'_c$
9	30"	$0.4d_{pile}$	12.0"	w/o interface reinforcement	$0A_g f'_c$
10	30"	$1.0d_{pile}$	30.0"	w/o interface reinforcement	$0A_g f'_c$

Table 6.1: Experimental matrix

6.1.1 Model Geometry

The geometry of the models was updated from the preliminary numerical study of Task 3, based on the final test set up for the experimental program where a self-reacting frame with two piles embedded in one pile cap was used.

The geometry was first drawn in AutoCAD 3D. Typical models consisted of five 3D volume components (pile cap, two piles, and two plates) and 1D lines representing the rebar in the pile

cap, strands, and wires in the pile, as shown in Figure 6.1 (a). After defining the geometry in AutoCAD 3D, each section was imported into ATENA [56], as shown in Figure 6.1(b).



Figure 6.1: Numerical models geometry: (a) AutoCAD drawing; (b) ATENA model.

Interfaces were defined between volume elements with different materials that shared common surfaces. As an example, a fixed contact (Master-Slave) connection was defined between the concrete pile and elastic plate where the load was applied.

The reinforcement scheme used in the typical pile-to-cap connection specimens is shown in Figure 6.2. The prestressing strands were $\frac{1}{2}$ " special strands with a diameter of 0.52 inches. Conventional reinforcement (#5, #6, #9 and W3.4 wire) was used in the piles and pile caps.



Figure 6.2: Reinforcement scheme in piles and pile cap.

6.1.2 Material Assumptions

Three different materials were used for the analysis: (1) a solid concrete material for the pile and pile cap, (2) an elastic solid material for the plates, and (3) 1D reinforcement for the reinforcing bars and prestressing strands.



Figure 6.3: Material properties: (a) solid materials; (b) 1D reinforcement.

6.1.2.1 Solid Concrete Material

The concrete material was created considering the average pile and pile cap concrete strength at the time of testing. The measured compressive strength on test day is summarized in Table 6.2.

Specimen	f'c,pile,west (ksi)	f'c,pile,east (ksi)	f'c,cap (ksi)
SP-01	11.90	11.90	12.48
SP-02	11.45	11.45	12.36
SP-03	11.58	11.58	12.70
SP-04	11.90	11.58	11.93
SP-05	12.02	12.02	13.26
SP-06	11.58	11.90	11.40
SP-07	11.58	11.90	10.32
SP-08	11.58	11.90	12.57
SP-09	13.13	13.13	9.37
SP-10	13.82	13.82	8.95

Table 6.2: Measured compressive strength on test day for concrete in piles and pile caps.

Concrete 11,700 (which corresponds to a concrete strength of 11.7 ksi) was used in the 18-inch piles, and Concrete 12,000 in the 18-inch cap. For the 30-inch models, Concrete 13,000 was used in the piles and Concrete 9,000 in the cap.

A summary of the concrete parameters is shown in Table 6.3. The modulus of elasticity and tensile strength, for normal weight concrete was found using ACI 318-19 [64] §19.2.2.1 and §19.2.3.1, as shown in Equation 5.6 and Equation 6.2, respectively. Poisson's ratio for normal weight concrete was assumed as 0.2.

Modulus of Elasticity: ACI 19.2.2.1	$E_c = 57,000\sqrt{f'_c}$	Equation 6.60
Tensile strength: ACI 19.2.3.1	$f_t = 7.5 \sqrt{f'_c}$	Equation 6.61

where:

 $\Delta f'_c$ = compressive strength of concrete (psi)

Table	6.3:	Material	parameters	of concrete
1 4010	0.5.	maicriai	parameters	of concrete

Material Parameter	Concrete9000	Concrete11700	Concrete12000	Concrete13000
Modulus of elasticity (ksi)	5407	6165	6244	6499
Poisson's ratio	0.2	0.2	0.2	0.2
Tensile strength (ksi)	0.711	0.811	0.821	0.855
Compressive strength (ksi)	-9.0	-11.7	-12.0	-13.0

During the prestressing of the pile, an additional concrete model was created for the pile cap, so that it did not restrain the pile during the prestressing process. ConcreteSoft was created with the same properties as the corresponding pile cap material, but with no stiffness.

6.1.2.2 Solid Elastic Material

The material used for the steel plates was generated using the Solid Elastic. option with the properties shown in Table 6.4. Similar to the concrete, a soft elastic material with no stiffness was used for the steel plates during the prestressing of the piles.

Table 6.4: Material parameters of steel plates

Material Parameter	Steel Plate
Modulus of elasticity (ksi)	29000
Poisson's ratio	0.3

6.1.2.3 1D Reinforcement

The reinforcing steel in the pile cap (#5, #6, and #9 bars) and the W3.4 wires confining the strands in the piles were all modeled as 1D reinforcement with a yield strength (f_1) of 60 ksi, yield strain (ε_1) of 0.00207, an ultimate strength (f_2) of 90 ksi and a strain at ultimate strength (ε_2) of 0.025 with a stress-strain relationship similar to that shown in Figure 6.4 (a).



Figure 6.4: Stress-strain relationship: (a) reinforcing steel; (b) strands.

The prestressing strands were also created using the 1D reinforcement option, but with a tendon type option. The stress-strain relationship used for the prestressing strands is shown in Figure 6.4 (b). The critical values used for this curve are the following: yield strength (f_1) of 204 ksi, yield strain (ε_1) of 0.007, second critical stress (f_2) of 243 ksi, second critical strain (ε_2) of 0.011, ultimate strength (f_3) of 270 ksi and strain at ultimate strength (ε_3) of 0.043. These values were based on the Ramberg-Osgood stress-strain relationship.

The stress in the strands was applied as an Initial Strain Function. The strain was calculated considering the actual jacking force during tensioning of 34 kips, the area of the strands, 0.167 in², and the experimental long-term losses.

The initial stress in strands:

Initial stress in strands:
$$f_{pi} = \frac{P_{strand}}{A_{strand}} = \frac{34 \text{ kips}}{0.167 \text{ in}^2} = 203.6 \text{ ksi}$$
 Equation 6.62

where:

 $P_{strands}$ = jacking force (kips) $A_{strands}$ = area of strands (in²)

Prestress losses estimates were found using AASHTO LRFD Bridge Design Specification (§5.9.3) [3].

In pretensioned members:
AASHTO 5.9.3.1-1
$$\Delta f_{pT} = \Delta f_{pES} + \Delta f_{pLT}$$
 Equation 6.63

where:

 $\Delta f_{pT} = \text{total loss (ksi)}$

- Δf_{pES} = sum of all losses or gain due to elastic shortening or extension at the time of application of prestress and or external loads (ksi)
- Δf_{pLT} = losses due to long-term shrinkage and creep of concrete, and relaxation of the steel (ksi)

Loss due to elastic shortening in pretensioned members was estimated using Equation 5.7.

AASHTO LRFD
(C5.9.3.2.3a-1)
$$\Delta f_{pES} = \frac{A_{ps}f_{pbt}(I_g + e_m^2 A_g) - e_m M_g A_g}{A_{ps}(I_g + e_m^2 A_g) + \frac{A_g I_g E_{ci}}{E_p}}$$
Equation 6.64

The long-term prestress loss, Δf_{pLT} , due to creep of concrete, shrinkage of concrete, and relaxation of steel should be found using the approximate estimate equation, shown in Equation 5.8.

AASHTO 5.9.3.3-1
$$\Delta f_{pLT} = 10.0 \frac{f_{pi}A_{ps}}{A_g} \gamma_h \gamma_{st} + 12.0 \gamma_h \gamma_{st} + \Delta f_{pR}$$
 Equation 6.65

In which:

AASHTO 5.9.3.3-2
$$\gamma_h = 1.7 - 0.01H$$
 Equation 6.66

AASHTO 5.9.3.3-3
$$\gamma_{st} = \frac{5}{(1 + f'_{ci})}$$
 Equation 6.67

where:

- f_{pi} = prestressing steel immediately prior to transfer (ksi)
- H = average annual ambient relative humidity (percent)
- y_h = correction factor for relative humidity of the ambient air
- y_{st} = correction factor for specified concrete strength at time of prestress transfer to the concrete member
- f_{pR} = an estimate of relaxation loss taken as 2.4 ksi for low relaxation strand and in accordance with the manufacturers recommendations for other types of strands (ksi)

Estimated losses for the piles are shown in Table 6.5.

Table 6.5: Estimated prestress losses and effective stress in strands for 18-inch and 30-inch piles

Pile Size	Elastic Shortening Loss (ksi)	Long-Term Prestress Loss (ksi)	Total Prestress Losses (ksi)	Effective Stress after all Losses (ksi)
18-inch	7.4	18.8	26.2	177.4
30-inch	5.4	16.4	21.8	181.8

The applied strain in strands after losses for the 18-inch piles:

Strain in strands after losses: $\varepsilon = \frac{f_{pe}}{E_{strands}} = \frac{177.4 \text{ ksi}}{29000} = 0.00613$ Equation 6.68

where:

 f_{pe} = effective prestressing steel (ksi) E_{strands} = modulus of elasticity of steel (ksi)

A summary of the strains used with each pile size is shown in Table 6.6

Table 6.6: Strain in strands after losses

Pile Size	Strain in strands
18-inch	0.00613
30-inch	0.00627

6.1.3 Boundary Conditions

The experimental test setup was a self-reacting frame system with two piles, as shown in Figure 6.5. This frame was determined to be the simplest setup to be used and have the least impact on the pile-to-cap connection behavior. Four threaded rods extended through the specimens attaching it to the strong floor, as shown in Figure 6.5 (a). The piles were loaded from the inside using a hydraulic jack located between 6 ft. and 12ft. from the pile-to-cap interface, as shown in Figure 6.5 (b).



Figure 6.5: Test configuration used for modeling connection specimens.

To create a fixed condition for the cap a constraint in the z direction was placed on the back of the pile cap (opposite to the pile); and a constraint in the x direction on the bottom of the pile cap, as shown in Figure 6.6. These boundary conditions created a moment restraint in the pile cap similar to what was expected in the laboratory, with the bottom of the cap resting on the strong floor.



Figure 6.6: Boundary conditions.

Similar boundary conditions were used in specimens without axial load application. Boundary conditions are an important parameter when defining the structure of the model, which showed to have a great impact in the stiffness of the model.

6.1.4 Load Protocol

A construction process was required to properly apply the prestressing and axial load in the piles before the lateral load was applied to fail the specimens. Three different loading stages were used, as shown in Figure 6.7, which are similar to how the specimens were loaded in the laboratory.

- *Load Stage #1*: prestrain applied to the prestressing strands.
- *Load Stage* #2: axial load applied to the piles (if required)
- *Load Stage #3*: lateral load applied to piles until failure of system.



Figure 6.7: Load protocol: (a) load stage #1; (b) load stage #2; (c) load stage #3.

6.1.4.1 Load Stage #1

The purpose of Load Stage #1 was to prestress the strands in the piles. The pile concrete strength was defined with typical stiffness. The pile cap concrete was specified with a stiffness close to zero, so the pile cap did not restrain the pile during prestressing. The total desired prestrain was applied to the piles in 10 steps. The pre-strain was locked in and kept constant at the end of this load stage.

6.1.4.2 Load Stage #2

The purpose of Load Stage #2 was to apply the axial load to the piles, if required. The "soft" materials were redefined with the material properties desired for the final test, as shown in Table 6.7. The axial load was applied to the end of the pile in 10 separate steps. The axial load was then kept constant on the pile at the end of this load stage.

Old Material	New Material
Concrete12000 (Soft)	Concrete12000
SteelPlate (Soft)	SteelPlate

Table 6.7: New material definitions for Load Stage #2

6.1.4.3 Load Stage #3

The purpose of Load Stage #3 was to determine the moment capacity of the pile-to-cap connection by applying a lateral load until failure. The prestrain in the strands and axial load in the piles were both kept constant during this load stage. Lateral load was applied, as shown in Figure 6.7 (c), by applying a displacement for 90 steps. The maximum observed load was recorded as the failure load.

6.1.5 Finite Element Mesh

The finite element mesh had an important influence on the quality of the analysis results and speed of the numerical modeling. Linear elements were used for the 1D Reinforcement elements (strands and rebar in the pile cap).

Two variables were considered when creating a mesh for the 3D volumes (piles and pile cap): type and number of elements. The default mesh generated by ATENA is an unstructured mesh with hexahedra elements, as shown in Figure 6.8 (a). This mesh showed results 68% higher than the experimental results. A structure mesh was defined using tetrahedra elements, as shown in Figure 6.8 (b)



Figure 6.8: Finite element mesh for pile-to-cap model: (a) tetrahedra elements; (b) hexahedra elements.

Different mesh sizes were considered, as shown in Figure 6.9. The final mesh size was selected considering the time it took to process the numerical model and the percentage of error with the experimental results. For the 18-inch specimens a mesh size of 3 inches was selected.



Figure 6.9: Size of finite element mesh for the 18-inch pile-to-cap model: (a) 1 inch; (b) 2 inches; (c) 3 inches.

6.2 NUMERICAL RESULTS FOR EXPERIMENTAL MATRIX

6.2.1 Bond-Slip Relationship of Strands

The bond-slip relationship of strands had an important influence on the pile-to-cap connection system. The bond-slip relationship is usually neglected and a perfect connection between the prestressed strands and the concrete is assumed in most nonlinear numerical analysis. For some cases, this approach is appropriate, but in the pile-to-cap connection system the effect of the bond slip could not be neglected.

The bond-slip relationship defines the bond strength (cohesion) τ_b depending on the value of current slip between the reinforcement and surrounding concrete. To consider the bond-slip relationship of the strands in the numerical analysis, ATENA contains three bond-slip models, the CEB-FIB model code 1990, slip law by Bigaj and the user defined law. The parameters of the first two are already predetermined by ATENA based on the concrete compressive strength,

reinforcement diameter and reinforcement type, as well as confinement conditions and the quality of concrete casting.

The selection of the adequate bond-slip relationship plays an important role in the accuracy of the numerical results. A description of different bond-slip used in this study is presented in this section.

6.2.1.1 CEB-FIP 1990 Model Code

The CEB-FIP 1990 Model Code [71] considers that under well-defined conditions there is an average "local bond" versus "local slip" relationship which is statistically acceptable. The bond stress-slip relationship depends on factors like bar roughness, concrete strength, position, and orientation of the bar during casting, state of stress, boundary conditions, and concrete cover.

The CEB-FIP 1990 Model Code bond-slip curve is shown in Figure 6.10.



Figure 6.10: Analytical bond stress-slip relationship by CEB-FIP model code 1990 [71].

The analytical bond stress-slip relationship by CEB-FIP 1990 consists of four different branches: the first ascending curvilinear part characterized by micro-cracking and local crushing; a constant plateau to express crushing and shearing of the concrete between the ribs, which occurs only in case of confined concrete; a descending branch which refers to a reduction in bond stress as concrete sheared off between the ribs; and a constant tail part, indicating the residual bond capacity.

Assumptions regarding the generation of bond stress include:

- Reinforcement and concrete have the same strain in areas of the structure which are under compression and in uncracked parts of the structure under tension.
- In cracked sections, the tension forces in the crack are transferred by the reinforcing steel.
- Due to relative displacements, bond stresses are generated between the concrete and the reinforcing steel.
- Between cracks, a part of the tension force of the reinforcing steel, acting in the crack, is transferred into the concrete by bond (tension stiffening effect).

The bond stresses between concrete and reinforcing bar can be calculated as a function of the relative displacement according to Equation 6.10 to Equation 6.13 .

$$\tau_b = \tau_{max} \left(\frac{s}{s_1}\right)^{\alpha}, 0 \le s \le s_1$$
Equation 6.69

$$\tau_b = \tau_{max}, s_1 < s \le s_2$$
 Equation 6.70

$$\tau_b = \tau_{max} - (\tau_{max} - \tau_f) \left(\frac{s - s_2}{s_3 - s_2}\right), s_2 < s \le s_3$$
 Equation 6.71

$$\tau_b = \tau_f, s_3 < s$$
 Equation 6.72

Where:

- τ_b = bond stress at slippage
- τ_{max} = maximum bond stress
- α = exponential coefficient
- τ_f = frictional bond stress

s, s_1, s_2 = characteristic slippage values at point 1, 2, 3, respectively.

Depending on the selection of the coefficient α ($0 \le \alpha \le 1$) in Equation 6.10, all forms of a bond stress-slip relationship can be modelled, starting from a bond characteristic with a constant stress ($\alpha = 0$) up to a bond stress-slip relationship with linear increasing bond stress ($\alpha = 1$).

The parameters for defining the mean bond strength-slip relationship that ATENA considers are given in Table 6.8. These parameters are valid for ribbed reinforcing steel with a related rib area according to international standards, depending on confinement, bond conditions, and concrete strength.

	2	3	4	5
Value	Unconfined concrete*	Unconfined concrete*	Confined concrete**	Confined concrete**
	Bond conditions	Bond conditions	Bond conditions	Confined concrete**
	Good	All other cases	Good	All other cases
S_1	0.6 mm	0.6 mm	1.0 mm	1.0 mm
S_2	0.6 mm	0.6 mm	3.0 mm	3.0 mm
S_3	1.0 mm	2.5 mm	Clear rib spacing	Clear rib spacing
α	0.4	0.4	0.4	0.4
$ au_{max}$	$2.0\sqrt{f_c}$	$1.0\sqrt{f_c}$	$2.5\sqrt{f_c}$	$1.25\sqrt{f_c}$
$\tau_{\rm f}$	$0.15 \tau_{max}$	$0.15 \tau_{max}$	$0.40 \tau_{max}$	$0.40 \tau_{max}$

Table 6.8 Parameters for defining the bond strength-slip relationship for ribbed bars [71]

*Failure by splitting of the concrete

**Failure by shearing of the concrete between the ribs

For ribbed reinforcement, confined concrete, and good bond quality, ATENA's CEB-FIB 1990 pre-determined bond model is shown in Figure 6.11.



Figure 6.11: CEB-FIB 1990 Model Code bond strength-slip relationship.

The CEB-FIB 1990 [71] bond model was defined to the strands in SP-01. Results are shown in Figure 6.12. Numerical results showed a stiffer behavior in comparison with the experimental results and a maximum moment of 99.5 kip-ft, which is approximately 87% the capacity of the pile.



Figure 6.12: SP-01 moment-displacement results with CEB-FIB 1990 bond model.

6.2.1.2 BIGAJ 1999

The second pre-defined bond model available in ATENA is based on the work by Bigaj (1999) [72]. Bigaj compared the bond stress-slip relationship experimentally obtained for confined concrete with the recommendations of the CEB-FIP Model Code 1990. The work concluded that the application of the CEB-FIP 1990 bond-stress slip relationship for the case of confined concrete leads to a considerable overestimation of bond stress when the yield stress of the bar is exceeded.

The bond stress-slip relation in the CEB-FIP 1990 has not been defined as a continuous function of the degree of confinement (quantified using the value of the concrete cover on the bar) but has only been given for two limit values for unconfined or confined concrete. Bigaj quantified the confining capacity of the concrete surrounding the bar and included this quantity in the description of the bond behavior to develop a bond model that will be fully capable of representing the influence of confinement on bond strength and force transfer by bond. This model depends on the bond quality, concrete cubic compressive strength f'_{cu} and reinforcement bar radius *d*. The slip law for this model is shown in Figure 6.13.



Figure 6.13: Bond law by Bigaj (1999) [72].

The ascending part of the stress-slip law, i.e. part a, is modeled by a bilinear curve. The coordinates of the four points defining this stress-slip relationship are listed in Table 6.9.

Concrete Type	Bond Quality		Point 1	Point 2	Point 3	Point 4
$f'_{c} < 60$	Excellent	s / D	0.000	0.020	0.044	0.480
		$\tau_b / \sqrt{0.8 f'_{cu}}$	0.500	3.000	0.700	0.000
	Good	s / D	0.000	0.030	0.047	0.480
		$\tau_b / \sqrt{0.8 f'_{cu}}$	0.500	2.000	0.700	0.000
	Bad	s / D	0.000	0.040	0.047	0.048
		$\tau_b / \sqrt{0.8 f'_{cu}}$	0.500	1.000	0.700	0.000
$f'_c > 60$	Excellent	s / D	0.000	0.012	0.030	0.340
		$\tau_b / \sqrt{0.88 f'_{cu}}$	0.600	2.500	0.900	0.000
	Good	s / D	0.000	0.020	0.030	0.340
		$\tau_b / \sqrt{0.88 f'_{cu}}$	0.600	1.900	0.900	0.000
	Bad	s / D	0.000	0.025	0.030	0.340
		$\tau_b / \sqrt{0.88 f'_{cu}}$	0.600	1.100	0.900	0.000

 Table 6.9: Parameters for defining the coordinates on the stress-slip relationship by Bigaj (1999) [72]

ATENA's Bigaj (1999) default stress-slip relationship for concrete type greater than 60 MPa (8.7 ksi), and excellent bond quality, is shown in Figure 6.14.



Figure 6.14: Bigaj (1990) bond strength-slip relationship.

Bigaj (1999) [72] model was defined for the strands in SP01 and the results are shown in Figure 6.15. Numerical results showed a maximum moment capacity of 125 kip-ft, 10% higher than the experimental results.
The Bigaj (1999) [72] and CEB-FIP 1990 [71] bond strength-slip relationships do not accurately predict the behavior of the pile-to-cap connection specimens, with the former overestimating the strength and the latter underestimating. The inaccuracy could be attributed to the fact that these models were originally developed for deformed bars and not prestressed strands.



Figure 6.15: SP-01 moment-displacement results with Bigaj (1990) bond model.

6.2.1.3 Modified bond-slip relationship for pretensioned concrete systems

The bond models presented by ATENA for the modeling of prestressed concrete systems showed a discrepancy between numerical results and the actual behavior of the pile-to-cap connection. While the literature on the numerical analysis for bond behavior of 7-wire strands is scarce, some researchers have evaluated the strand bond performance in concrete by performing bond tests to evaluate the bond strength between strands and concrete [73], [74], [75].

Mohandoss et al. [74] explained that the strand-concrete bond in pretensioned concrete systems is governed by three mechanisms: (i) adhesion, (ii) friction, and (iii) mechanical interlock. Unlike conventional reinforced concrete systems, due to the lubricant residue on the strand surface and the possible slip during the prestress release, the role of adhesion is minimal (at the member ends, the adhesion would be lost during prestress transfer). The friction and mechanical interlock play a significant role in the strand-concrete bond in pretensioned systems. Friction is provided by the concrete confinement and the wedging/interlock action is due to the Hoyer effect. The wedging action induces compressive stresses and enhances bonding of the released prestressing steel with the surrounding concrete. Mechanical interlock is provided by the concrete keys formed by the helical shape of the six outer wires of the strand.

Aly et al. [75] performed pullout tests for modeling bond stress-slip of 7-wire strands with Hanchorage dead-end embedded in concrete and developed an analytical model to predict the bond behavior. The measured bond stress-slip relationships for tested specimens exhibited four performance stages: an ascending curvilinear portion for the mechanical interlock between strand and the surrounding concrete, a constant plateau for mechanical interlocking strength and strand elongation, a linear ascending portion for representing the H-anchorage resistance, and a linear descending portion at post-peak failure stage. Stress-slip predicted bond model is shown in Figure 6.16.



Figure 6.16: Predicted bond model by Aly et al. [75].

Aly et al. [75] concluded that the bond stress increases with shorter embedment lengths and decreases as the embedment length increases with significant decrease in the stiffness. Aly et al. performed regression analysis to drive the relationships between the characteristics slip values (S_{1s}, S_{2s}, and S_{3s}) and L_s. It was observed that the experimental characteristic slip value, S_{3s}, increases as the bonded length increases. This is because the slippage increases with the increase of the ultimate load which increases with increasing bonded length. They also concluded that the mechanical interlocking resistance (τ_{cs}) is ultimately dependent on the bonded length of strand with concrete.

Aly et al. modified CEB FIB 1990 stress-slip relationship to provide a reasonable prediction for the bond behavior between concrete and strand with H-anchorage dead end so that it can predict the minimum failure load and the minimum bond strength in concrete-strand systems. The equations for each stage are shown in Equation 6.14 to Equation 6.23.

$S_{1s} = 1.91 + 5.4 \times 10^{-3} L_s$	Equation 6.73
$S_{2s} = 3.8 + 5.3 \times 10^{-3} L_s$	Equation 6.74
$S_{3s} = 2.55 + 18 \times 10^{-3} L_s$	Equation 6.75

- $S_{4s} = S_{3s} + 5.91$ Equation 6.76
- $\tau_{s} = \tau_{cs} \left(\frac{s}{S_{1s}}\right)^{0.7}, 0 \le S \le S_{1s}$ Equation 6.77 $\tau_{cs} = \left(\frac{450}{L_{s}}\right) \sqrt{f_{c}} \left(\frac{1}{L_{s}}\right)^{0.05}$ Equation 6.78

$$\tau_s = \tau_{cs}$$
, $S_{1s} \le S \le S_{2s}$ Equation 6.79

$$\tau_{max,s} = \tau_{cs} + (H - anchorage \ capacity) \ , S_{2s} \le S \le S_{3s}$$
 Equation 6.80

$$\tau_{s} = \tau_{fs} - (\tau_{max,s} - \tau_{fs}) \left(\frac{S_{4s} - S}{S_{4s} - S_{3s}}\right), S_{3s} < s \le S_{4s}$$
 Equation 6.81

$$\tau_{fs} = \tau_{max,s} - 2.86 Mpa$$
 Equation 6.82

Where:

s, s_1, s_2, s_3, s_4 = characteristic slippage values at point 1, 2, 3, 4, respectively (mm)

 L_s = straight bonded length of the strand (mm)

 τ_s = bond stress at slippage (S) (MPa)

 τ_{cs} = mechanical interlocking resistance (MPa)

 f_c = concrete cube compressive strength (MPa)

 $\tau_{max,s}$ = maximum bond stress capacity (MPa)

 τ_{fs} = stress at failure (MPa)

The characteristic slippage values at Points 1, 2, and 3, Equation 6.14 to Equation 6.16, and the mechanical interlocking resistance, Equation 6.19, proposed by Aly et al. [75], depend on the straight bonded length of the strand (the bonded length without the anchorage length). In the case the prestressed strands without anchorage, the maximum bond stress capacity corresponds to the mechanical interlocking resistance, which is in accordance with the CEB-FIP 1990.

In this study, more than thirty FEM numerical models were created with different slippage values and bond stress parameters until convergence was found between the numerical and experimental results. The proposed bond-slip relationship for 7-wire, $\frac{1}{2}$ " -diameter special strands was based on the CEB-FIB 1990 and modified so that it can predict the maximum capacity of the pile-to-cap connection.

The initial values for slippage (s_1 , s_2 , and s_3) and maximum bond strength τ_{max} were based on the experimental results by Aly et al. [75] and modified until a good correlation between the numerical and experimental results was obtained. The bond strength at s_1 , s_2 , s_3 , was found using Equation 6.10 to Equation 6.13 and stress at failure was set to 80% of the maximum bond strength. The parameters for Modified Bond Model 1 are shown in Table 6.10

Parameter	ModifiedBondModel1
S ₁ (unit length)	4
S ₂ (unit length)	5
S ₃ (unit length)	7
α	0.2
τ_{max} (MPa)	10.5
$ au_{\mathrm{f}}(\mathrm{MPa})$	8.4

Table 6.10: Modified Bond Model 1 parameters

The Modified Bond Model 1 was applied to the 18-inch specimens without axial load application or interface reinforcement. Results are shown in Table 6.11, and moment versus displacement curves plotted in Figure 6.17.

Table 6.11: Summary of results for 18-inch specimens with Modified Bond Model 1

Spec.	Experim ental		Numerical		
	Failure Load (kips)	Max. moment (kip-ft)	Failure Load (kips)	Max. moment (kip-ft)	Meas./ Est.
SP-01	9.5	114.1	7.76	93.15	1.225
SP-04	13.6	122.8	14.40	126.23	0.973
SP-06	17.7	159.4	17.56	158.03	1.009
SP-07	33.6	201.4	41.32	247.96	0.812
SP-08	44.6	267.6	52.13	312.8	0.855

The average measured-to-estimated moment capacity ratio for specimens SP-01, SP-04, and SP-06 with Modified Bond Model 1 is 1.069, and for specimen SP-07, and SP-08 is 0.8335. For specimens with shallow embedment length (6-inch, 9-inch, and 12-inch), the Modified Bond Model 1 predicted the behavior of the pile-to-cap connection very well but overestimated the capacity of the connection for the deeper embedment length (18-inch, and 27-inch).



Figure 6.17: Moment-displacement results for 18-inch specimens with Modified Bond Model 1.

More iterations for the bond-slip relationship in the strands were performed and a second bondslip model was defined. The values for s_1 and s_2 were kept constant; slippage value s_3 was increased; and the bond strength was reduced to 8.5 MPa. The stress at failure was kept to 80% of the maximum bond strength. The parameters for Modified Bond Model 2 are shown in Table 6.12.

Parameter	ModifiedBondModel2
S ₁ (unit length)	4
S ₂ (unit length)	5
S ₃ (unit length)	8
α	0.3
τ_{max} (MPa)	8.5
$\tau_{\rm f}({\rm MPa})$	6.8

Table 6.12: Modified Bond Model 2 parameters

The Modified Bond Model 2 was applied to the 18-inch specimens without axial load application or interface reinforcement. The results are shown in Table 6.13, and moment versus displacement curves plotted in Figure 6.18.

Table 6.13: Summary of results for 18-inch specimens with Modified Bond Model 2

Spec.	Experim ental		Numerical		
	Failure Load (kips)	Max. moment (kip-ft)	Failure Load (kips)	Max. moment (kip-ft)	Meas./ Est.
SP-01	9.5	114.1	5.68	68.27	1.671
SP-04	13.6	122.8	10.72	96.52	1.272
SP-06	17.7	159.4	15.16	136.47	1.168
SP-07	33.6	201.4	36.23	215.75	0.933
SP-08	44.6	267.6	47.01	274.43	0.975

The average measured-to-estimated moment capacity ratio for specimens SP-01, SP-04, and SP-06 with Modified Bond Model 2 is 1.373, and for specimen SP-07, and SP-08 is 0.954. Modified Bond Model 2 with a lower bond strength in the strands had a better estimate of the pile-to-cap capacity on the specimens with deeper embedment length (18-inch, and 27-inch), but underestimated the behavior of the connection for specimens with shallow embedment (6-inch, 9-inch, and 12-inch).



Figure 6.18: Moment-displacement results for 18-inch specimens with Modified Bond Model 2.

Two bond-slip models were defined in the numerical analysis depending on the embedment length of the strands. Modified Bond Model 1 was defined for specimens with shallow embedment (SP-01, SP-04, and SP-07), and Modified Bond Model 2 for specimens with deeper embedment (SP-07 and SP-08). These two models provided a reasonable prediction for the bond behavior between concrete and strands in the pile-to-cap connection. Models are shown in Figure 6.19. It was observed that the bond strength and slippage value s3 is dependent on the embedment length. The

bond strength decreased with deeper embedment lengths and increased as the embedment length decreased.



Figure 6.19: Modified Bond Model 1 and Modified Bond Model 2 for bond-slip relationship of strands.

6.2.2 Crack Pattern and Failure Modes

A realistic visualization of the crack pattern during different stages of the nonlinear analyses was obtained.

In the experimental program a strand development failure was observed in all the 18-inch specimens with a large crack at the pile-to-cap interface. The numerical analysis of SP-01 captured this failure mechanism, as shown in Figure 6.20 (b). Specimens with deeper embedment lengths, SP-07 and SP-08, developed additional flexural cracks along the length of the pile. The crack pattern obtained in the numerical model for SP-08 is shown in Figure 6.21 (b).

SP-10 failed due to punching shear where wide shear cracks developed from the edge of the pile to the top of the pile cap with an inclination angle of approximately 45 degrees. A similar pattern was obtained in the numerical analyses for this specimen, as shown in Figure 6.22 (b).

The nonlinear FE analyses showed strong agreements of the overall moment deflection curves and failure modes of the pile-to-cap specimens, validating the experimental results.



Figure 6.20: Cracking pattern SP-01: (a) failure mechanism; (b) numerical model.



Figure 6.21: Cracking patterns SP-08: (a) failure mechanism; (b) numerical model.



Figure 6.22: Cracking pattern SP-10: (a) failure mechanism; (b) numerical model.

6.3 ADDITIONAL NUMERICAL ANALYSIS

After validating the FE numerical analyses with the experimental results, additional numerical models were created to study the impact of variables not tested experimentally.

6.3.1 Embedment Length

For the 18-inch specimens, embedment lengths between 0.33 and 1.5 the pile depth were experimentally tested. The 18-inch specimen with the deeper embedment length, SP-08 with 27-inch embedment, developed a moment of 81% the capacity of the pile.

The estimated transfer and development length were found using AASHTO LRFD BDS [3] and ElBatanouny and Ziehl [4]. A summary of the required transfer and development length for the 18-inch specimens is shown in Table 6.14. A pile embedment length of 41.4 inches for the 18-inch piles would be required for full moment capacity using ElBatanouny and Ziehl and, 72.1 inches using AASHTO LRFD BDS.

Specimen	Description	AASHTO LRFD BDS		ElBatanouny	and Ziehl
Pile Size	Strand diameter (in)	Transfer length, <i>lt</i> (in)	Development length, <i>l_d</i> (in)	Transfer length, <i>l</i> t (in)	Development length, <i>l_d</i> (in)
18-inch	0.52	31.2	72.1	18.4	41.4

Table 6.14: Estimated development and transfer length for 18-inch piles

A numerical model with an embedment length of 42 inches (EMB-42) was created for the 18-inch specimens, as recommended by ElBatanouny and Ziehl [4]. The maximum moment developed by specimens with embedment lengths between 0.33 and 2.5 the depth of the pile is shown in Figure 6.23. The numerical results aligned well with the predicted moment capacity recommended by ElBatanouny and Ziehl. Specimen EMB-42 did not reach the full moment capacity of the 18-inch piles with a maximum moment of 304.4 kip-ft.



Figure 6.23: Relationship between moment capacity and embedment length for 18-inch specimens.

The cracking pattern of EMB-42 is shown in Figure 6.24. Cracks on the shape of punching shear cone developed in the pile cap. The smaller capacity developed by EMB-42 was likely due to punching shear occurring before the slipping of the strands occurred.



Figure 6.24: Crack pattern of EMB-42.

A punching shear reinforcement bar proposed by Aaleti and Sritharan [76] was included in the numerical model as shown in Figure 6.25. Two #6 bars were added around the embedded pile close to the pile-to-cap interface to improve the punching shear capacity of the specimen and prevent punching shear failure from happening.



Figure 6.25: Rebar detail recommendation for punching shear.

Moment displacement curves for the numerical models with and without additional shear reinforcement around the embedded piles are shown in Figure 6.26 (a). Including the U shape #6 bar around the embedded pile increased the demand of the connection. The moment displacement response for EMB-42 with the additional reinforcement, is what would be expected for a flexure failure.



Figure 6.26: Numerical results for EMB-42 with additional shear reinforcement.

EMB-42 with additional shear reinforcement, developed a moment of 322.3 kip-ft, reaching the full moment capacity of the 18-inch piles, as shown in Figure 6.27. The reinforcement detail proposed by Aaleti and Sritharan [76] increased the capacity of the pile-to-cap connection and prevented a punching shear failure from developing.



Figure 6.27: Relationship between moment capacity and embedment length for 18-inch specimens. Results for EMB-42 include additional shear reinforcement around embedded piles .

6.3.2 Strand Diameter

The second variable studied in the numerical program was the strand diameter. A typical strand diameter of 0.6-inch was selected. The strand pattern for 18-inch piles with 0.6-inch strands is similar as the pattern for 0.5-inch strands, as shown in Figure 6.28.



Figure 6.28: FDOT Standard Plans for piles: (a) 18-inch pile cross section; (b) alternate strand patterns.

The capacity of the 18-inch piles with a strand pattern of 12-0.6-inch strands was determined using RESPONSE2000. The capacity was found to be 402.2 kip-ft with the moment versus curvature response shown in Figure 6.29.



Figure 6.29: Estimated moment versus curvature for 18-inch piles with 0.6-inch strands using RESPONSE2000.

The transfer and development length proposed by ElBatanouny and Ziehl [4] and specified by AASHTO LRFD BDS [3] for 18-inch piles with 0.6-inch strands is shown in Table 6.15. Prestress losses estimates were found using AASHTO LRFD Bridge Design Specification (§5.9.3). A pile embedment length of 55.7 inches for the 18-inch piles with 0.6-inch strands would be required for full moment capacity using ElBatanouny and Ziehl, and 98.02 inches using AASHTO LRFD BDS. Increasing the diameter of the strands, increased the embedment length required to develop the full moment capacity of the pile.

Specimen	Description	AASHTO LRFD BDS		ElBatanouny	and Ziehl
Pile Size	Strand diameter (in)	Transfer length, <i>l_t</i> (in)	Development length, l_d (in)	Transfer length, <i>l_t</i> (in)	Development length, l_d (in)
18-inch	0.6	36.0	98.02	16.2	55.7

Table 6.15: Estimated development and transfer length for 18-inch piles with 0.6-inch strands

The slipping strand stress was found using AASHTO LRFD BDS [3] and ElBatanouny and Ziehl [4] and used to find the corresponding maximum moment with RESPONSE2000. The slipping stress and maximum moments for the 18-inch piles with 0.6-inch strand pattern are summarized in Table 6.16

Embedment	bedment AASHTO LRFD BDS		ElBatanouny	and Ziehl
	Slipping stress (ksi)	Maximum Moment (kip-ft)	Slipping stress (ksi)	Maximum Moment (kip-ft)
6	22.5	42.8	50.0	92.4
9	33.7	62.8	75.0	136.7
12	44.9	83.3	100.0	179.5
18	67.4	123.3	140.2	243.1
27	101.0	181.2	167.2	282.9
36	134.7	234.7	194.2	320.0
42	146.2	252.1	212.2	343.8
56	172.9	291.1	254.2	398

Table 6.16: Maximum moment and slipping stress for 0.6" strands.

The stress in the pile strands versus available development length are plotted in Figure 6.30. The estimated development length found using ElBatanouny and Ziehl [4] proposed equations are much less than the estimated development length found using AASHTO LRFD BDS [3], for the 0.6-inch strands.



Figure 6.30: Stress in strand versus available development length plots for 0.6-inch strand pattern.

A comparison between the stress in strands with different strand patterns (0.5-inch special and 0.6inch) is shown in Figure 6.31. Increasing the diameter of the prestressing strands, increased the required pile embedment length to develop the full moment capacity of the pile. Similar to the initial recommendation based on the experimental testing for the 0.5-inch special strands, it is recommended to determine the embedment length using ElBatanouny and Ziehl [4] where the punching shear capacity does not control.



Figure 6.31: Stress in strand versus available development length plots using: (a) AASHTO LRFD BDS; (b) ElBatanouny and Ziehl [4].

6.3.3 Pile Cap Concrete Strength

In the experimental testing, a punching shear of the edge of the pile cap was observed in SP-10. This specimen had a lower concrete strength in the cap than in the pile, which decreased the punching shear capacity. Such concrete strength disparity is more representative of field conditions where the piles would likely be made with higher strength concrete than the pile caps.

To investigate further the effect of concrete strength on the development of punching shear failure, additional numerical models were created for the 18-inch specimens without interface reinforcement and axial load application, with a lower concrete strength of 5.5 ksi. The Model PC-01 has the same embedment length and properties as SP-01, but with a Pile Cap concrete strength of 5.5 ksi instead of 12 ksi. Similar approach was considered for specimens with different embedment length. A summary of the results is shown in Table 6.17. Moment displacement curves are plotted in Figure 6.32.

Model	Embedment (in)	Pile cap f'c	12,000 psi	Pile cap f'c	5,000 psi	Percentage reduction
		Failure Load (kips)	Max. moment (kip-ft)	Failure Load (kips)	Max. moment (kip-ft)	strength (%)
PC-01	6	9.5	114.1	5.87	70.47	38.2
PC-04	9	13.6	122.8	13.18	118.65	3.3
PC-06	12	17.7	159.4	15.53	139.8	12.3
PC-07	18	33.6	201.4	30.16	180.9	10.2
PC-08	27	44.6	267.6	39.76	238.76	10.7

Table 6.17: Summary of results for 18-inch models with lower concrete strength

All the models with a pile cap concrete strength of 5.5 ksi developed lower moment capacity than the specimens with concrete strength of 12 ksi. The sudden failure in the moment versus displacement plots for the specimens with lower pile cap strength was likely due the punching shear controlling the failure of the pile-to-cap connection before slipping of the strands occurred.



Figure 6.32: Moment versus displacement curves for 18-inch models with different pile cap concrete strength.

The failure mechanism for all models analyzed for reduced concrete strength showed development of crack pattern consistent with punching shear failure. A comparison between the crack pattern of SP-04 and PC-04 is shown in Figure 6.33. The crack pattern at maximum load of SP-04 (9-inch embedment length and 12 ksi pile cap concrete strength) developed cracks on the compression zone of the piles which suggests a flexure failure of the piles, as shown in Figure 6.33 (a). The crack pattern at maximum load of PC-04 (9-inch embedment length and 5.5 ksi pile cap concrete strength), developed cracks consistent with punching shear, as shown in Figure 6.33 (b).



Figure 6.33: Crack pattern of specimen with 9-inch embedment length: (a) SP-04 with pile cap concrete strength 12 ksi; (b) PC-04 with pile cap concrete strength 5.5 ksi.

A sequence of the crack pattern of PC-08 is shown in Figure 6.34. The failure started with the development of cracks perpendicular to the piles, Figure 4.12 (a). At maximum load the cracks propagated towards the top of the pile cap, Figure 4.12 (b). Finally failure of the pile cap occurred with minimum damage to the piles, Figure 4.12 (c). This type of failure with cracks propagating towards the top of the pile cap is similar to the crack pattern in the experimental testing of SP-10.



Figure 6.34: PC-08 failure mechanism: (a) before reaching maximum load; (b) at maximum load; (c) after reaching maximum load.

The shear reinforcement detail from Aaleti and Sritharan [76] was added to PC-08 around the embedded piles to increase the shear capacity of the pile-to-cap connection and to prevent the punching shear failure. Moment-curvature response for PC-08 with and without additional shear

reinforcement is shown in Figure 6.35 (a). The capacity of the pile-to-cap connection increased with the additional shear reinforcement around the embedded piles.



Figure 6.35: Numerical results for PC-08 with additional shear reinforcement: (a) moment-curvature response; (b) crack pattern.

Additional numerical models for specimens with lower pile cap concrete strength showed a reduction in the moment capacity of the pile-to-cap connection between 3% and 38%, depending on the embedment length. This reduction in capacity is mostly due to a punching shear of the edge of the pile cap occurring before the slipping of the strands. Lower pile cap or footing concrete strengths are more representative of field conditions where the piles would likely have higher concrete strength than the pile caps. To control the punching shear failure, additional shear reinforcement was included in the numerical analysis. The additional reinforcement increased the punching shear capacity of the pile cap and increased the capacity of the connection by approximately 10%. More importantly, as shown in Fig. 4.13, adding shear reinforcement increased the ductility of the pile to footing connection.

Chapter 7: Summary of Observations

Results from the computational analysis and experimental testing were used to develop a modification to current equation(s) and a method for predicting the level of moment transfer for various embedment lengths. Design guidance was developed based on the conclusions of the research efforts.

A total of 10 specimens were tested experimentally. A summary of results is presented in §4.9.5. The ultimate strength testing was performed at the FDOT SRC. All specimens experienced a ductile failure mechanism, where a significant deflection after the maximum load was reached. All 18-inch pile specimens held a load close to the ultimate capacity while additional deflection was observed. The 30-inch specimens experienced a drop in capacity immediately after the ultimate load was reached. A strand development failure was observed in the 18-inch specimens and the shallower 30-inch embedment. A punching shear failure was observed in the deeper embedment of the 30-inch specimens.

Design recommendations will be presented in the following sections for the design of pile embedded in cast-in-place pile caps or footings.

7.1 PARTIAL MOMENT RESISTANCE

7.1.1 Modified Strand Development Equation

Based on the experimental results and numerical modeling, a modification to the strand development equation by AASHTO LRFD BDS is proposed in this study for calculating the partial moment resistance in piles embedded in pile caps or footings. The proposed modified development length equation which considers the confining stresses and clamping forces that develop around the embedded portion of the pile is shown in Equation 7.1.

Required development length:
AASHTO LRFD MODIFIED
$$l_d \ge \kappa_p \left(f_{ps} - \frac{2}{3} f_{pe} \right) d_b$$
 Equation 7.83

where:

 d_b = nominal strand diameter (in)

 f_{ps} = average stress in prestressing steel at the time for which the nominal resistance of the member is required (ksi)

 f_{pe} = effective stress in the prestressing steel after losses (ksi)

 $\kappa_p = 0.6$ when finding strand development length in piles embedded into cast-in-place pile caps; included to account for confining stresses.

A trilinear relationship is assumed in AASHTO LRFD BDS [3] for determining the stress in strands when the available development length is less than the required development length. The stress in the prestressing strand varies linearly from 0 ksi at the point where bonding starts to the effective stress after losses, f_{pe} , at the end of the transfer length, l_t . Between the end of the transfer length and the development length, l_d , the strand stress is assumed to increase linearly, reaching the stress at nominal resistance, f_{ps} , at the development length. The idealized relationship between steel stress and distance from the free end of strand per AASHTO LRFD BDS is shown in Figure 5.72.

The stress in the pile strands versus the available development length for the 18-inch and 30-inch piles measured through the experimental testing is plotted with the strand stress estimation equations from AASHTO LRFD BDS and the proposed AASHTO modification in Figure 7.1. The

results generally align well with the estimated strand stress found using AASHTO Modified (Equation 7.1).

The AASHTO Modified equations suggest that for the 18-inch and 30-inch pile-to-cap specimens with $\frac{1}{2}$ " (special) strand pattern a development length of 43 inches would be required to fully developed the strands.



Figure 7.1: Stress in strand versus available development length plot for: (a) 18-inch piles; (b) 30-inch piles.

7.1.2 Moment Capacity and Pile Embedment Length

The calculated strand stress using AASHTO Modified equations, was used to find the corresponding maximum moment capacity at different embedment lengths by using RESPONSE2000. Results are plotted in Figure 7.2. The experimental results for the pile moment capacity for the 18-inch and 30-inch specimens with ¹/₂" (special) strand configuration is included in Figure 7.2. The experimental results for the 18-inch and so-inch specimens with ¹/₂" (special) strand configuration is included in Figure 7.2. The experimental results for the 18-inch specimens align well with the moment capacity found using the AASHTO Modified equations. The moment capacity for SP-10 is not included in the analysis, since SP-10 failed due to punching shear of the edge of the pile cap, which is not captured by the development length calculations.



Figure 7.2: Pile moment capacity versus embedment length using AASHTO Modified for (a) 18-inch piles with 1/2" (special) strands (b) 30-inch piles with 1/2" (special) strands.

The trilinear relationship between stress in strands and available development length can be developed for any pile size and strand configuration considering four important points:

- 0 ksi stress in the strands, at 0 inches embedment length
- Effective stress after losses (f_{pe}) , at transfer length (l_t)
- Stress at nominal resistance (f_{ps}) , at development length (l_d)
- Stress at nominal resistance (f_{ps}) , at any embedment greater than development length

Assuming that the moment versus embedment length curve has the same shape, a relationship was found for different pile sizes and strand configurations. Three different square pile sizes and three strand configurations were selected based on common practice by FDOT [5]. Stress in strands and moment developed at different embedment length for the 18-inch, 24-inch, and 30-inch piles are shown in Table 7.1 to Table 7.9.

18-inch piles:

- 12-0.6" strand, Grade 270 LRS at 35 kips
- 12- ¹/₂" (special) strands, Grade 270 at 34 kips
- 16- ¹/₂" strands, Grade 270 LRS at 26 kips

24-inch piles:

- 16- 0.6" strand, Grade 270 LRS at 44 kips
- 20- ¹/₂" (special) strands, Grade 270 LRS at 34 kips
- 24- ¹/₂" strands, Grade 270 at 31 kips

30-inch piles:

- 20- 0.6" strands, Grade 270 at 41 kips
- 24- ¹/₂" (special) strands, Grade 270 LRS at 34 kips

- 28- ¹/₂" strands, Grade 270 at 29 kips

Embedment Length (in)	Stress in Strands (ksi)	Maximum moment (kip-ft)	% Moment Resistance
12	113.7	151.6	46.5
18.72 (<i>l</i> _{tr})	177.4	236.5	72.6
24	194.5	255.7	78.5
36	233.4	299.4	91.9
43.24 (<i>l</i> _d)	256.9	325.8	100
48	256.9	325.8	100

Table 7.1: Percentage of moment resistance for 18-inch specimens with $\frac{1}{2}$ " special strands

Table 7.2: Percentage of moment resistance for 18-inch specimens with ¹/₂" strands

Embedment Length (in)	Stress in Strands (ksi)	Maximum moment (kip-ft)	% Moment Resistance
12	95.7	157.2	40.9
18 (<i>l</i> _{tr})	143.5	235.7	61.3
24	166.0	265.9	69.1
36	210.9	326.4	84.9
45.5 (<i>l</i> _d)	254.1	384.6	100
$\geq l_d$	254.1	384.6	100

Table 7.3: Percentage of moment resistance for 18-inch specimens with 0.6" strands

Embedment Length (in)	Stress in Strands (ksi)	Maximum moment (kip-ft)	% Moment Resistance
12	74.84	130.6	32.4
21.6 (<i>l</i> _{tr})	134.7	235.2	58.4
24	142.4	246.0	61.1
36	180.6	300.0	74.5
58.8 (l_d)	253.2	402.6	100
$\geq l_d$	253.2	402.6	100

Embedment Length (in)	Stress in Strands (ksi)	Maximum moment (kip-ft)	% Moment Resistance
12	114.3	342.0	45.9
18.72 (l_{tr})	178.4	533.5	71.6
24	195.4	578.3	77.7
36	234.1	680.3	91.3
43.57 (<i>l</i> _d)	258.6	744.6	100
$\geq l_d$	258.6	744.6	100

Table 7.4: Percentage of moment resistance for 24-inch specimens with $\frac{1}{2}$ " special strands

Table 7.5: Percentage of moment resistance for 24-inch specimens with ¹/₂" strands

Embedment Length (in)	Stress in Strands (ksi)	Maximum moment (kip-ft)	% Moment Resistance
12	117.3	382.7	47.6
18 (<i>l</i> _{tr})	176.0	574.0	71.4
24	196.4	631.4	78.5
36	237.0	746.2	92.8
42 (<i>l</i> _d)	257.5	804.0	100
$\geq l_d$	257.5	804.0	100

Table 7.6: Percentage of moment resistance for 24-inch specimens with 0.6" strands

Embedment Length (in)	Stress in Strands (ksi)	Maximum moment (kip-ft)	% Moment Resistance
12	98.3	305.2	39.7
21.6 (<i>l</i> _{tr})	177.0	549.3	71.4
24	183.8	567.6	73.8
36	217.5	658.9	85.7
50.4 (<i>l</i> _d)	258.2	768.9	100
$\geq l_d$	258.2	768.9	100

Embedment Length (in)	Stress in Strands (ksi)	Maximum moment (kip-ft)	% Moment Resistance
12	116.5	556.7	46.9
18.7 (l_{tr})	181.7	868.5	73.1
24	198.6	936.6	78.8
36	236.7	1091.4	91.9
43.5 (<i>l</i> _d)	260.6	1188.0	100
$\geq l_d$	260.6	1188.0	100

Table 7.7: Percentage of moment resistance for 30-inch specimens with $\frac{1}{2}$ " special strands

Table 7.8: Percentage of moment resistance for 30-inch specimens with 1/2" strands

Embedment Length (in)	Stress in Strands (ksi)	Maximum moment (kip-ft)	% Moment Resistance
12	111.8	551.2	44.2
18 (<i>l</i> _{tr})	167.8	826.8	66.3
24	188.7	922.2	73.9
36	230.5	1113.0	89.2
44 (l_d)	259.9	1247.0	100
$\geq l_d$	259.9	1247.0	100

Table 7.9: Percentage of moment resistance for 30-inch specimens with 0.6" strands

Embedment Length (in)	Stress in Strands (ksi)	Maximum moment (kip-ft)	% Moment Resistance
12	92.8	461.6	36.8
21.6 (<i>l</i> _{tr})	167.1	831.0	66.2
24	174.1	862.9	68.8
36	209.0	1022.3	81.5
53.4 (l_d)	259.8	1254.0	100
$\geq l_d$	259.8	1254.0	100

7.1.3 Recommendation for Fixed Connection

The typical objective for a fixed connection between the pile and pile cap is to provide a connection capable of developing the full moment capacity of the pile. To ensure that the pile-to-cap connection reaches the maximum capacity, the pile should be embedded to a sufficient depth in order for the strands to fully developed its maximum stress.

AASHTO Modified (Equation 7.1) calculates the required development length for the strands, which corresponds to the embeddment length in the case of piles embedded in pile cap or footings, considering the clamping forces and confining stresses provided to the embedded portion of the pile.

The capacity of the pile-to-cap connection seems to be independent on the pile size but depended on the strand pattern. The moment resistance of the connection for different embedment lengths and different strand patterns can be found using Figure 7.6.

7.1.4 Rotational Stiffness

For computational and modeling purposes, it is quite beneficial and perhaps necessary to have an estimate of elastic bending stiffness of the pile to footing connection. This can be translated to an estimate of level of fixity at the pile-to-footing connection according to various embedment lengths. The rotational stiffness was calculated for different embedment lengths in the elastic region from the rotation vs. moment curves from the experimental results for the 18-inch specimens.

The moment versus rotation plot for the 18-inch pile specimen with an embedment length of 6 inches is shown in Figure 7.7. As shown, the rotational stiffness was determined based on two points along the elastic response line.



Figure 7.3: Moment versus rotation plot for 18-inch pile with 6 inches embedment length.

The same procedure was developed for specimens without axial load and interface reinforcement. The results are shown in Table 7.10.

Specimen	Embedment length (in)	Failure Load (kips)	Moment developed (kip-ft)	Rotational stiffness (kip-ft/deg)
SP-01	6.0	9.5	114.12	498.115
SP-04	9.0	13.6	122.8	1059.728
SP-06	12.0	17.7	159.4	752.5341
SP-07	18.0	33.6	201.4	1061.846
SP-08	27.0	44.6	267.6	2296.827
SP-09	12.0	63.84	574.6	3856.28
SP-10	30.0	96.45	868.1	8578.94

Table 7.10: Rotational stiffness for specimens without axial load nor interface reinforcement

Rotational stiffness versus embedment length results for 18-inch and 30-inch specimens are shown in Figure 7.8. A tendency for a linear relationship between rotational stiffness and embedment length can be seen in the results. This linear relationship was used to calculate the rotational stiffness for an embedment length of 43-inches, that corresponds to a full moment capacity of the 18-inch and 30-inch specimens. At pile capacity the rotational stiffness for the 18-inch piles is 3,607 kip-ft/rad, and for the 30-inch piles 11,989 kip-ft/rad.



Figure 7.4: Linear relationship between rotational stiffness versus embedment length: (a) 18-inch piles, (b) 30-inch piles.

7.2 SERVICEABILITY LIMIT

During the experimental testing, the specimen was visually inspected at each load step for any cracks. The load at first cracking was recorded. The percentage of pile capacity at first cracking is shown in Table 7.11.

Specimen	Embedment length (in)	Failure Load (kips)	Moment developed (kip-ft)	Moment at first cracking (kip-ft)	Percentage of pile capacity at first cracking (%)
SP-01	6.0	9.5	114.12	72.00	22
SP-02	6.0	40.7	244.59	60.00	18
SP-03	6.0	21.2	190.82	72.00	22
SP-04	9.0	13.6	122.8	85.50	26
SP-05	9.0	41.0	246.19	120.00	36
SP-06	12.0	17.7	159.44	90.00	27
SP-07	18.0	33.6	201.38	120.00	36
SP-08	27.0	44.6	267.59	180.00	54
SP-09	12.0	63.8	574.569	288.00	24
SP-10	30.0	96.5	868.06	810.00	68

Table 7.11: Summary of results for experimental testing

7.3 PUNCHING SHEAR CONTROL

A punching shear failure was observed on specimens with lower concrete strength in the pile cap than in the piles. The different concrete strengths between the pile and the pile cap reflected a field condition between the precast piles and the cast in place pile caps, which likely contributed to the punching shear failure.

Table 7.12: Summary of numerical model res	ults assuming	a strand developmen	t and a punching shear
	failure		

Embedment (in)	Strand development failure	Punching shear failure	Percentage reduction
	Max. moment (kip-ft)	Max. moment (kip-ft)	strength (%)
6	114.1	70.47	38.2
9	122.8	118.65	3.3
12	159.4	139.8	12.3
18	201.4	180.9	10.2
27	267.6	238.76	10.7

As shown in Table 7.12, numerical models for pile-to-cap specimens with lower concrete strength showed a reduction in the moment capacity of the connection and consequently in the punching shear capacity of the cap. Lower concrete strength in the cap, can results in change of failure mode and in moment capacities significantly lower than those estimated by assuming a strand development failure. This capacity reduction can range from 3% to 38% depending on the embedment length. Previous research has suggested the implementation of an additional bar

around the embedded pile to improve the punching shear capacity of the specimen. Aaleti and Sritharan [76] pile cap reinforcement detail is shown in Figure 7.9.



Figure 7.5: Aaleti and Sritharan [76] pile cap reinforcement detail.

A similar configuration was included in the pile-to-cap models with lower concrete strength for pile cap. Two N6 bars were added around the embedded portion of the piles, as close to the pile-to-cap interface as possible. The additional reinforcement for punching shear control is shown in Figure 7.10. Numerical models with the additional reinforcement for punching shear control showed an increase in the capacity of the connection by approximately 10% compared to the models without the shear reinforcement, and an increase of the ductility of the pile to footing connection.



Figure 7.6: Additional reinforcement detail for punching shear control.

The punching shear capacity of the pile cap, estimated in §4.10.2.2 was found considering the amount of transverse reinforcement engaged on the punching shear cone. The additional N6 bar is located within the punching shear crack as shown in Figure 7.11 increasing the shear capacity of the pile cap (V_u) by increasing the shear resistance provided by the steel (V_s).



Figure 7.7: Assumed 45-degree spread for punching shear failure with N6 bar: (a) elevation view of 18inch specimen; (b) plan view of 18-inch specimen.

Chapter 8: Summary and Conclusions

A summary of the observations and conclusions from the experimental testing and numerical study are as follows.

- The average measured transfer length was 26 inches for the 18-inch piles and 14.6 inches for the 30-inch piles. The estimated transfer length for both piles is 31.2 inches based on AASHTO LRFD BDS [3].
- The average prestress losses due to elastic shortening was 7.2 ksi for the 18-inch piles and 5.9 for the 30-inch piles, which were within 2.2% and 8.6% of the estimated elastic shortening losses, respectively.
- The average long-term loss measured for the 18-inch piles was 16.2 ksi (within 13.9% of estimated loss) and 9.8 ksi for the 30-inch piles (40.1% less than estimate).
- Nine of the ten specimens failed due to slipping of the prestressing strand (strand development failure). These specimens had a large failure crack at the location where the strands began to slip, which was near the pile-to-cap interface for specimens without interface reinforcement. The 18-inch specimens all held a load around the maximum capacity of the connection as the strands were slipping and pile rotating. The 30-inch pile cap with strand slipping saw a drop in strength when the strands began to slip.
- A pile embedment length of 72.1 inches for 18-inch piles and 117.0 inches for the 30-inch piles would be required for full moment capacity when using AASHTO LRFD BDS [3]. A pile embedment length of 41.4 inches for 18-inch piles and 42.0 inches for the 30-inch piles would be required for full moment capacity when using equations developed by ElBatanouny and Ziehl [4].
- Using the transfer and development length equations proposed by ElBatanouny and Ziehl [4] to estimate the moment capacity of the specimens that failed due to strand development led to an average measured-to-estimated ratio of 1.07, standard deviation of 0.14, and coefficient of variation of 0.13. Using AASHTO LRFD BDS [3] equation for the same specimens led to an average measured-to-estimated ratio of 1.52, standard deviation of 0.31, and coefficient of variation of 0.20. It is concluded that the moment capacity estimated using AASHTO LRFD BDS is noticeably conservative and that the equations proposed by ElBatanouny and Ziehl provide for a more accurate estimation.
- The failure of SP-10 resembled a punching shear failure where the side of the pile punched through the side face of the pile cap. The demand could be estimated using a compression block developed from Mattock and Gaafar [42] and Belarbi et al. [70] and the measured compressive strain in the face of the pile cap. The capacity could be estimated with a good approximation using standard punching shear equations from AASHTO LRFD BDS §5.12.8.6 [3].
- A small axial compression force greatly increased the capacity of the connection; an average 107% increase in capacity of the connection was observed when $0.05A_g f'_{c,pile}$ axial compression was applied to the pile and connection.
- The specimen with the interface reinforcement (SP-03) developed a moment capacity 67% higher than the similar specimen without interface reinforcement (SP-01), both with 6-inch pile embedment lengths.
- Because the tests needed to be stopped due to stroke limitation of the hydraulic jack, conclusion could not be made on the effect of the presence of interface reinforcement on the rotational capacity of the connection.

- The capacity of the specimen with interface reinforcement (SP-03) was controlled by the available development length at the pile-to-cap interface section (6 inches from the pile end) rather than the section at the end of the interface reinforcement (24 inches from the pile end). For design of connections with interface reinforcement, it is recommended to use the minimum of these two capacities to estimate the strength of the connection.
- The capacity of the connection did not appear to be dependent on the pile embedment length as a function of the pile size when strand development failure is controlling. The behavior of the connection appeared to be more dependent on the available strand development length provided by the pile embedment length.
- The capacity of the connection appears to be dependent on the pile embedment length as a function of the strand configuration.
- A factor of 0.6 is proposed to be applied to the equation for estimating the required development length as an addition to the current AASHTO LRFD BDS development length equation. This factor considers the confining stresses developed around the embedded pile, decreasing the required development length to reach full capacity of the piles in the pile-to-cap connection.
- A pile embedment length of 42 inches for 18-inch piles and 30-inch piles would be required for full moment capacity using the proposed modification to AASHTO LRFD BDS.
- A linear relationship was observed between rotational stiffness and embedment length in 18-inch piles with 1/2" (special) strand configuration.
- Lower concrete strength in the cap resulted in change of failure mode and in moment capacities significantly lower than those estimated by assuming a strand development failure. This capacity reduction range between 3% to 38% depending on the embedment length. This condition can be more prevalent for actual pile to footing connection for which the footing normally uses concrete with strength lower than that in pile.
- An additional N6 bar around the embedded pile is recommended to prevent punching shear failure and therefore allow the connection to reach its full moment capacity.

References

- K. M. Rollins and T. E. Stenlund, *Laterally Loaded Pile Connections* (UDOT Research Report UT-10.16), Salt Lake City, UT: Utah Department of Transportation, 2010.
- [2] M. Issa, Testing of Pile-to-Pile Cap Moment Connection for 30" Prestressed Concrete Pipe-Pile (FDOT Research Report 98-9), Tallahassee, FL: Florida Department of Transportation, 1999.
- [3] American Association of State Highway and Transportation Officials (AASHTO), "AASHTO LRFD Bridge Design Specification, Customary U.S. Units, 8th Edition," Washington, D. C., Sep. 2020.
- [4] M. ElBatanouny and P. Ziehl, "Determining Slipping Stress of Prestressing Strands in Confined Sections," ACI Struct. J., vol. 109, pp. 767–776, Nov. 2012.
- [5] Florida Department of Transportation (FDOT), *Structures Design Guidelines FDOT Structures Manual* Volume 1, Tallahassee, FL: Florida Department of Transportation ,Jan. 2023.
- [6] Minnesota Department of Transportation, *LRFD Bridge Design 10 Foundations*, Oakdale, MN: Minnesota Department of Transportation, Jun. 2007.
- [7] Wisconsin Department of Transportation, *WisDOT Bridge Manual Chapter 11 Foundation Support*, Jan. 2019.
- [8] Oregon Department of Transportation, *Bridge Design Manual*, Salem, OR: Oregon Department of Transportation, May 2018.
- [9] Colorado Department of Transportation, *LRFD Bridge Design Manual*, Denver, CO: Colorado Department of Transportation Jan. 2018.
- [10] Illinois Department of Transportation, *Bridge Manual*, Springfield, IL: Illinois Department of Transportation, 2012.
- [11] New Hampshire Department of Transportation, Bridge Design Manual Chapter 6 Substructure, Concord, NH: New Hampshire Department of Transportation Jan. 2015.
- [12] K. Harries and M. Petrou, "Behavior of Precast, Prestressed Concrete Pile to Cast-in-Place Pile Cap Connections," PCI J., vol. 46, no. 4, 2001.
- [13] A. A. Shama, J. B. Mander, and A. J. Aref, "Seismic Performance and Retrofit of Steel Pile to Concrete Cap Connections," ACI Struct. J., vol. 99, no. 1, pp. 51–61, 2002.
- [14] M. K. ElBatanouny, P. Ziehl, A. Larosche, T. Mays, and J. Caicedo, "Bent-Cap Confining Stress Effect on Slip of Prestressing Strands," ACI Struct. J., vol. 109, no. 4, pp. 487–496.
- [15] C. D. White, R. W. Castrodale, and M. C. Nigels, "Prestressed Concrete Piles" (Chapter 20 of the *Bridge Design Manual*), Precast/Prestressed Concrete Institute (PCI), BM-20-04, 2004.
- [16] Y. Xiao, H. Wu, T. T. Yaprak, G. R. Martin, and J. B. Mander, "Experimental studies on seismic behavior of steel pile-to-pile-cap connections," *J. Bridge Eng.*, vol. 11, no. 2, pp. 151–159, 2006.

- [17] P. H. Joen and R. Park, "Simulated Seismic Load Tests on Prestressed Concrete Piles and Pile-Pile Cap Connections," PCI J., vol. 35, no. 6, pp. 42–61, Dec. 1990.
- [18] A. Larosche, P. Ziehl, M. ElBatanouny, and J. Caicedo, "Plain Pile Embedment for Exterior Bent Cap Connections in Seismic Regions," J. Bridge Eng., vol. 19, no. 4, pp. 1–12, 2014.
- [19] F. Castilla, P. Martin, and J. Link, *Fixity of Members Embedded in Concrete*, (Technical Report M-339), Champaign, IL, U.S. Army Construction Engr Research Laboratory, 1984.
- [20] M. Shahawy and M. Issa, "Effect of Pile Embedment on the Development Length of Prestressing Strands," PCI J., vol. 37, no. 6, pp. 44–59, 1992.
- [21] Alaska Department of Transportation and Public Facilities, *Alaska Bridges and Structures Manual*, Juneau, AK: Alaska Department of Transportation and Public Facilities, 2017.
- [22] State of Connecticut Department of Transportation, *Bridge Design Manual*, CT: State of Connecticut Department of Transportation, Edition (Revised /11 2003.
- [23] Delaware Department of Transportation, *Bridge Design Manual*, DE: Delaware Department of Transportation, 2017.
- [24] Idaho Transportation Department, *Load Resistance Factor Design (LRFD) Bridge Manual*, Boise, ID: Idaho Transportation Department, Section 10.7.1.2, 2008.
- [25] Illinois Tollway, *Structures Design Manual*, Illinois State Toll Highway Authority, Mar. 2018.
- [26] Indiana Department of Transportation, 2013 Design Manual Chapter 408 Foundation, Indianapolis, IN: Indiana Department of Transportation, Aug. 2018.
- [27] Iowa Department of Transportation, *Bridge Design Manual (BDM)*, Methods Unit of the Bridges and Structures Bureau (BSB), Jan. 2019.
- [28] Kansas Department of Transportation, *Bridge Construction Manual* 5.3 Driven Piles, Kansas: Kansas Department of Transportation, May 2013.
- [29] Michigan Department of Transportation, *Michigan Design Manual* Bridge Design Chapter 7 Design Criteria, MI: Michigan Department of Transportation, 2018.
- [30] Montana Department of Transportation, *Montana Structures Manual* Chapter 20 Foundations, Helena, MO: Montana Department of Transportation, Aug. 2002.
- [31] Nevada Department of Transportation, *Structures Manual* Chapter 17 Foundations, NDOT Structures Division, NV: Nevada Department of Transportation Sep. 2008.
- [32] New York State Department of Transportation, *Bridge Manual*, NY: New York Department of Transportation, 2017.
- [33] Ohio Department of Transportation, *Bridge Design Manual* Section 303.3.3 Footing on Piles, OH: Ohio Department of Transportation, Jan. 2004.
- [34] Pennsylvania Department of Transportation, *Design Manual* Part 4 Structures Procedures - Design - Plans Presentation, PA: Pennsylvania Department of Transportation, Apr. 2015.
- [35] State of Rhode Island Department of Transportation, *Rhode Island LRFD Bridge Design Manual*, RI: State of Rhode Island Department of Transportation, 2007.

- [36] South Carolina Department of Transportation, *SCDOT Bridge Design Manual*, SC: South Carolina Department of Transportation, Jun. 2006.
- [37] Vermont Agency of Transportation, *VTrans Structures Design Manual*, VT: Vermont Agency of Transportation, Section 2010.
- [38] West Virginia Department of Transportation, *Bridge Design Manual*, WV: West Virginia Department of Transportation, Mar. 2016.
- [39] P. Zia and T. Mostafa, "Development Length of Prestressing Strands," PCI J., vol. 22, no. 5, pp. 54–65, Oct. 1977.
- [40] M. Shahawy, M. Issa, and M. Polodna, "Development Length of Prestressed Concrete Piles," Florida Department of Transportation (FDOT), SSR-01-90, 1990.
- [41] M. F. Stocker and M. A. Sozen, "Investigation of Prestressed Reinforced Concrete for Highway Bridges - Part VI: Bond Characteristics," 1969.
- [42] A. Mattock and G. H. Gaafar, "Strength of Embedded Steel Sections as Brackets," ACI Struct. J., vol. 79, no. 2, pp. 83–93, 1982.
- [43] K. Marcakis and D. Mitchell, "Precast Concrete Connections with Embedded Steel Members," PCI J., vol. 25, no. 4, pp. 88–116, Aug. 1980.
- [44] A. A. Shama and J. B. Mander, "Behavior of Timber Pile-to-Cap Connections under Cyclic Lateral Loading," J. Bridge Eng., vol. 130, no. 8, pp. 1252–1262, Aug. 2004.
- [45] Y. Xiao, "Experimental Studies on Precast Prestressed Concrete Pile to CIP Concrete Pile-Cap Connections," PCI J., vol. 48, no. 6, pp. 82–91, Dec. 2003.
- [46] J. E. Stephens and L. R. McKittrick, "Performance of Steel Pipe Pile-to-Concrete Bent Cap Connections Subject to Seismic or High Transverse Loading: Phase II," Montana State University - Bozeman, FHWA/MT-05-001/8144, Mar. 2005.
- [47] L. Kappes, M. Berry, and J. E. Stephens, "Performance of Steel Pipe Pile-to-Concrete Cap Connections Subject to Seismic or High Transverse loading: Phase III Confirmation of Connection Performance," FHWA/MT-13-001/8203, Jan. 2013.
- [48] Standards Association of New Zealand, "New Zealand Standard Specification for Concrete Construction, NZS 3109," Wellington, New Zealand, 1980.
- [49] Florida Department of Transportation (FDOT), "Index 20010 Series Prestressed Florida-I Beams," Tallahassee, 2012.
- [50] Florida Department of Transportation (FDOT), "Prestressed Beam v5.2." Nov. 07, 2018. [Online]. Available: https://www.fdot.gov/structures/proglib.shtm
- [51] Florida Department of Transportation (FDOT), "Prestressed Concrete Piles Standard Plans," 455, 2019.
- [52] Florida Department of Transportation (FDOT), "Final Design of Wekiva River Bridges," Feb. 2014.
- [53] Precast/Prestressed Concrete Institute (PCI), "Bridge Design Manual, 3rd Edition, Second Release, August 2014," 2014.

- [54] A. Ahmed, "Straddle Bent Design Using MIDAS CIVIL." MIDAS TUTORIALS, Dec. 06, 2018.
- [55] American Concrete Institute (ACI) Committee 209, "Guide for Modeling and Calculating Shrinkage and Creep in Hardened Concrete (ACI 209.2R-08)," American Concrete Institute (ACI), Farmington Hill, MI, Reapproved 2008.
- [56] "ATENA." Cervenka Consulting s.r.o, Czech Republic, Apr. 08, 2020. [Online]. Available: www.cervenka.cz
- [57] V. Cervenka, J. Cervenka, Z. Janda, and D. Pryl, "ATENA Program Documentation User's Manual for ATENA-GiD Interface," 2017.
- [58] V. Cervenka, L. Jendele, and J. Cervenka, "ATENA Program Documentation Part 1 Theory," 2018.
- [59] D. Garber and M. L. Ralls, "ABC Project Database." Accessed: May 24, 2016. [Online]. Available: http://utcdb.fiu.edu/
- [60] Florida Department of Transportation (FDOT), "Standard Specification for Road and Bridge Construction, FY 2023-24," 2023.
- [61] B. W. Russell and N. H. Burns, "Design Guidelines for Transfer, Development and Debonding of Large Diameter Seven Wire Strands in Pretensioned Concrete Girders," The University of Texas at Austin, Austin, TX, 1993.
- [62] A. Al-Kaimakchi and M. Rambo-Roddenberry, "Measured transfer length of 15.2-mm (0.6in.) duplex high-strength stainless steel strands in pretensioned girders," *Eng. Struct.*, vol. 237, 2021, doi: https://doi.org/10.1016/j.engstruct.2021.112178.
- [63] A. H. Mattock, "Proposed Redraft of Section 2611 Bond of the Proposed Revision of Building Code Requirements for Reinforced Concrete (ACI 318-56)," ACI 323 Corresp., 1962.
- [64] American Concrete Institute (ACI) Committee 318, "Building Code Requirements for Structural Concrete (ACI 318-19) and Commentary," Farmington Hills, MI, 2019.
- [65] Norman W. Hanson and Paul H. Kaar, "Flexural Bond Tests of Pretensioned Prestressed Beams," *ACI J. Proc.*, vol. 55, no. 1, Jan. 1959, doi: 10.14359/11389.
- [66] T. E. Cousins, D. W. Johnston, and P. Zia, "Transfer and Development Length of Epoxy Coated and Uncoated Prestressing Strand," *Pci J.*, vol. 35, pp. 92–103, 1990.
- [67] Federal Highway Administration (FHWA), "A New Development Length Equation for Pretensioned Strands in Bridge Beams and Piles," FHWA, U.S. Department of Transportation, Washington, DC, FHWA-RD-98-116, 1998.
- [68] C. D. Buckner, "A Review of Strand Development Length for Pretensioned Concrete Members," PCI J., vol. 40, no. 2, pp. 84–105, Apr. 1995.
- [69] M. P. Collins and D. Mitchell, *Prestressed Concrete Structures*. Englewood Cliffs, New Jersey: Prentice-Hall, Inc., 1991.
- [70] A. Belarbi et al., NCHRP Research Report 907: Design of Concrete Bridge Beams Prestressed with CFRP Systems. Washington, DC: National Cooperative Highway Research Program (NCHRP), 2019.
- [71] CEB-FIP model code 1990: design code. London: T. Telford, 1993., 1993. [Online]. Available: https://search.library.wisc.edu/catalog/9910085019702121
- [72] A. Bigaj-van Vliet, "Structural Dependence of Rotational Capacity of Plastic Hinges in RC Beams and Slabs," *TU Delft Civ. Eng. Geosci. PhD Diss.*, pp. 1999–09, Sep. 1999.
- [73] J. Khalaf and Z. Huang, "Analysis of the bond behaviour between prestressed strands and concrete in fire," *Constr. Build. Mater.*, vol. 128, pp. 12–23, 2016, doi: https://doi.org/10.1016/j.conbuildmat.2016.10.016.
- [74] P. Mohandoss, R. Pillai, and R. Gettu, "Determining bond strength of seven-wire strands in prestressed concrete," *Structures*, vol. 33, pp. 2413–2423, Oct. 2021, doi: 10.1016/j.istruc.2021.06.004.
- [75] J. H. Aly, A. F. Maree, M. Kohail, and A. H. Khalil, "Modeling of bond stress-slip relationships of mono-prestressing strands with H-anchorage dead end," *Ain Shams Eng. J.*, vol. 14, no. 6, p. 102105, 2023, doi: https://doi.org/10.1016/j.asej.2022.102105.
- [76] S. Aaleti and S. Sritharan, *Experimental and Analytical Investigation of UHPC Pile-to-Abutment Connections*. 2016. doi: 10.21838/uhpc.2016.117.