



CFRP-PC Training Course

Design Example

Square Pile 18''x18''

For Training Purposes Only, NOT To Be Used For Construction

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P-M DIAGRAM OF 18" SQUARE PILE PRESTRESSED WITH 0.6" DIAMETER CFRP STRANDS

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CFRP -PC TRAINING COURSE DESIGN EXAMPLE: 18" SQUARE PILE

1. REFERENCES

LRFD: AASHTO LRFD Bridge Design Specifications, 8th Edition, 2017

AASHTO CFRP: Guide Specifications for the Design of Concrete Bridge Beams
Prestressed with Carbon Fiber-Reinforced Polymer (CFRP) Systems, 1st Edition, 2018

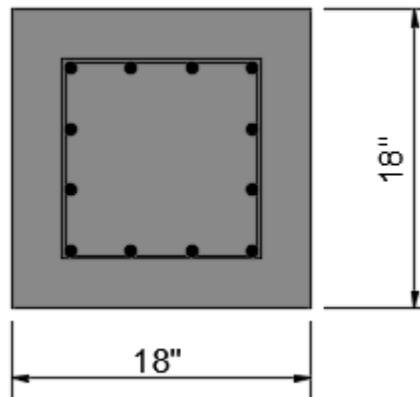
SDG: FDOT Structures Manual, Volume 1 -Structures Design Guidelines

FRPG: FDOT Structures Manual, Volume 4 -Fiber Reinforced Polymer Guidelines

FDOT Standard Plans Index 455-101, 455-118

FRP Pile Standards by Zach Behring (MathCAD)

2. INPUTS



$$kcf = \frac{\text{kip}}{\text{ft}^3}$$

2.1 Geometry

18" X 18" Square pile

hh := 18in

Depth of pile section

bb := 18in

Width of pile section

cham := 0.75in

Chamfer

cover := 3in

Clear cover

(Standard Plans Index 455-101)

$$A_g := bb \cdot hh - 4 \cdot \frac{\text{cham}^2}{2} = 323 \cdot \text{in}^2$$

Gross pile area

$$I_g := \frac{bb \cdot hh^3}{12} = 8.748 \times 10^3 \cdot \text{in}^4$$

Moment of inertia

$$\text{Perimeter} := (bb + hh) \cdot 2 = 72 \cdot \text{in}$$

Perimeter of section

2.2 Concrete

$$w_c := 0.145 \frac{\text{kip}}{\text{ft}^3}$$

Concrete unit weight
(SDG 1.4.1A)

$$f_c := 6\text{ksi}$$

Specified concrete strength
(SDG Table 1.4.3-2)

$$f_{ci} := 4\text{ksi}$$

Concrete strength at transfer
(Standard Plans Index 455-101)

$$K_1 := 1.0$$

Correction factor for aggregate
(SDG 1.4.1A)

$$E_{ci} := 120000 \cdot K_1 \cdot \left(\frac{w_c}{\text{kcf}}\right)^2 \cdot \left(\frac{f_{ci}}{\text{ksi}}\right)^{0.33} \cdot \text{ksi} = 3987 \cdot \text{ksi}$$

Elastic modulus of concrete at transfer
(LRFD 5.4.2.4-1)

$$E_c := 120000 \cdot K_1 \cdot \left(\frac{w_c}{\text{kcf}}\right)^2 \cdot \left(\frac{f_c}{\text{ksi}}\right)^{0.33} \cdot \text{ksi} = 4557 \cdot \text{ksi}$$

Elastic modulus of concrete
(LRFD 5.4.2.4-1)

$$\alpha_1 := \min\left(\max\left(0.85 - 0.02 \cdot \frac{f_c - 10\text{ksi}}{\text{ksi}}, 0.75\right), 0.85\right) = 0.85$$

$$\beta_1 := \min\left(\max\left(0.85 - 0.05 \cdot \frac{f_c - 4\text{ksi}}{\text{ksi}}, 0.65\right), 0.85\right) = 0.75$$

Concrete stress block factor
(LRFD 5.6.2.2)

2.3 Reinforcement

Stirrups

$$D_{\text{stir}} := 0.2\text{in}$$

Diameter of CFRP strand spiral ties
(Standard Plans Index 455-101)

Prestressing strands

[Assume 0.6in diameter CFRP Cable; Properties refer to FDOT Standard Plans Index 455-101 and Specification Section 933 Table 1-2, 7-strand-15.2mm CFRP prestressing strand]

$$\text{StrandType}_{\text{CFRP}} := 1$$

CFRP strand type: 1 for Cable; 2 for Bar

$$n_{\text{p.total}} := 12$$

Total number of tendons

$$D_{\text{p}} := 0.6\text{in}$$

Diameter of CFRP prestressing tendon

$$A_{\text{pf}} := 0.179\text{in}^2$$

Effective cross-sectional area of each tendon

$$A_{\text{p.total}} := n_{\text{p.total}} \cdot A_{\text{pf}} = 2.148 \cdot \text{in}^2$$

Total area of tendons

$$E_{\text{p}} := 22480\text{ksi}$$

Elastic modulus of prestressing tendon

$$P_{\text{u}} := 66.2\text{kip}$$

Ultimate tensile force for each tendon

$$f_{\text{pu}} := \frac{P_{\text{u}}}{A_{\text{pf}}} = 370 \cdot \text{ksi}$$

Ultimate tensile strength

Design tensile strength, f_{pu} , is defined later in "other inputs"

$$C_{\text{E}} := 1$$

Environmental reduction factor
(AASHTO CFRP Table 1.4.1.2-1)

$$f_{\text{pu}} := C_{\text{E}} \cdot f_{\text{pu}} = 370 \cdot \text{ksi}$$

Design tensile strength of CFRP tendon

$$f_{\text{p.limit}} := f_{\text{pu}} = 370 \cdot \text{ksi}$$

$$P_i = 32 \cdot \text{kip}$$

Jacking force, need to satisfy 1) jacking stress limit 2) Standard Plans Index 455-101 requirement
(the value is defined globally later after the prestress loss estimation)

$$f_{pi} := \frac{P_i}{A_{pf}} = 179 \cdot \text{ksi}$$

Jacking stress

$$f_{pi.\text{limit}} := \begin{cases} 0.70 \cdot f_{pu} & \text{if StrandType}_{CFRP} \leq 1 \\ 0.65 \cdot f_{pu} & \text{if } 1 < \text{StrandType}_{CFRP} \leq 2 \end{cases} = 258.9 \cdot \text{ksi}$$

Jacking stress limit

(AASHTO CFRP Table 1.9.1.1)

$$\text{Check}_{f_{pi.\text{limit}}} := \begin{cases} \text{"OK"} & \text{if } f_{pi} \leq f_{pi.\text{limit}} \\ \text{"NOT GOOD"} & \text{if } f_{pi} > f_{pi.\text{limit}} \end{cases} = \text{"OK"}$$

Arrangement of prestressing tendons

$$n_p := \begin{pmatrix} 4 \\ 2 \\ 2 \\ 4 \end{pmatrix}$$

Number of tendons in rows 1, 2, 3, 4

(sum of $n_p = n_p$, total)

$$A_p := n_p \cdot A_{pf} = \begin{pmatrix} 0.716 \\ 0.358 \\ 0.358 \\ 0.716 \end{pmatrix} \cdot \text{in}^2$$

Area of tendons in rows 1, 2, 3, 4

$$d'_{p0} := \left(\text{cover} + \frac{D_p}{2} \right) + D_{\text{stir}} = 3.5 \cdot \text{in}$$

Distance from top of the section to the center of the 1st row tendons

$$d_{ps0} := \frac{hh - 2 \cdot d'_{p0}}{\text{rows}(n_p) - 1} = 3.667 \cdot \text{in}$$

Space of rows

$$d_p := \begin{pmatrix} d'_{p0} \\ d'_{p0} + d_{ps0} \\ d'_{p0} + 2d_{ps0} \\ d'_{p0} + 3d_{ps0} \end{pmatrix} = \begin{pmatrix} 3.500 \\ 7.167 \\ 10.833 \\ 14.500 \end{pmatrix} \cdot \text{in}$$

Distance from top of the section to each tendon



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$$e_{pg} := 0 \cdot \text{in}$$

Eccentricity of prestressing force
(non-composite section)
0 for prestressed piles

$$e_{pc} := 0 \text{ in}$$

Eccentricity of prestressing force with
respect to composite section
0 for prestressed piles
(LRFD 5.9.3.4.3)

2.4 Other Inputs

$$H_{\text{wv}} := 75$$

Ambient relative humidity
(SDG 4.6.6)

$$\Delta f_{pTH} := 0$$

Prestress loss due to temperature
change. Not considered in this example

$$t_i := 1$$

Age at transfer (day)

$$t_d := 120$$

Age at pile installation (day)

$$t_f := 10000$$

final time (day)

3. DETERMINE PRESTRESS LOSSES

$$\Delta f_p = \Delta f_{pES} + \Delta f_{pLT} + \Delta f_{pTH}$$

Total prestress loss
(AASHTO CFRP 1.9.2.1)

Δf_{pES} : prestress loss due to elastic shortening

Δf_{pLT} : long-term time-dependent prestress losses, due to shrinkage, creep, and relaxation

Δf_{pTH} : prestress losses due to temperature change (Not considered in this example)

3.1 Prestress Loss due to Elastic Shortening

$$\Delta f_{pES} = \frac{E_f}{E_{ct}} f_{cgp}$$

Prestress loss due to elastic shortening
(AASHTO CFRP 1.4.2)

Use variables defined in this example,

$$f_{cgp} := \frac{A_{p,total} \cdot f_{pi}}{A_g} = 1.189 \cdot \text{ksi}$$

Concrete stress at gravity center of the
prestressing force at transfer
(c.g. is the center of the cross-section)

$$\Delta f_{pES} := \frac{E_p}{E_{ci}} f_{cgp} = 6.707 \cdot \text{ksi}$$

Prestress loss due to elastic shortening
(AASHTO CFRP 1.4.2)

$$f_{pt} := f_{pi} - \Delta f_{pES} = 172 \cdot \text{ksi}$$

Prestress stress at transfer

3.2 Long-Term Time-Dependent Prestress Losses (Refined Estimation)

$$\Delta f_{pLT} = (\Delta f_{pSR} + \Delta f_{pCR} + \Delta f_{pR1})_{id} + (\Delta f_{pSD} + \Delta f_{pCD} + \Delta f_{pR2} - \Delta f_{pSS})_{df}$$

Total long-term time-dependent losses
id - time between transfer and pile installation
df - time between pile installation and the final time

(LRFD 5.9.3.4.1-1)

-----Time-Dependent losses between transfer and pile installation-----

Shrinkage of pile concrete (i->d)

$$\Delta f_{pSR} = \epsilon_{bid} \cdot E_p \cdot K_{id} \quad \text{(LRFD 5.9.3.4)}$$

$$k_s := \max\left(1.45 - 0.13 \frac{A_g}{\text{Perimeter} \cdot \text{in}}, 1.0\right) = 1.000$$

Factor for the effect of the volume-to-surface ratio of the component
(LRFD 5.4.2.3.2)

$$k_{hs} := 2.00 - 0.014H = 0.950$$

Humidity factor for shrinkage
(LRFD 5.4.2.3.3)

$$k_{hc} := 1.56 - 0.008H = 0.960$$

Humidity factor for creep
(LRFD 5.4.2.3.2)

$$k_f := \frac{5}{1 + \frac{f_{ci}}{\text{ksi}}} = 1.000$$

Factor for the effect of concrete strength
(LRFD 5.4.2.3.2)

$$k_{td}(t_0, t_1) := \frac{t_1 - t_0}{12 \left[\frac{100 - 4 \cdot \frac{f_{ci}}{\text{ksi}}}{\frac{f_{ci}}{\text{ksi}} + 20} \right] + (t_1 - t_0)}$$

Time development factor
(LRFD 5.4.2.3.2)

$$k_{td}(t_i, t_d) = 0.739$$

Time development factor
Time from transfer to pile installation

$$k_{td}(t_i, t_f) = 0.996$$

Time development factor
Time from transfer to final time

$$k_{td}(t_d, t_f) = 0.996$$

Time development factor
Time from pile installation to final time

$$\epsilon_{bid} := k_s \cdot k_{hs} \cdot k_f \cdot k_{td}(t_i, t_d) \cdot 0.48 \cdot 10^{-3} = 3.370 \times 10^{-4}$$

Shrinkage strain of pile concrete
(LRFD 5.4.2.3.3)

$$\Psi_b(t_1, t_0) := 1.9 \cdot k_s \cdot k_{hc} \cdot k_f \cdot k_{td}(t_0, t_1) \cdot t_0^{-0.118}$$

Creep coefficient
(LRFD 5.4.2.3.2)

$$\Psi_b(t_d, t_i) = 1.348$$

Creep coefficient
Time from transfer to installation

$$\Psi_b(t_f, t_i) = 1.816$$

Creep coefficient
Time from transfer to final time

$$\Psi_b(t_f, t_d) = 1.032$$

Creep coefficient
Time from installation to final time

$$K_{id} := \frac{1}{1 + \frac{E_p}{E_{ci}} \cdot \frac{A_{p.total}}{A_g} \cdot \left(1 + \frac{A_g \cdot e_{pg}^2}{I_g}\right) \cdot (1 + 0.7 \cdot \Psi_b(t_d, t_i))} = 0.932$$

Transformed section coefficient
(LRFD 5.9.3.4.2)

$$\Delta f_{pSR} := \epsilon_{bid} \cdot E_p \cdot K_{id} = 7.062 \cdot \text{ksi}$$

Prestress loss due to
Shrinkage of pile concrete
(LRFD 5.9.3.4)

Creep of pile concrete (i->d)

$$\Delta f_{pCR} := \frac{E_p}{E_{ci}} \cdot f_{cgp} \cdot \Psi_b(t_d, t_i) \cdot K_{id} = 8.427 \cdot \text{ksi}$$

Prestress loss due to
Creep of pile concrete
(LRFD 5.9.3.4)

Relaxation of prestressing CFRP (i->d)

$f_{pu} = 370 \cdot \text{ksi}$ Design tensile strength

$f_{pt} = 172 \cdot \text{ksi}$ Prestress stress at transfer

$$\Delta f_{pR}(t_0, t_1) := \begin{cases} \left[\left(0.019 \frac{f_{pt}}{f_{pu}} - 0.0066 \right) \cdot \log[24 \cdot (t_1 - t_0)] \cdot f_{pu} \right] & \text{if StrandType}_{CFRP} \leq 1 \\ \left[\left(0.013 \frac{f_{pt}}{f_{pu}} - 0.006 \right) \cdot \log[24 \cdot (t_1 - t_0)] \cdot f_{pu} \right] & \text{if } 1 < \text{StrandType}_{CFRP} \leq 2 \end{cases}$$

Prestress loss due to relaxation
(AASHTO CFRP 1.9.2.5.2)

$\Delta f_{pR1} := \Delta f_{pR}(t_i, t_d) = 2.863 \cdot \text{ksi}$ Prestress loss due to relaxation
Time from transfer to installation

Total time-depedent prestress loss between transfer and pile installation

$\Delta f_{pLT.id} := \Delta f_{pSR} + \Delta f_{pCR} + \Delta f_{pR1} = 18.351 \cdot \text{ksi}$

-----Time-Dependent losses between pile installation to final time-----

Shrinkage of pile concrete (d->f)

$\Delta f_{pSD} = \epsilon_{bdf} \cdot E_p \cdot K_{df}$ (LRFD 5.9.3.4.3)

$\epsilon_{bdf} := k_s \cdot k_{hs} \cdot k_f \cdot k_{td}(t_d, t_f) \cdot 0.48 \cdot 10^{-3} = 4.541 \times 10^{-4}$ Shrinkage strain of pile concrete
(LRFD 5.4.2.3.3)

$$e_{pc} = 0$$

Eccentricity of prestressing force with respect to composite section
0 for prestressed piles
(LRFD 5.9.3.4.3)

$$I_c := I_g = 8.748 \times 10^3 \cdot \text{in}^4$$

Moment inertia for transformed composite section

$$A_c := A_g = 323 \cdot \text{in}^2$$

Area for transformed composite section

$$K_{df} := \frac{1}{1 + \frac{E_p}{E_{ci}} \cdot \frac{A_{p,\text{total}}}{A_c} \cdot \left(1 + \frac{A_c \cdot e_{pc}^2}{I_c}\right) \cdot (1 + 0.7 \cdot \Psi_b(t_f, t_d))} = 0.939$$

Transformed section coefficient
(LRFD 5.9.3.4.3)

$$\Delta f_{pSD} := \epsilon_{bdf} \cdot E_p \cdot K_{df} = 9.588 \cdot \text{ksi}$$

Prestress loss due to Shrinkage of pile concrete
(LRFD 5.9.3.4.3)

Creep of pile concrete (d->f)

$$\Delta f_{cd} := \frac{-\Delta f_{pLT, id} \cdot A_{p,\text{total}}}{A_g} = -0.122 \cdot \text{ksi}$$

Change in concrete stress at centroid of prestressing strands due to long-term losses between transfer and installation, combined with deck weight and superimposed loads
(for piles, it is simplified)

$$\Delta f_{pCD} := \frac{E_p}{E_{ci}} f_{cgp} \cdot (\Psi_b(t_f, t_i) - \Psi_b(t_d, t_i)) \cdot K_{df} + \frac{E_p}{E_c} \Delta f_{cd} \cdot \Psi_b(t_f, t_d) \cdot K_{df} = 2.365 \cdot \text{ksi}$$

Prestress loss due to Creep of pile concrete
(LRFD 5.9.3.4.3)

Relaxation of prestressing CFRP (d->f)

$$f_{pu} = 370 \cdot \text{ksi}$$

Design tensile strength



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$$f_{pt} = 172 \cdot \text{ksi}$$

Prestress stress at transfer

$$\Delta f_{pR2} := \Delta f_{pR}(t_d, t_f) = 4.452 \cdot \text{ksi}$$

Prestress loss due to relaxation

Time from transfer to installation

Shrinkage of deck concrete (d->f)

$$\Delta f_{pSS} := 0 \text{ksi}$$

Not applicable to piles

(LRFD 5.9.3.4.3)

Total time-depedent prestress loss between pile installation and final time

$$\Delta f_{pLT.df} := \Delta f_{pSD} + \Delta f_{pCD} + \Delta f_{pR2} - \Delta f_{pSS} = 16.405 \cdot \text{ksi}$$

Total time-depedent prestress loss between transfer and final time

$$\Delta f_{pLT} := \Delta f_{pLT.id} + \Delta f_{pLT.df} = 34.757 \cdot \text{ksi}$$

3.3 Summary -Prestress Loss

$$\Delta f_p := \Delta f_{pES} + \Delta f_{pLT} + \Delta f_{pTH} = 41.463 \cdot \text{ksi}$$

Total prestress loss
(AASHTO CFRP 1.9.2.1)

$$\text{Loss\%} := \frac{\Delta f_p}{f_{pi}} = 23.2 \cdot \%$$

Total prestress loss percentage

$$\Delta f_{pES} = 6.707 \cdot \text{ksi}$$

Prestress loss due to elastic shortening

$$\Delta f_{pTH} = 0$$

Prestress loss due to temperature change (not considered)

$$\Delta f_{pLT} = 34.757 \cdot \text{ksi}$$

Total long-term time-dependent prestress loss

$$\Delta f_{pLT.id} = 18.351 \cdot \text{ksi}$$

Long-term time-dependent prestress loss between transfer and pile installation

$$\Delta f_{pLT.df} = 16.405 \cdot \text{ksi}$$

Long-term time-dependent prestress loss between pile installation and final time

4. DETERMINE JACKING STRESS/FORCE

$$\Delta f_{p.installation} := \Delta f_{pES} + \Delta f_{pLT.id} + \Delta f_{pTH} = 25.058 \cdot \text{ksi}$$

Total prestress loss at time of pile installation

$$f_{c.installation} := \frac{A_{p.total} \cdot (f_{pi} - \Delta f_{p.installation})}{A_g} = 1.02 \cdot \text{ksi}$$

Concrete stress (compression) at time of pile installation

$$P_i = 32 \text{kip}$$

Jacking force (Need to adjust this value to let $\sigma_{c.installation}$ slightly greater than 1 ksi)

$$\text{Check}_{f_{pi.limit}} = \text{"OK"}$$

(FDOT 455-101 series)

$$P\% := \frac{P_i}{P_u} = 48.3\%$$

Jacking percentage

5. SECTION CAPACITY CALCULATION

5.1 Summary of Strain/Stress

$f_{pu} = 370 \cdot \text{ksi}$	Design tensile strength
$f_{pi} = 179 \cdot \text{ksi}$	Jacking stress
$f_{pei} := f_{pi} - \Delta f_{p.installation} = 154 \cdot \text{ksi}$	Effective prestress at time of pile installation
$f_{c.installation} = 1.023 \cdot \text{ksi}$	Concrete stress (compression) at time of pile installation
$f_{pe} := f_{pi} - \Delta f_p = 137 \cdot \text{ksi}$	Final effective prestress in tendons
$f_{ce} := \frac{A_{p.total} \cdot f_{pe}}{A_g} = 0.913 \cdot \text{ksi}$	Concrete stress (compression) at final time
$\epsilon_{pe} := \frac{f_{pe}}{E_p} = 6.108 \times 10^{-3}$	Strain in prestressing tendons at final time due to prestress force
$\epsilon_{ce} := \frac{f_{ce}}{E_c} = 2.004 \times 10^{-4}$	Strain in concrete at final time due to prestress force
$\epsilon_{cu} := 0.003$	Concrete crushing strain
$\epsilon_{pu} := \frac{f_{pu}}{E_p} = 0.016$	CFRP rupture strain
$\epsilon_{p.limit} := \frac{f_{p.limit}}{E_p} = 0.016$	
$\epsilon_{c.rest} := \epsilon_{cu} - \epsilon_{ce} = 2.800 \times 10^{-3}$	Remaining strain in concrete until crushing
$\epsilon_{p.rest} := \epsilon_{pu} - \epsilon_{pe} = 0.010$	Remaining strain in CFRP until rupture

5.2 P-M Diagram

$$\alpha_1 = 0.85$$

Concrete stress block factors
(LRFD 5.6.2.2)

$$\beta_1 = 0.75$$

$$\phi := 0.75$$

Resistance factor
(AASHTO CFRP 1.5.3.2)

$$k_c := \min\left(\max\left(0.85 - 0.02 \cdot \frac{f_c - 10\text{ksi}}{\text{ksi}}, 0.75\right), 0.85\right) = 0.85$$

$$P_{\max} := 0.85 \cdot [k_c \cdot f_c \cdot (A_g - A_{p,\text{total}}) - A_{p,\text{total}} \cdot (f_{pe} - E_p \cdot \epsilon_{cu})] = 1263 \cdot \text{kip}$$

Nominal axial resistance
(LRFD 5.6.4.4)

$$a_{\max} := hh = 18 \cdot \text{in}$$

$$c_{\max} := \frac{a_{\max}}{\beta_1} = 24 \cdot \text{in}$$

Max compression depth

$$c_{\text{increment}} := 0.01 \text{in}$$

Compression depth c increment

$$n_{c,\max} := \frac{c_{\max}}{c_{\text{increment}}} = 2400$$

$$cc_0 := \begin{cases} \text{for } i \in 0 .. n_{c,\max} - 1 \\ cc_{0_i} \leftarrow c_{\text{increment}} \cdot (n_{c,\max} - i) \\ cc_0 \end{cases}$$

Give a compression depth
from top of the section to N.A.

```

εf0 := | for j ∈ 0..rows(cc0) - 1
      |   for i ∈ 0..rows(dp) - 1
      |     εf0j,i ← εpe + εc.rest * (dp_i - (εc.rest/εcu) * cc0_j) / (εc.rest/εcu) * cc0_j
      |     (break) if εf0j,i ≥ εp.limit
      | εf0
  
```

CFRP strain calculation
"break" the loop when CFRP strain is greater than rupture strain

```

cc := | for i ∈ 0..(rows(εf0) - 2)
      |   j ← nc.max - (rows(εf0) - 2) + i
      |   cc_i ← j * c.increment
      | cc
  
```

	0
0	3.31
1	3.32
2	3.33
3	3.34
4	3.35
5	3.36
6	3.37
7	3.38
8	3.39
9	3.4
10	3.41
11	3.42
12	3.43
13	3.44
14	3.45
15	...

.in

"Good" compression depth

Note: "Good" compression depth refers to those compression depths that should be included in the P-M diagram calculation. In these cases, the compression depth of the section is large enough so that CFRP stresses are smaller than the stress limits according to AASHTO-CFRP Table 1.9.1. If a small compression depth is selected, the tensile strain at CFRP will be larger than the rupture strain. These cases are excluded in the P-M diagram since CFRP already ruptured and the section already failed before reaching to this point.

aa := β₁ · cc

```

εf := | for j ∈ 0..rows(cc) - 1
      |   for i ∈ 0..rows(dp) - 1
      |     εfj,i ← εpe + εc.rest * (dp_i - (εc.rest/εcu) * cc_j) / (εc.rest/εcu) * cc_j
      | εf
  
```



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$$f_f := \begin{cases} \text{for } j \in 0 \dots \text{rows}(cc) - 1 \\ \text{for } i \in 0 \dots \text{rows}(d_p) - 1 \\ f_{f,j,i} \leftarrow E_p \cdot \epsilon_{f,j,i} \\ f_f \end{cases} \quad \begin{array}{l} \text{CFRP stress calculation} \\ \text{only for parts when stress} < f_p.\text{limit} \end{array}$$

$$T_f := \begin{cases} \text{for } j \in 0 \dots \text{rows}(cc) - 1 \\ \text{for } i \in 0 \dots \text{rows}(d_p) - 1 \\ T_{f,j,i} \leftarrow E_p \cdot \epsilon_{f,j,i} \cdot n_{p_i} \cdot A_{pf} \\ T_f \end{cases} \quad \begin{array}{l} \text{Tensile force of each layer of CFRP} \\ \text{only for parts when stress} < f_p.\text{limit} \end{array}$$

	0	1	2	3	
$\epsilon_f =$	0	$6.481 \cdot 10^{-3}$	$9.804 \cdot 10^{-3}$	0.013	0.016
	1	$6.471 \cdot 10^{-3}$	$9.784 \cdot 10^{-3}$	0.013	0.016
	2	$6.462 \cdot 10^{-3}$	$9.765 \cdot 10^{-3}$	0.013	0.016
	3	$6.452 \cdot 10^{-3}$	$9.746 \cdot 10^{-3}$	0.013	0.016
	4	$6.443 \cdot 10^{-3}$	$9.726 \cdot 10^{-3}$	0.013	0.016
	5	$6.433 \cdot 10^{-3}$	$9.707 \cdot 10^{-3}$	0.013	0.016
	6	$6.424 \cdot 10^{-3}$	$9.688 \cdot 10^{-3}$	0.013	0.016
	7	$6.415 \cdot 10^{-3}$	$9.669 \cdot 10^{-3}$	0.013	0.016
	8	$6.406 \cdot 10^{-3}$	$9.651 \cdot 10^{-3}$	0.013	0.016
	9	$6.397 \cdot 10^{-3}$	$9.632 \cdot 10^{-3}$	0.013	0.016
	10	$6.388 \cdot 10^{-3}$	$9.613 \cdot 10^{-3}$	0.013	0.016
	11	$6.379 \cdot 10^{-3}$	$9.595 \cdot 10^{-3}$	0.013	0.016
	12	$6.37 \cdot 10^{-3}$	$9.577 \cdot 10^{-3}$	0.013	0.016
	13	$6.361 \cdot 10^{-3}$	$9.558 \cdot 10^{-3}$	0.013	0.016
	14	$6.352 \cdot 10^{-3}$	$9.54 \cdot 10^{-3}$	0.013	0.016
	15	$6.343 \cdot 10^{-3}$	$9.522 \cdot 10^{-3}$	0.013	...



CFRP -PC TRAINING COURSE DESIGN EXAMPLE: 18" SQUARE PILE

$$C_{\text{concrete}} := \begin{cases} \text{for } i \in 0 \dots \text{rows}(f_f) - 1 & \text{Compression force from concrete} \\ C_{\text{concrete}_i} \leftarrow \alpha_1 \cdot f_c \cdot \beta_1 \cdot cc_i \cdot bb \\ C_{\text{concrete}} \end{cases}$$

$$T_{\text{CFRP}} := \begin{cases} \text{for } i \in 0 \dots \text{rows}(f_f) - 1 & \text{Total tensile force from CFRP} \\ T_{\text{CFRP}_i} \leftarrow \sum_{j=0}^{\text{rows}(d_p)-1} T_{f_{i,j}} \\ T_{\text{CFRP}} \end{cases}$$

$$P := C_{\text{concrete}} - T_{\text{CFRP}}$$

$$M := \begin{cases} \text{for } i \in 0 \dots \text{rows}(f_f) - 1 \\ M_i \leftarrow C_{\text{concrete}_i} \cdot \left(\frac{hh}{2} - \frac{\beta_1 \cdot cc_i}{2} \right) + \sum_{j=0}^{\text{rows}(d_p)-1} \left[T_{f_{i,j}} \cdot \left(d_{p_j} - \frac{hh}{2} \right) \right] \\ M \end{cases}$$

aa =

	0
0	2.482
1	2.49
2	2.498
3	2.505
4	2.513
5	2.52
6	2.527
7	2.535
8	2.542
9	2.55
10	2.558
11	2.565
12	2.572
13	2.58
14	2.588
15	...

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P =

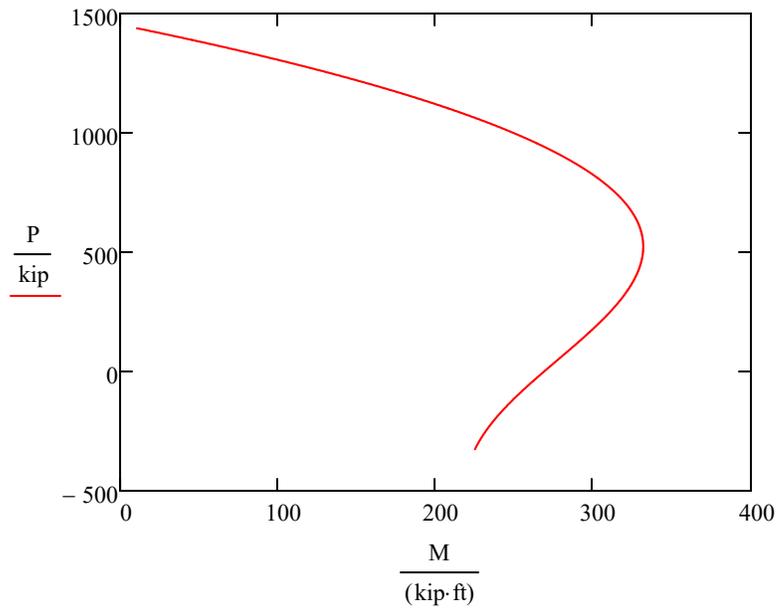
	0
0	-326
1	-324
2	-322
3	-320
4	-318
5	-316
6	-315
7	-313
8	-311
9	-309
10	-307
11	-306
12	-304
13	-302
14	-300
15	...

·kip

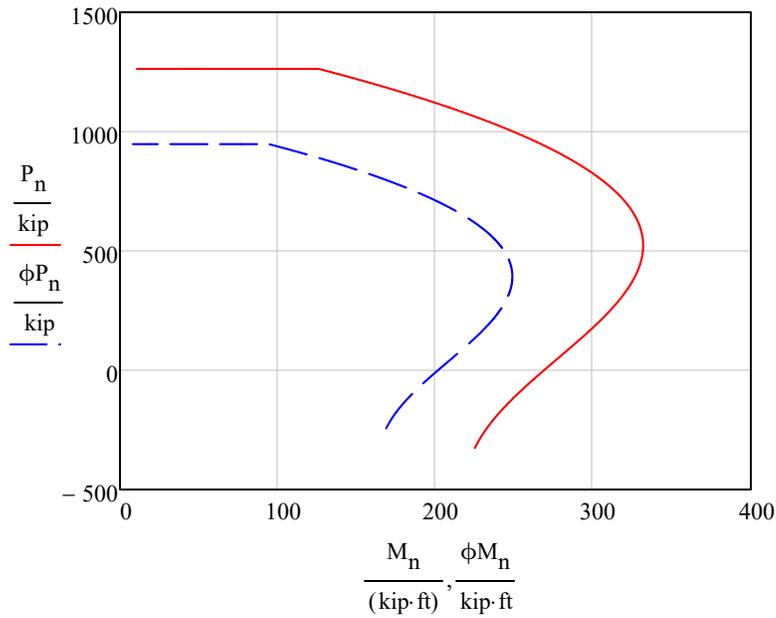
M =

	0
0	225
1	225
2	225
3	225
4	226
5	226
6	226
7	226
8	226
9	226
10	226
11	227
12	227
13	227
14	227
15	...

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$$P_n := \begin{cases} \text{for } i \in 0 \dots \text{rows}(P) - 1 \\ P_{n,i} \leftarrow \min(P_i, P_{\max}) \\ P_n \end{cases} \quad \begin{aligned} M_n &:= M \\ \phi P_n &:= \phi \cdot P_n \\ \phi M_n &:= \phi \cdot M_n \end{aligned}$$



$$P_{\text{tension}} := A_{p,\text{total}}(f_{p,\text{limit}} - f_{pe}) = 499 \cdot \text{kip}$$