



# **Bearing Capacity Factors for Shallow Foundations Subject to Combined Lateral and Axial Loading**

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# PRESENTATION OVERVIEW

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- 2) PROJECT TASKS
- 3) BEARING CAPACITY EQUATIONS
- 4) SOIL PROPERTIES
- 5) CENTRIFUGE & LOAD CASE SENARIOS
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  - $L/B=1$
  - CONCENTRIC LOADING
  - ECCENTRIC LOADING
  - INCLINED LOADING
  - INCLINED-ECCENTRIC LOADING
- 6) MEASURED RESULTS
  - $L/B=20$  (Verify  $N_q$  &  $N_\gamma$ )
  - $L/B=20$  (Verify shape and depth factors)
  - $L/B=10$  ( $D_f=0$  &  $0.5B$ , Very Dense,  $L/A=0.10$  &  $0.25$ )
  - $L/B=10$  ( $D_f=0$  &  $0.5B$ , Medium Dense,  $L/A=0.10$  &  $0.25$ )
  - $L/B=10$  (Verify eccentricity,  $i_\gamma$  &  $i_q$ )
- 7) CONCLUSIONS

# BACKGROUND AND MOTIVATION

- 1) AASHTO Specifications (10.6.3.1.2) make allowance for load inclination
  - Meyerhof (1953), Vesic (1973) and Hansen (1973) are considered
  - Based on small scale experiments
  - Derived for footings without embedment
- 2) AASHTO commentary (C10.6.3.1.2a) suggest inclination factors may be overly conservative
  - Footing embedment ( $D_f$ ) = B or greater
  - Footing with modest embedment may omit load inclination factors
- 3) FHWA GEC No.6 indicates load inclination factors can be omitted if lateral and vertical load checked against their respective resistances
- 4) Resistance factors included in the AASHTO code were derived for vertical loads
  - Applicability to combined lateral/axial loads are currently unknown
  - Up to 75% reduction in Nominal Bearing Resistance computed with AASHTO load inclination factors

# BACKGROUND AND MOTIVATION



- 5) NCHRP 651 on LRFD Design and Construction of Shallow Foundations for Highway Bridges
  - Identify and propose the concept of a combined failure state
  - Similar to beam/column interaction diagram
  
- 6) FDOT research project BDK75-977-22 completed in December 2013
  - Limited set of combined vertical and horizontal loads
  - Results indicated the inclination of resultant load had an experimentally proven effect on the bearing capacity of MSE walls

# PROJECT OBJECTIVES AND TASKS

## OBJECTIVES

Measure bearing capacity of representative shallow foundations in centrifuge tests to identify the influence of embedment, lateral/axial concentric and eccentric loads through experimentally determined load factors.

## TASKS

- 1) Task-1: Collect data on current practice through online survey
- 2) Task-2: Select foundation scenarios to test and design experimental program
- 3) Task-3: Conduct centrifuge tests on model foundations for bearing capacity
- 4) Task-4: Compare measured bearing capacity to predictions
- 5) Tasks-5 and 6: Closeout Teleconference and Final Report

# TASK 1: METHODS OF BEARING CAPACITY

FDOT recommends analysis of shallow foundations be done in accordance with AASHTO LRFD Bridge Design Specifications

**General bearing capacity equation recommended by AASHTO (2016)**

$$q_n = \cancel{c}N_{cm}^{\rightarrow 0} + \gamma D_f N_{qm} \cancel{C_{wq}}^{\rightarrow 1} + 0.5\gamma B N_{\gamma m} \cancel{C_{w\gamma}}^{\rightarrow 1} \quad \text{Eq.1}$$

$$q_n = \gamma D_f N_{qm} + 0.5\gamma B N_{\gamma m} \quad \text{Eq.2}$$

$$N_{qm} = N_q S_q d_q i_q \quad \text{Eq.3}$$

$$N_{\gamma m} = N_\gamma S_\gamma i_\gamma \quad \text{Eq.4}$$

$$N_q = e^{\pi \tan \phi_f} \tan^2 \left( 45^\circ + \frac{\phi_f}{2} \right) \quad \text{Eq.5}$$

$$N_\gamma = 2(N_q + 1) \tan(\phi_f) \quad \text{Eq.6}$$

$B$  = Foundation width

$S_q, S_\gamma$  = Shape correction factor

$\gamma$  = Soil unit weight

$d_q$  = Depth correction factor

$D_f$  = Embedment depth

$i_q, i_\gamma$  = Inclination correction factors

# TASK 2: TEST SOIL

## AASHTO CLASS: A-3

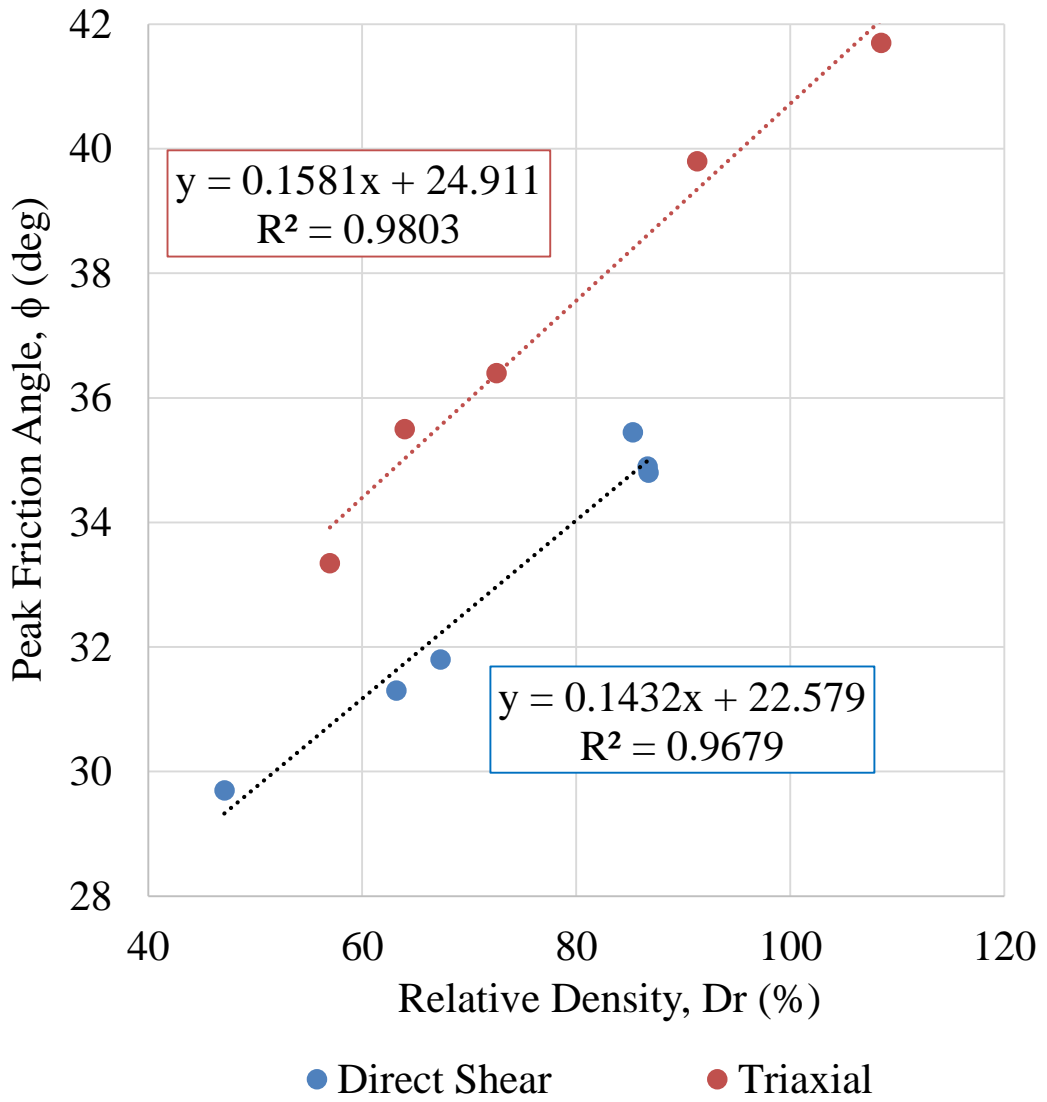
- Max unit weight: 108.9 pcf
- Min unit weight: 90.7 pcf
- 2.5% Passing #200
- 97.5% Sand
- Coefficient of Uniformity: 1.67
- Coefficient of Curvature: 1.35
- Specific gravity: 2.67
- $e_{min}$ : 0.53
- $e_{max}$ : 0.84
- SP Unified Soil Classification

## DIRECT SHEAR TEST:

- $D_r = 55 - 93\%$
- $\phi = 29.5^\circ - 34^\circ$

## TRIAXIAL CD-TEST:(c=0)

- $D_r = 61 - 94\%$
- $\phi = 36.0^\circ - 41.2^\circ$

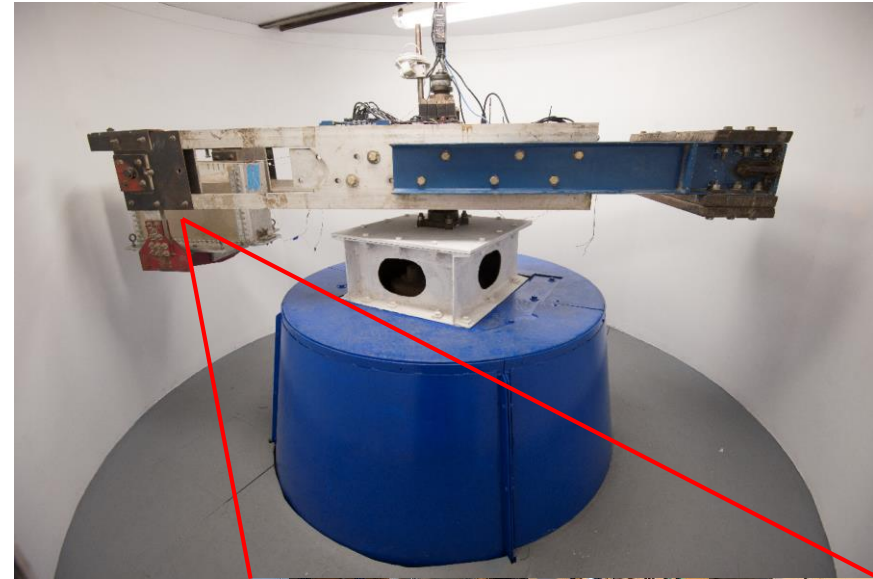


# TASK 3: GEOTECHNICAL CENTRIFUGE TESTS

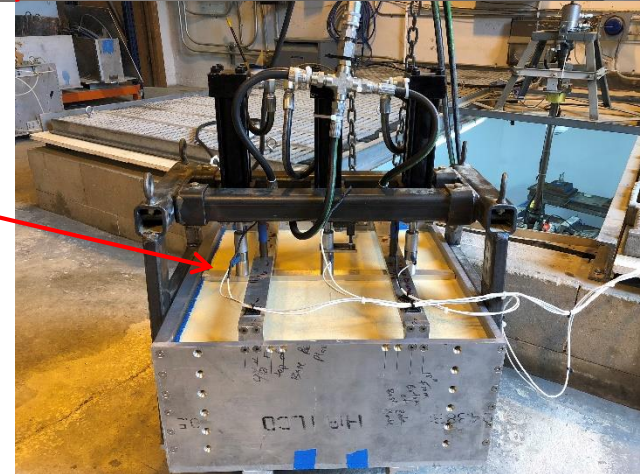
- Useful to study geotechnical problems (capacity of foundations) at a fraction of the cost of prototype study
- Soil has non-linear mechanical properties dependent on effective stress and stress history
- Spinning model in centrifuge increases the “gravitational” acceleration model which produces identical self-weight stresses between model and prototype ( $\sigma_{\text{model}} / \sigma_{\text{prototype}} = 1$ )
- Scale other properties for testing  
ex.  $L_{\text{model}} / L_{\text{prototype}} = 1/N$

Property	Scale Factor
Length	1/N
Area	1/N <sup>2</sup>
Volume	1/N <sup>3</sup>
Force	1/N <sup>2</sup>
Unit Weight	N
Stress	1
Strain	1

3 meter diameter centrifuge



1/36<sup>th</sup> scale  
model: Shallow  
foundation  
L/B = 20



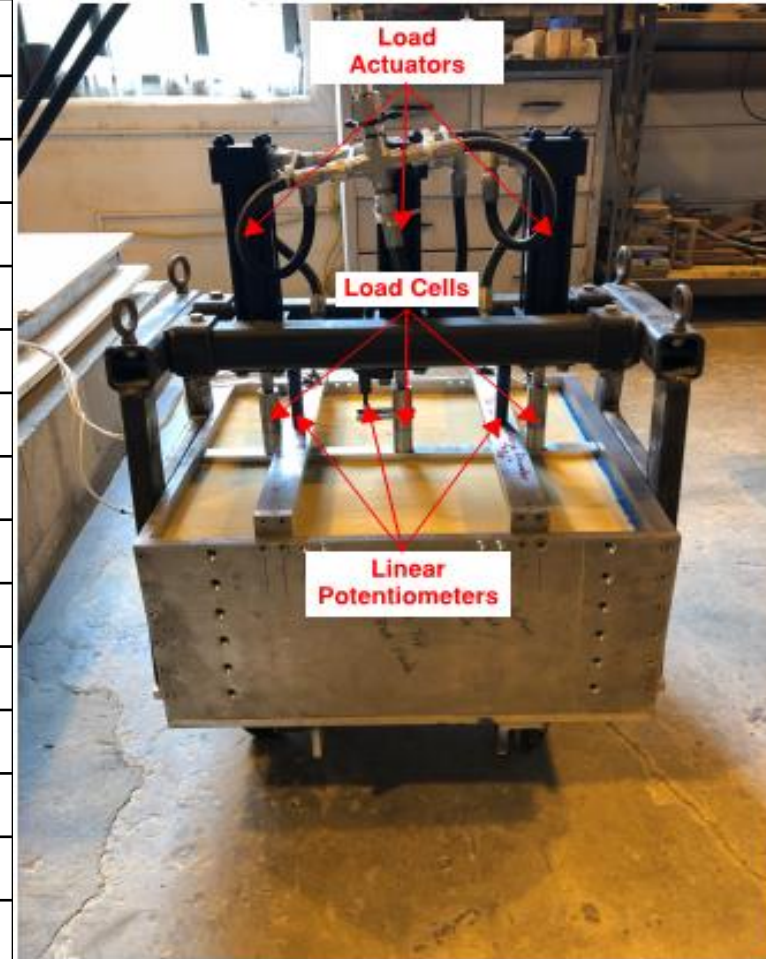
- In flight load application and monitoring of foundation response (displacement and soil pressure)



# TASK 3: TEST CONDITIONS

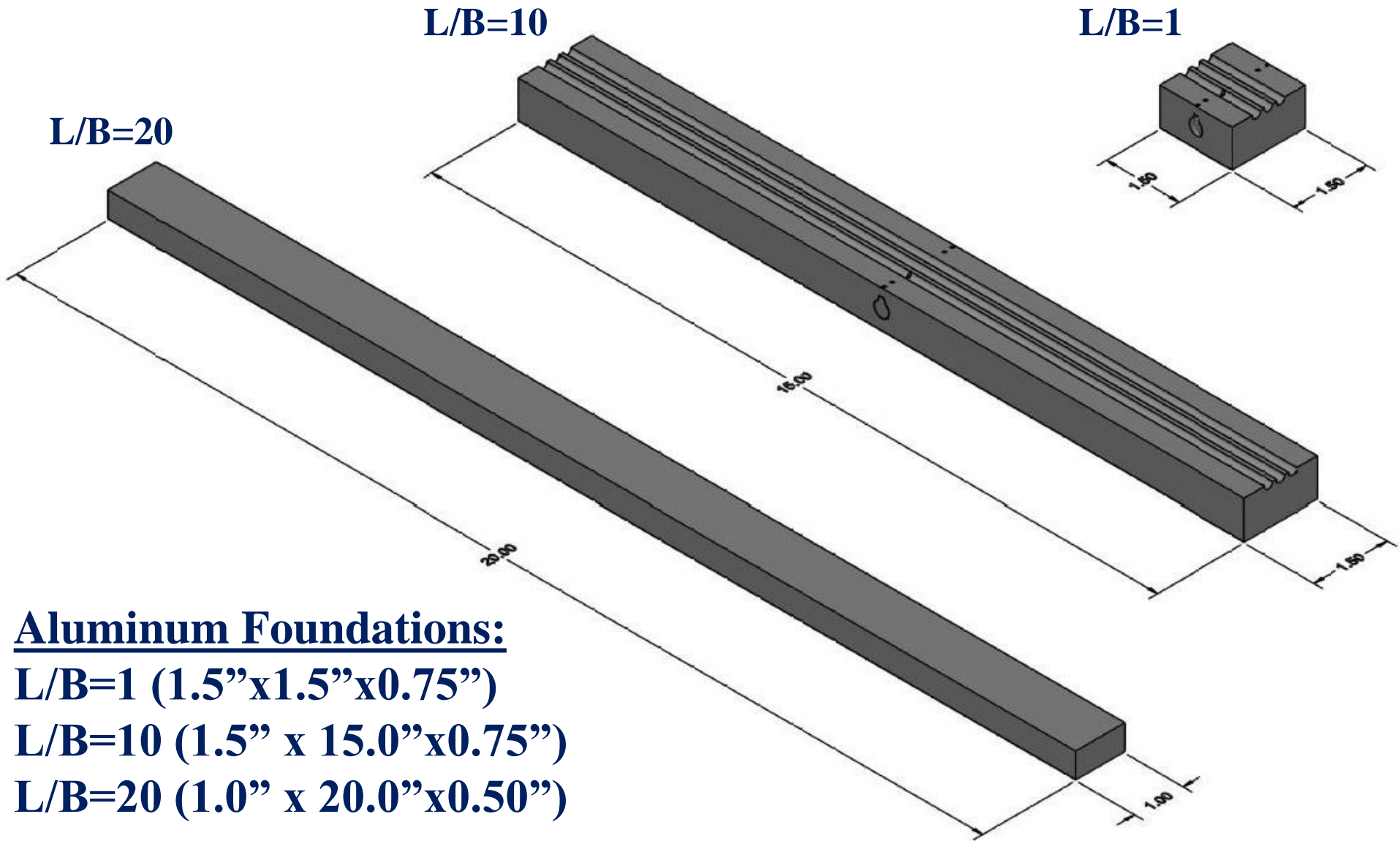
## Test Apparatus

L/B Ratio	20	10	1
Interior container width (in.)	20		
Interior container length (in.)	20	15	20
Interior container height (in.)	9.5		
Soil height (in.)	8.5		
Scale factor (N)	36	40	40
Foundation material	Alum.		
Model width (in)	1	1.5	1.5
Model length (in.)	20	15	1.5
Model thickness (in.)	0.5	0.75	0.75
# of Hyd. load actuators	3	3	1
# of Omega load cells	3	3	1
# of BEI linear potentiometers	3	3	1
# of Pressure sensors	0	4	4



\* Container designed to accommodate max load for ultimate bearing capacity and minimize boundary influences on failure surfaces.

# TASK 3: TEST FOUNDATIONS



## Aluminum Foundations:

L/B=1 (1.5" x 1.5" x 0.75")

L/B=10 (1.5" x 15.0" x 0.75")

L/B=20 (1.0" x 20.0" x 0.50")

# LOAD CASE SCENARIOS & NUMBER OF TEST

Load Cases – 5 (Positions 1-5)

Relative Density – 2 (Medium & Very dense)

Embedment Depth – 2 (Surface condition &  $D_f=0.5B$ )

Inclination Angles -2 ( $L/A=0.1$  &  $0.25$ )

L/B Ratios -2 (1 & 10)

Test Repeatability -2

Load Case Scenarios: Meyerhof (1953)

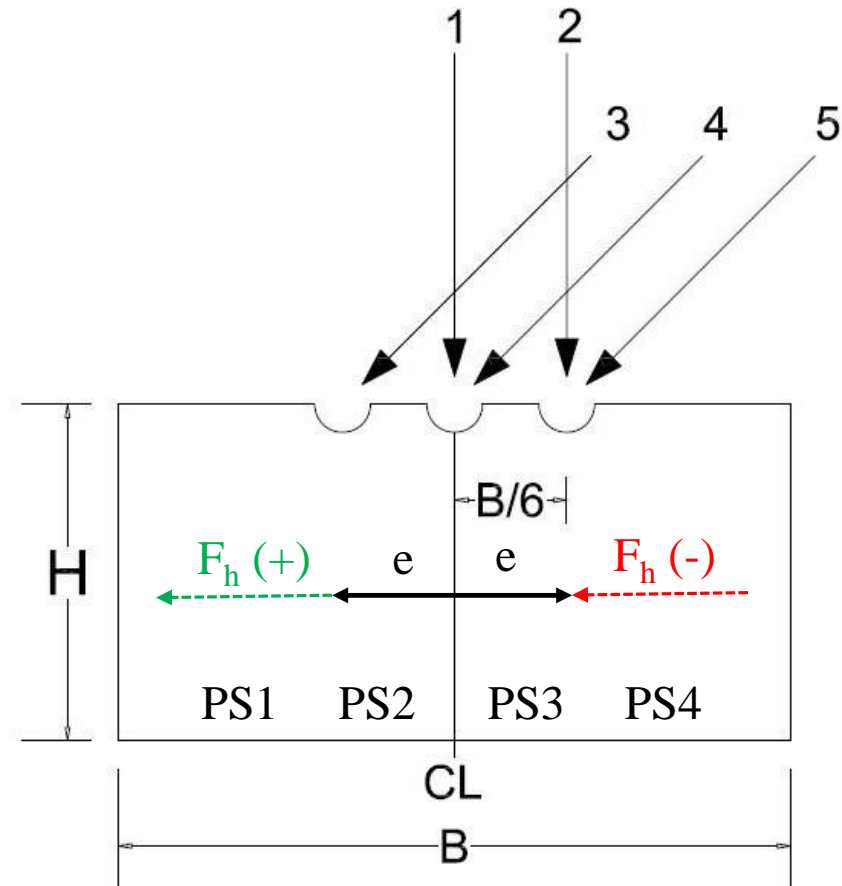
Load Case-1: Concentric

Load Case-2: Eccentric

Load Case-3: Eccentric-inclined, horizontal component **positive (+)**, to the direction of the eccentricity

Load Case-4: Inclined

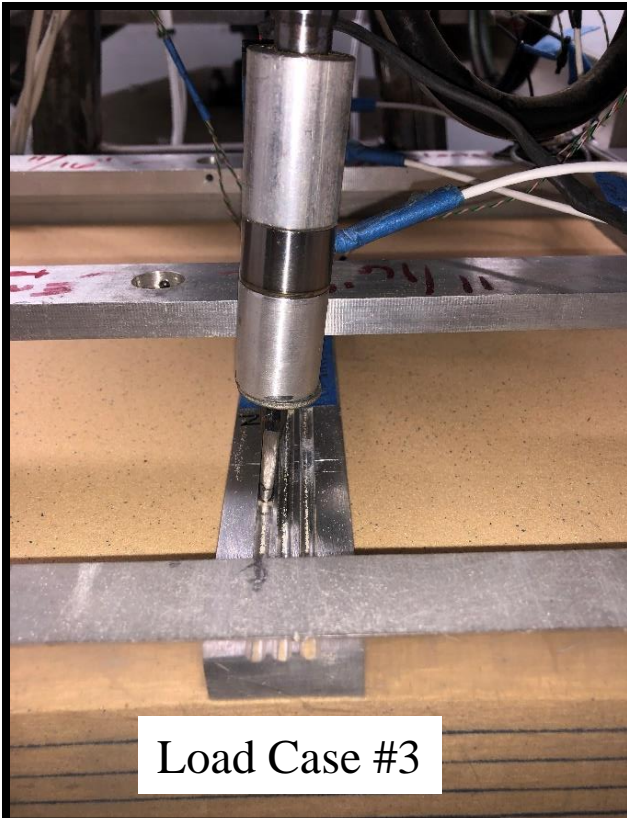
Load Case-5: Eccentric-inclined, horizontal component **negative (-)**, to the direction of the eccentricity



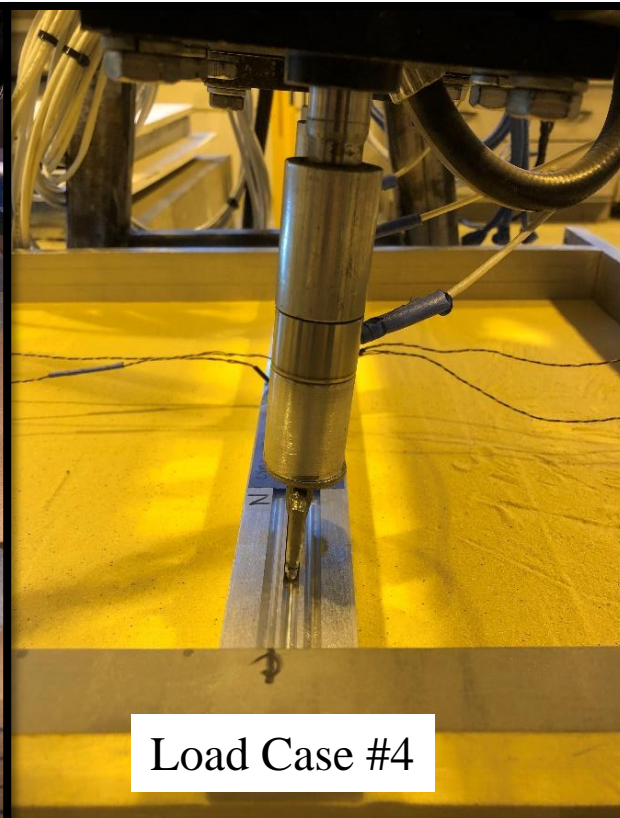
Footing loading scenarios:

Where  $B$  = width,  $H$  = Height,  $a$  = angle of inclination (not to scale) and eccentricity =  $B/6$ .

# INCLINED LOAD SCENARIOS (L/B = 1 & 10)



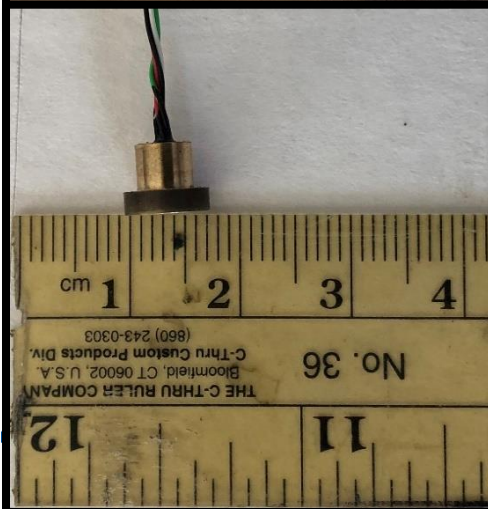
Load Case #3



Load Case #4



Load Case #5



Manufacture	Tokyo Measuring Instruments Lab.)
Type	PDB-3MPB
Capacity	62 ksf (3MPa)
Rated Output	1mV/V (2000x10 <sup>-6</sup> strain)

# CONCENTRIC LOADING ON STRIP FOUNDATION (L/B=20)

FOR THE PURPOSE OF THIS STUDY:

$$q_n = \gamma D_f N_{qm} + 0.5\gamma B N_{\gamma m} \quad \text{Eq.7}$$

STRIP FOUNDATION AT SURFACE:

$$q_n = 0.5\gamma B N_{\gamma m} \quad \text{Eq.8}$$

- $D_f = 0$
- Measured  $N_{\gamma m}$  Term
- $F_{cs}$ ,  $F_{qs}$  &  $F_{\gamma s} \approx 1.00$
- L/B = 20 the shape factors  $s_q$  and  $s_\gamma$  are 1.04 and 0.98 (<4% error)

STRIP FOUNDATION AT  $D_f = B$ :

$$q_n = \gamma D_f N_{qm} + 0.5\gamma B N_{\gamma m} \quad \& \quad N_{qm} = N_q S_q d_q i_q$$

- $D_f = B$
- Measured  $N_{qm}$  & depth corrections,  $d_q$
- $N_q$  &  $N_\gamma$  are only functions of  $\phi$

# CONCENTRIC LOADING ON STRIP FOUNDATION (L/B=20)



Name	D <sub>r</sub> (%)	γ (pcf)	φ (degree)	Measured-qu (psf)	Embedment Depth (D <sub>f</sub> )	Eccentricity	Inclination	Series #
LT-01*	86.82	106.09	35.01	14,480	0	0	0	1
LT-02*	86.71	106.07	35.00	14,570	0	0	0	2
LT-03*	63.97	101.56	31.74	10,012	0	0	0	1
LT-04*	62.81	101.34	31.57	10,880	0	0	0	2
LT-05*	63.72	101.51	31.70	12,000	0.5B	0	0	1
LT-06*	63.75	101.52	31.71	11,780	0.5B	0	0	2
LT-07*	86.80	106.09	35.01	14,700	0.5B	0	0	1
LT-08*	86.07	105.94	34.90	11,800	0.5B	0	0	2
LT-09*	62.26	101.23	31.49	10,654	0.5B	0	0	3
LT-10*	88.47	106.44	35.25	14,938	0.5B	0	0	3
LT-11*	86.61	106.05	34.98	13,816	0.5B	0	0	4
LT-12*	88.83	106.51	35.30	16,500	0.5B	0	0	5
LT-13*	91.11	106.99	35.63	17,500	0.5B	0	0	6
LT-14	94.16	107.64	36.06	19,700	0.5B	0	0	7
LT-15**	-	-	-	-	0	0	0	3
LT-16	94.31	107.67	36.08	24,540	B	0	0	1
LT-17	95.37	107.90	36.24	14,160	0	0	0	4
LT-18	94.88	107.79	36.17	13,780	0	0	0	5
LT-19**	-	-	-	-	0.5B	0	0	8
LT-20	95.02	107.82	36.19	20,150	0.5B	0	0	9
LT-21	95.55	107.94	36.26	26,080	B	0	0	2

\* Vacuumed Soil Samples

\*\* Load test excluded from analysis due to instrumentation malfunction

# SHAPE & DEPTH FACTORS (L/B=20)

## Shape Factors considered in analysis:

(L/B=20 < 4% error for the factors used)

Reference	$S_q$	$S_\gamma$
DeBeer (1970) as modified by Vesić (1973)	1.04	0.98
Paikowsky et. Al (2010)	1.03	0.99
Meyerhof (1963)	1.02	1.02
Perau (1995, 1997)	1.06	0.95
Zhu and Michalowski (2005)	-	1.00

## Depth Factors considered in analysis:

### Hansen (1970):

$$d_q = 1 + 2 \tan \phi_f \cdot (1 - \sin \phi_f)^2 \left( \frac{d_f}{B} \right) \text{ for } \frac{d_f}{B} \leq 1$$

$$d_\gamma = 1$$

### Meyerhof (1963)

$$d_q = 1 + 0.1 \sqrt{K_p} \left( \frac{d_f}{B} \right) \text{ for } \phi_f > 10^\circ$$

$$d_\gamma = d_q$$

# MEASURED $N_q$ and $N_\gamma$ (L/B=20)

$$q_u = \gamma(D_f + \delta)N_{qm} + (1/2)\gamma B N_{\gamma m}$$

or in a normalized form as

$$\frac{q_u}{\gamma B} = \left( \frac{D_f + \delta}{\delta B} \right) N_{qm} + (1/2) N_{\gamma m}$$

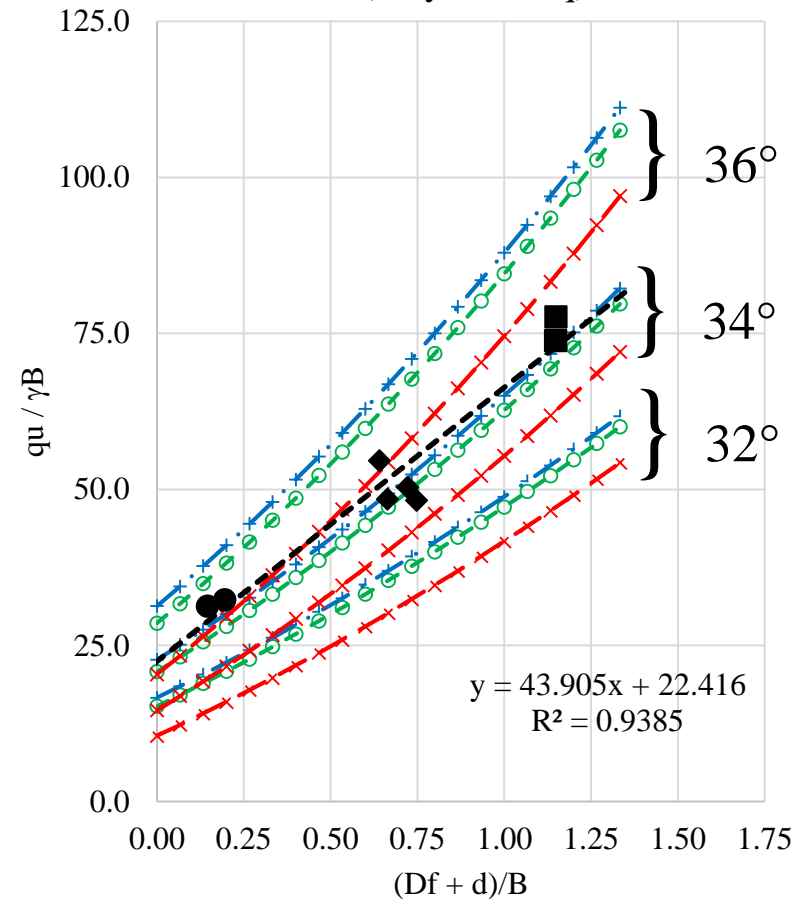
$$y = m x + b$$

$N_q$  = slope

$N_\gamma$  = 2 \* intercept

Density	$N_q$ (slope)	$N_\gamma$ (2 * intercept)	Reissner - $N_q$	Vesic'- $N_\gamma$
MD	21.38	25.97	24.83	28.05
VD-Vac	23.69	43.37	39.82	48.53
VD	43.91	44.83	44.65	56.78

Bearing Capacity Analysis-VD  
(Meyerhof-dq)

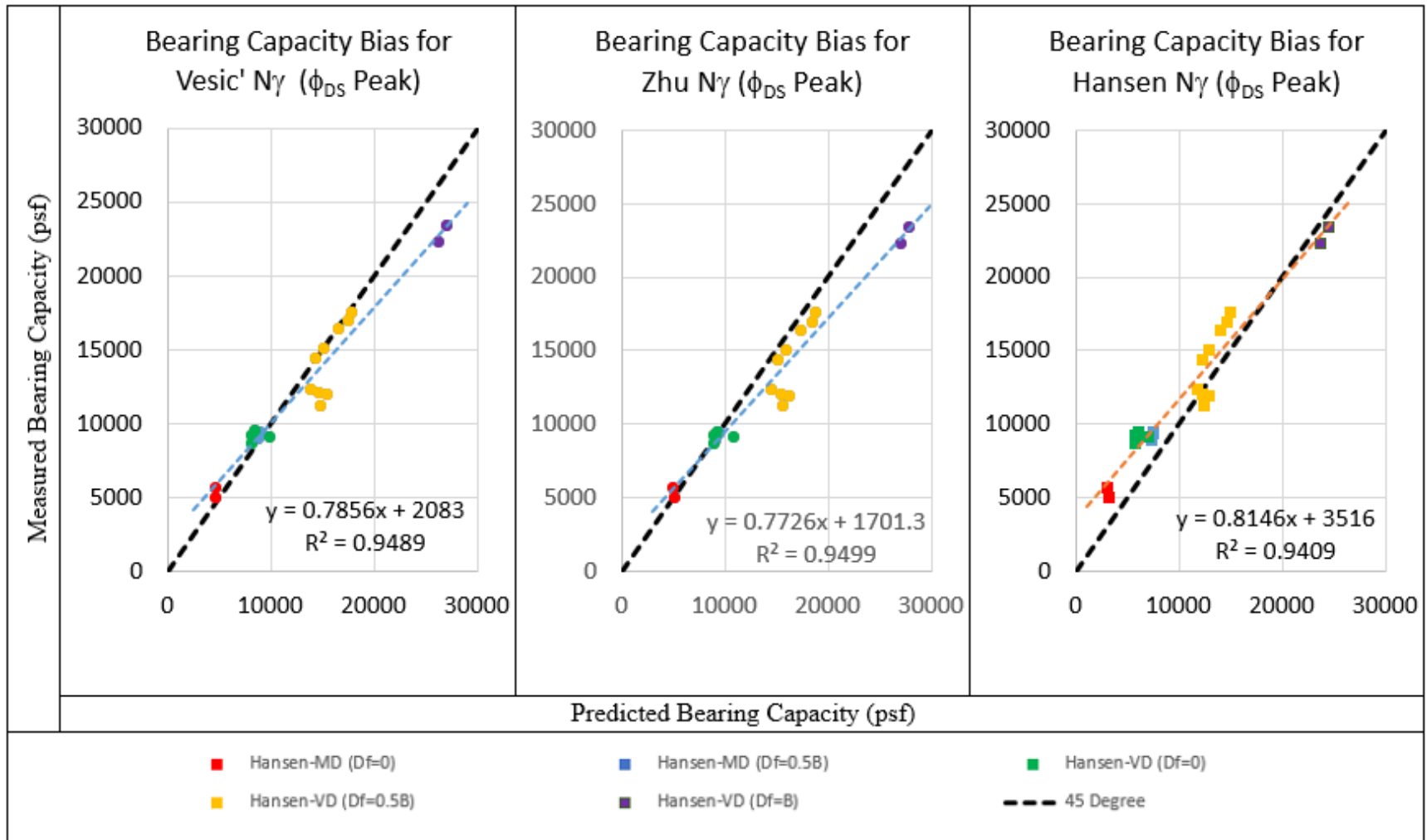


Prediction Methods:

Vesic'- $N_\gamma$     Zhu- $N_\gamma$     Hansen- $N_\gamma$

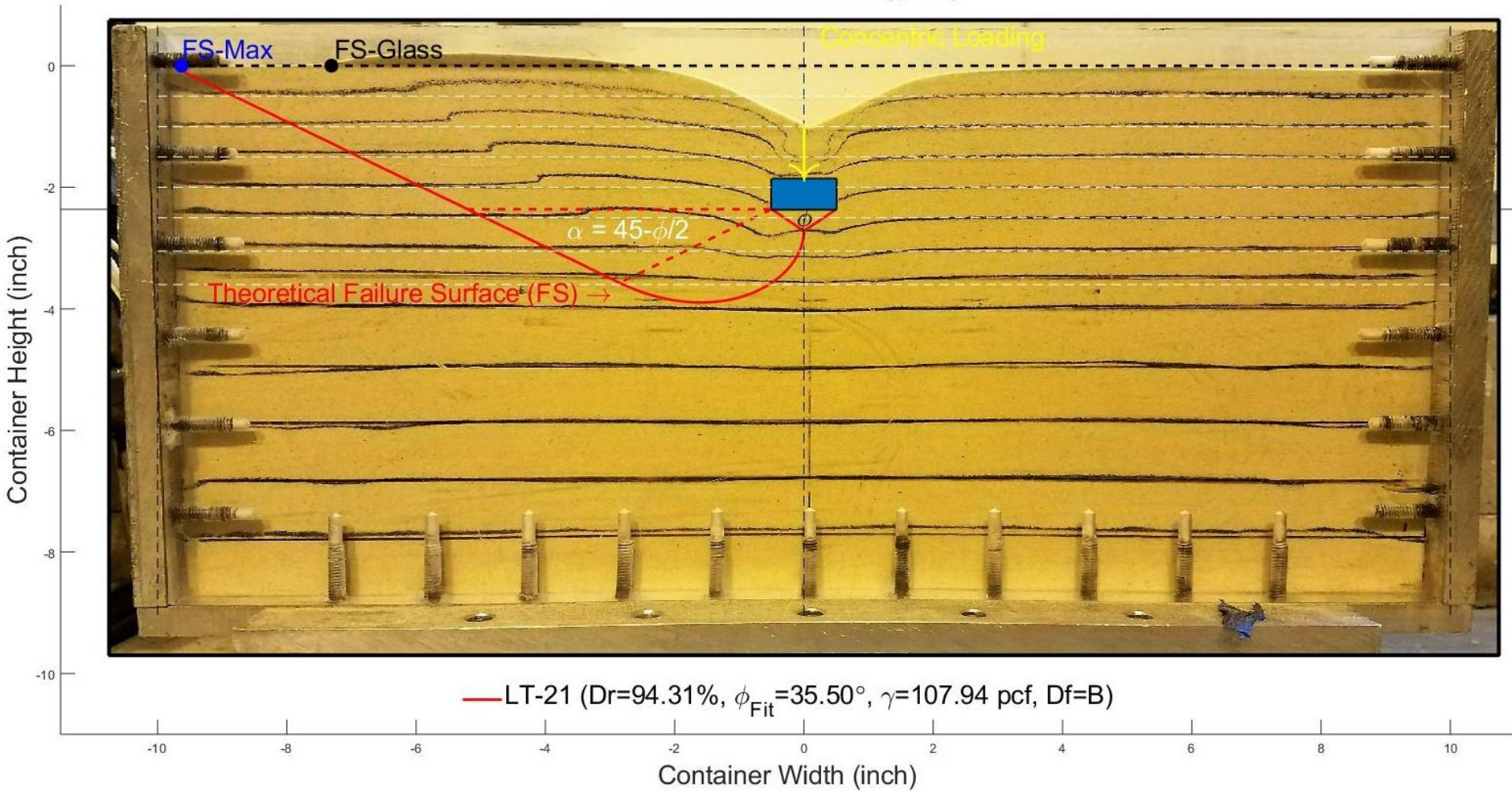


# BEARING CAPACITY BIAS PLOT (L/B=20)



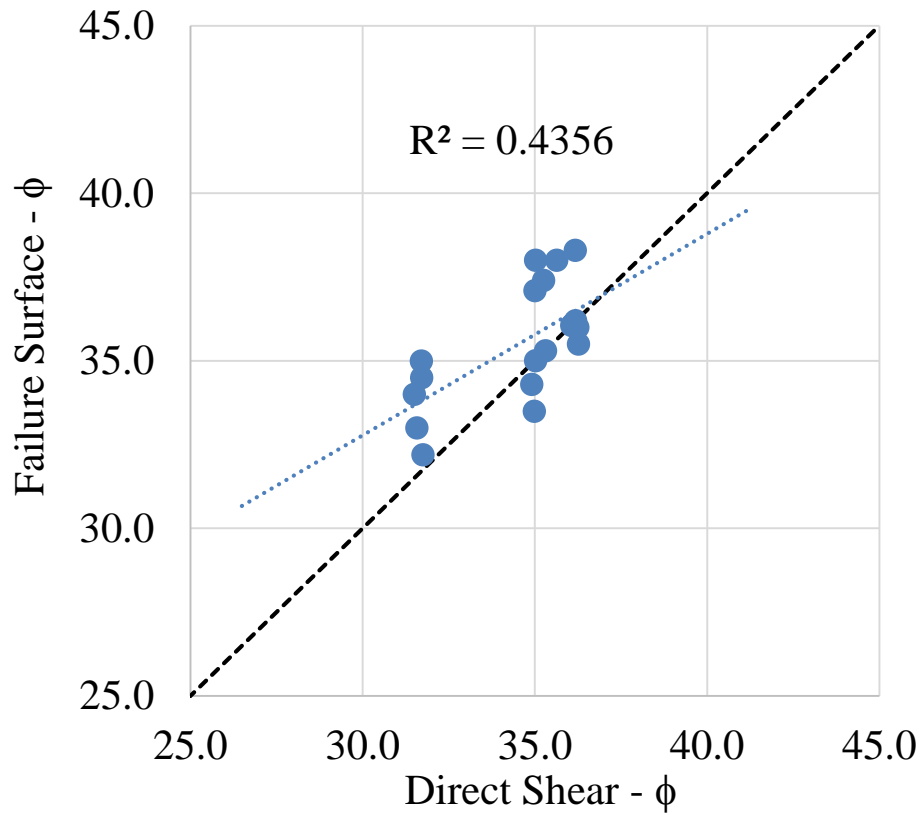
# THEORETICAL FAILURE SURFACE (LT-21)

LT-21 Failure Surface ( $\phi$ -Fit)

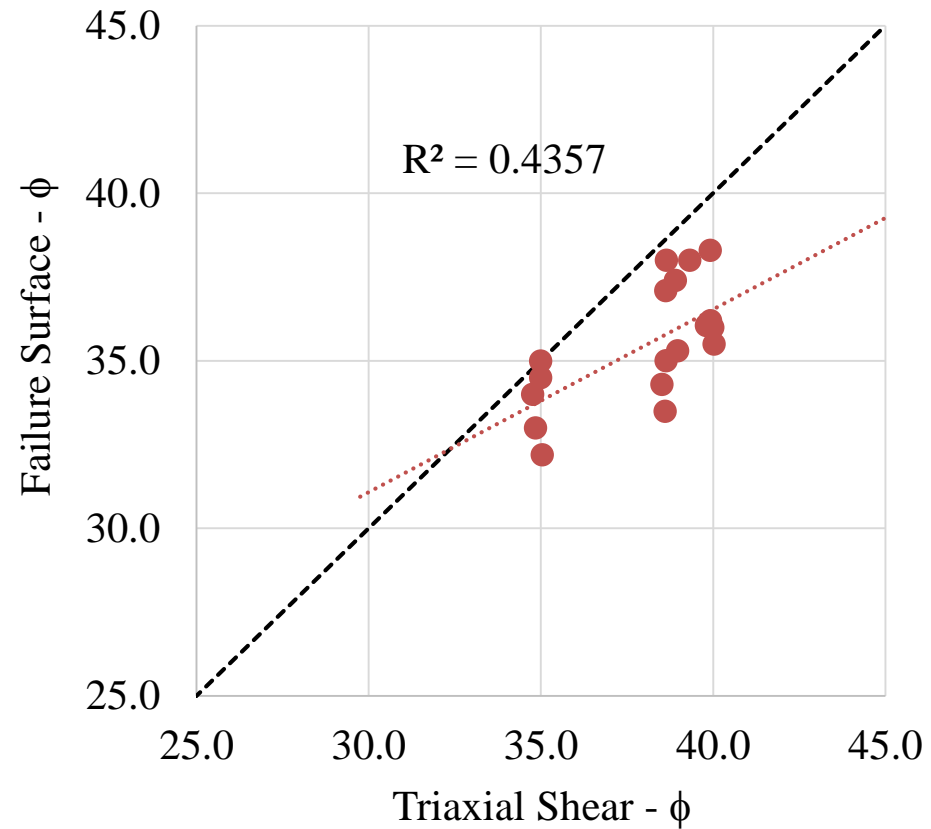


# DIRECT SHEAR & TRIAXIAL $\Phi$ - $\phi$ (Bias plot)

## Direct Shear $\Phi$ - $\phi$ (Bias)



## Triaxial Shear $\Phi$ - $\phi$ (Bias)



# LOADING ON RECTANGULAR FOUNDATION (L/B=10)

RECTANGLE FOUNDATION AT  $D_f = 0$  &  $D_f = B$ :

$$N_{qm} = N_q S_q d_q i_q \text{ \& } N_{\gamma m} = N_\gamma S_\gamma i_\gamma$$

- $D_f = 0$  &  $D_f = B$
- Measured  $N_{qm}$  & depth corrections,  $d_q$
- $N_q$  &  $N_\gamma$  are only functions of  $\phi$

RECTANGLE FOUNDATION AT with eccentricity:

$$N_{qm} = N_q S_q d_q i_q \text{ \& } N_{\gamma m} = N_\gamma S_\gamma i_\gamma$$

- $D_f = 0$  &  $D_f = B$
- Lateral/Axial load ratios: 0.1 & 0.25
- Maximum eccentricity:  $B/6$
- $B' = B - 2 \cdot e_B$

RECTANGLE FOUNDATION with load inclination:

$$N_{qm} = N_q S_q d_q i_q \text{ \& } N_{\gamma m} = N_\gamma S_\gamma i_\gamma$$

- $D_f = 0$  &  $D_f = B$
- Lateral/Axial load ratios: 0.1 & 0.25
- Isolate the inclination factors

# LOAD TEST ON RECTANGULAR FOUNDATION (L/B=10)-VD



Name	Load Case	D <sub>r</sub> (%)	γ (pcf)	φ (degree)	Measured-qu (psf)	Embedment Depth (D <sub>f</sub> )	Eccentricity	Inclination	Series #
LT-22**	1	-	-	-	-	-	-	-	-
LT-23	1	95.82	108.00	36.30	18860	0	0	0	2
LT-24	1	96.73	108.20	36.43	19060	0	0	0	3
LT-25	4	90.63	106.90	35.56	13750	0	B/6	0.10	1
LT-26	4	94.20	107.65	36.07	12460	0	B/6	0.10	2
LT-27	5	94.67	107.75	36.14	15970	0	B/6	-0.10	1
LT-28	5	96.60	108.16	36.41	17070	0	B/6	-0.10	2
LT-29	3	95.07	107.84	36.19	8612	0	B/6	0.10	1
LT-30	3	95.10	107.84	36.20	7944	0	B/6	0.10	2
LT-31	2	98.89	108.66	36.74	14790	0	B/6	0	1
LT-32	2	98.29	108.53	36.65	18670	0	B/6	0	2
LT-33	2	95.40	107.91	36.24	22060	0.5B	B/6	0	1
LT-34	2	95.65	107.96	36.28	24080	0.5B	B/6	0	2
LT-35	1	92.99	107.39	35.9	21762	0.5B	0	0	1
LT-36	1	95.60	107.95	36.27	25900	0.5B	0	0.10	2
LT-37	4	96.54	108.15	36.4	22900	0.5B	0	0.10	1
LT-38	4	95.89	108.01	36.31	21090	0.5B	0	0.10	2
LT-39	5	97.02	108.25	36.47	26520	0.5B	B/6	-0.10	1
LT-40	5	97.58	108.38	36.55	24830	0.5B	B/6	-0.10	2

\*\* Load test excluded from analysis due to instrumentation malfunction

# LOAD TEST ON RECTANGULAR FOUNDATION (L/B=10)-VD

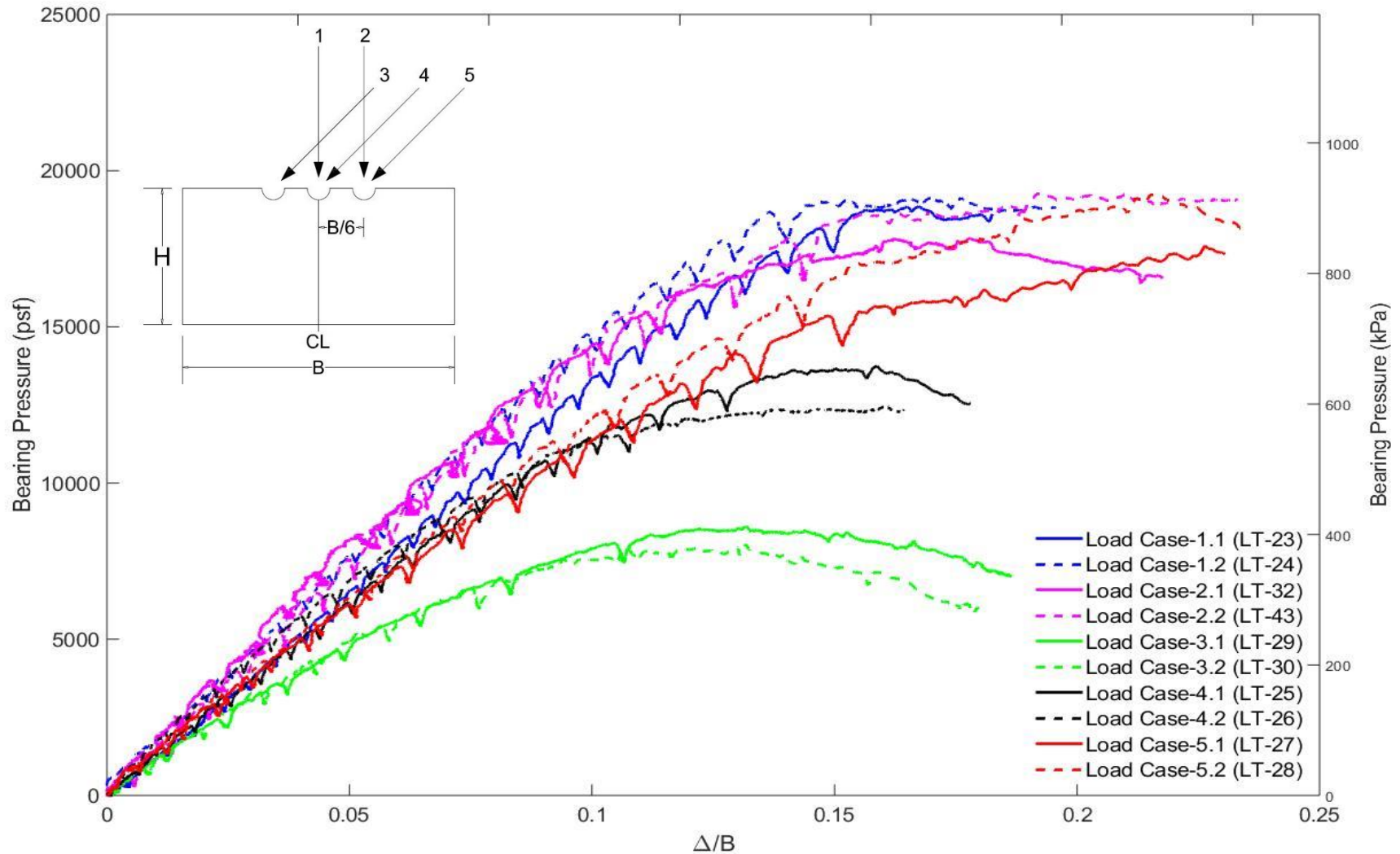


Name	Load Case	D <sub>r</sub> (%)	γ (pcf)	φ (degree)	Measured-qu (psf)	Embedment Depth (D <sub>f</sub> )	Eccentricity	Inclination	Series #
LT-41	3	96.65	108.17	36.42	10460	0.5B	B/6	0.10	1
LT-42	3	97.10	108.27	36.48	13400	0.5B	B/6	0.10	2
LT-43	2	96.71	108.19	36.43	17830	0	B/6	0	3
LT-44	1	95.70	107.97	36.28	29540	0.5B	0	0	3
LT-45	4	95.70	107.97	36.28	7596	0	0	0.25	1
LT-46	4	96.41	108.12	36.39	5681	0	B/6	0.25	2
LT-47	5	95.22	107.87	36.21	14590	0	B/6	-0.25	1
LT-48	5	94.99	107.82	36.18	13740	0	B/6	-0.25	2
LT-49	3	95.89	108.01	36.31	3547	0	B/6	0.25	1
LT-50*	3	-	-	-	-	-	-	-	-
LT-51	4	94.63	107.74	36.13	12800	0.5B	B/6	0.25	1
LT-52	4	97.06	108.26	36.48	12650	0.5B	B/6	0.25	2
LT-53	5	95.56	107.94	36.26	25410	0.5B	B/6	-0.25	1
LT-54	5	95.22	107.87	36.21	22660	0.5B	B/6	-0.25	2
LT-55	3	95.77	107.98	36.29	7242	0.5B	B/6	0.25	1
LT-56	3	94.94	107.81	36.17	9037	0.5B	B/6	0.25	2
LT-57	3	95.00	107.82	36.18	3684	0	B/6	0	3

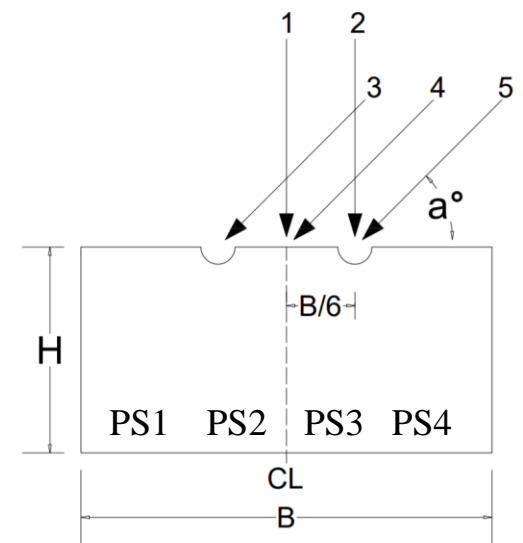
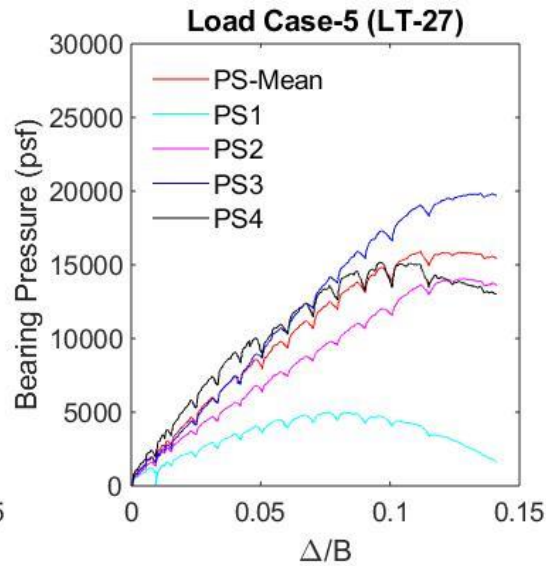
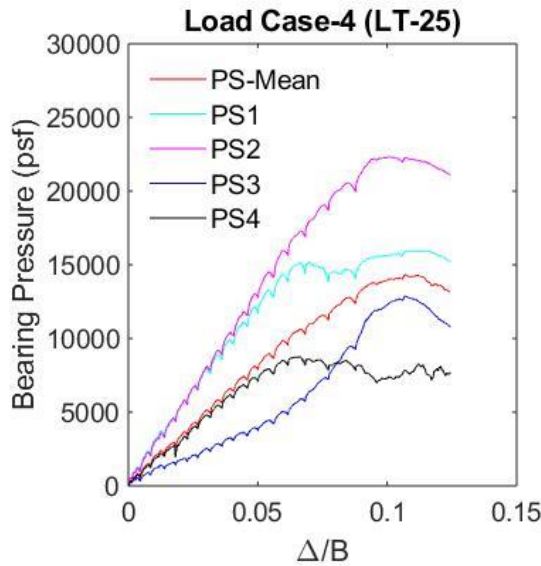
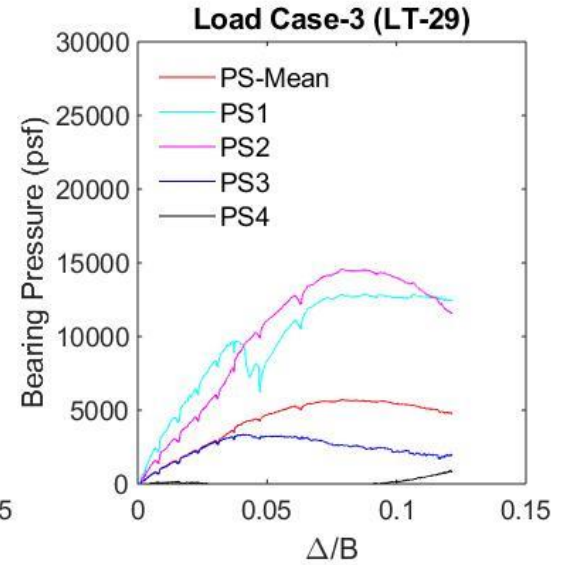
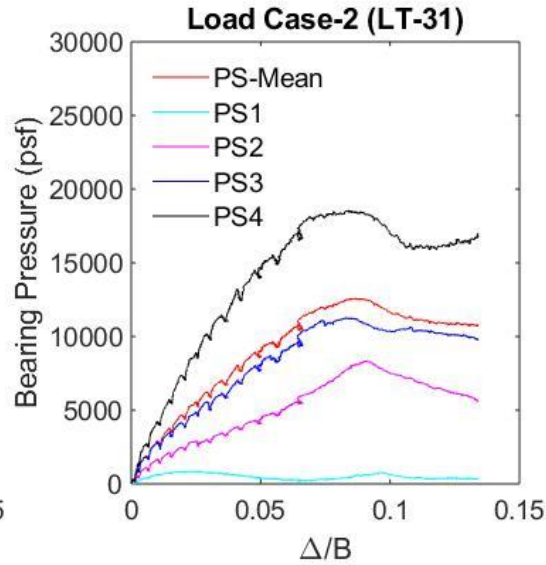
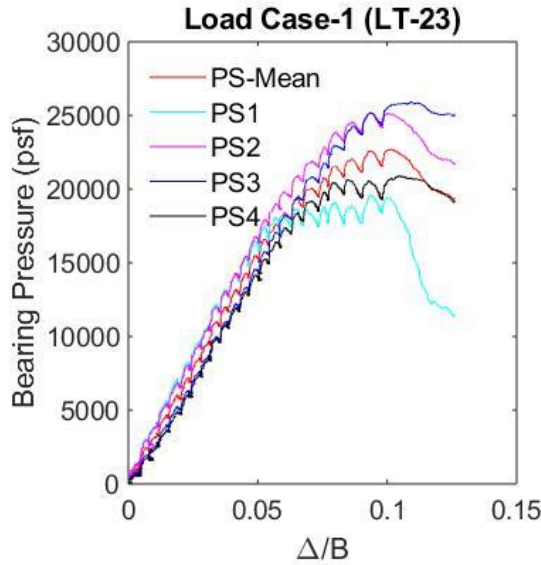
\*\* Load test excluded from analysis due to instrumentation malfunction

# Pressure vs. Displacement Plot-VD (Df=0 and L/A=0.10)

Bearing Capacity Equation:  $q_n = 0.5\gamma B N_\gamma S_\gamma i_\gamma$

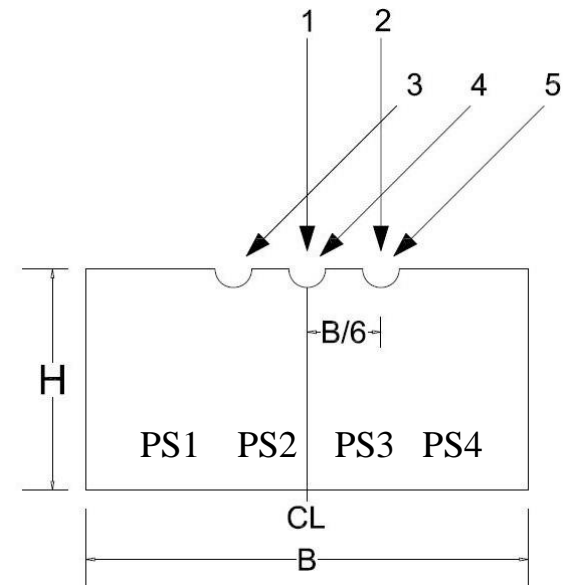
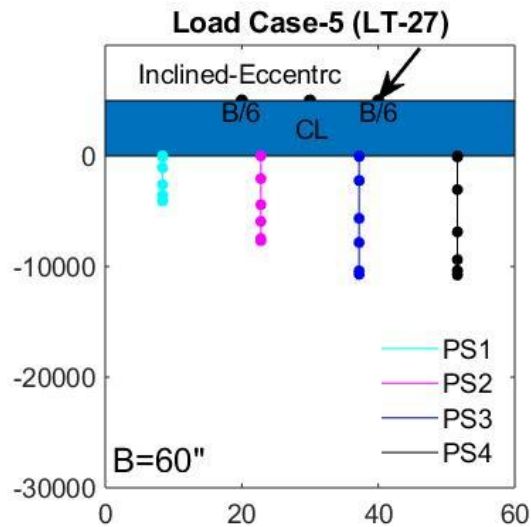
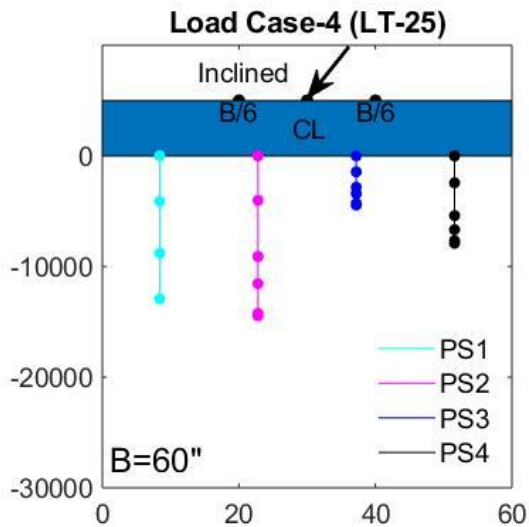
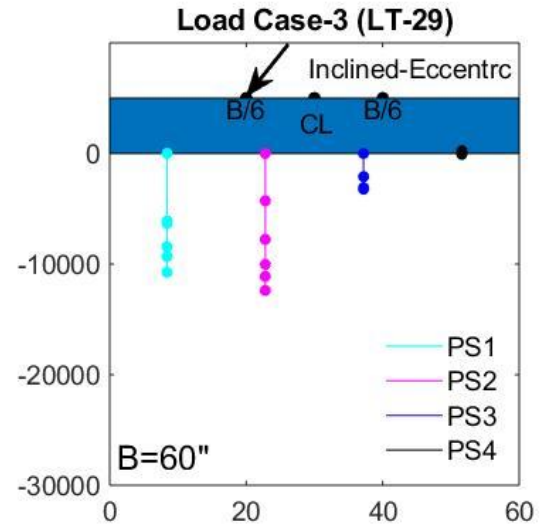
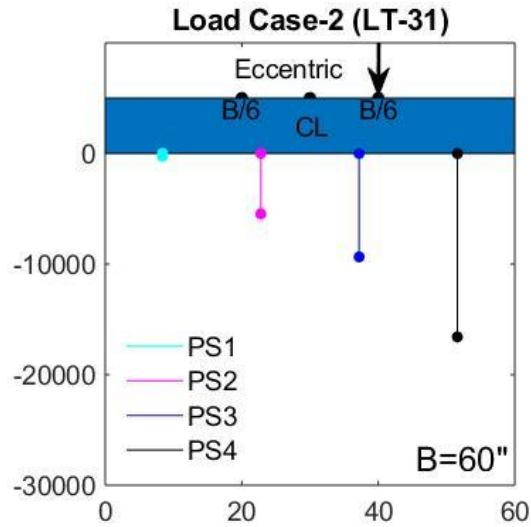
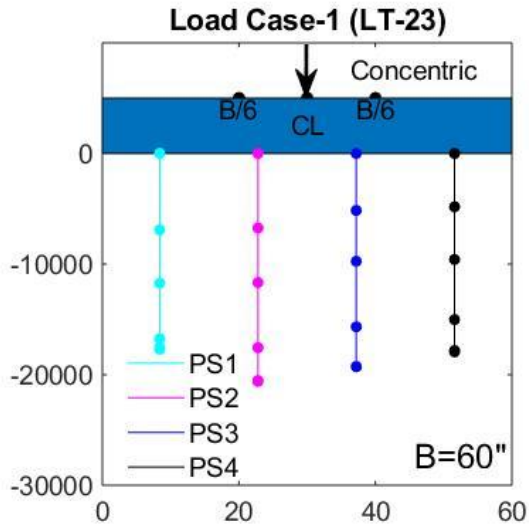


# Pressure vs. Displacement Plot (Df=0 and L/A=0.10)





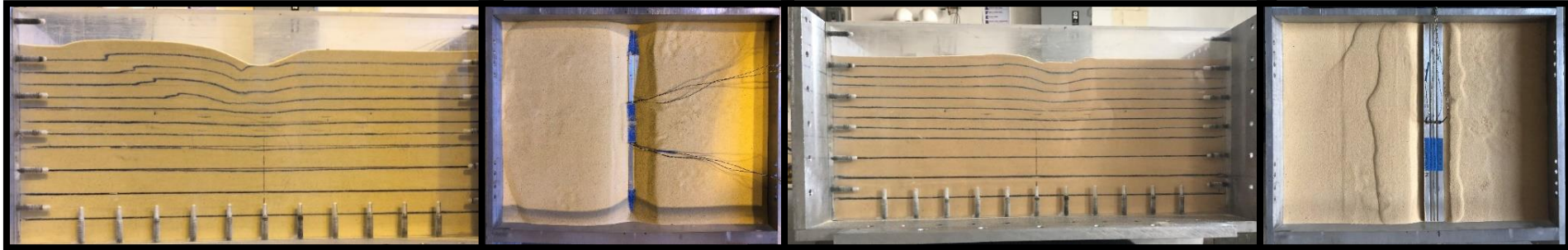
# Pressure Distribution Plot-VD (Df=0 and L/A=0.10)



# FAILURE SURFACE IMAGES-VD (Df=0 and L/A=0.10)

Load Case -1 (LT-24) Df=0

Load Case -4 (LT-26)

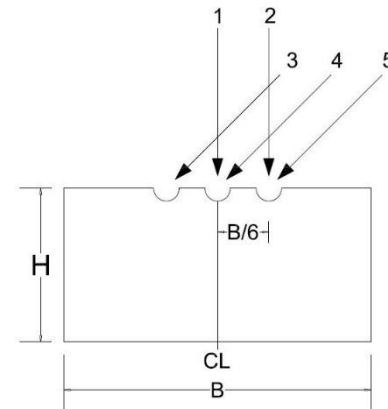


Load Case -2 (LT-31)

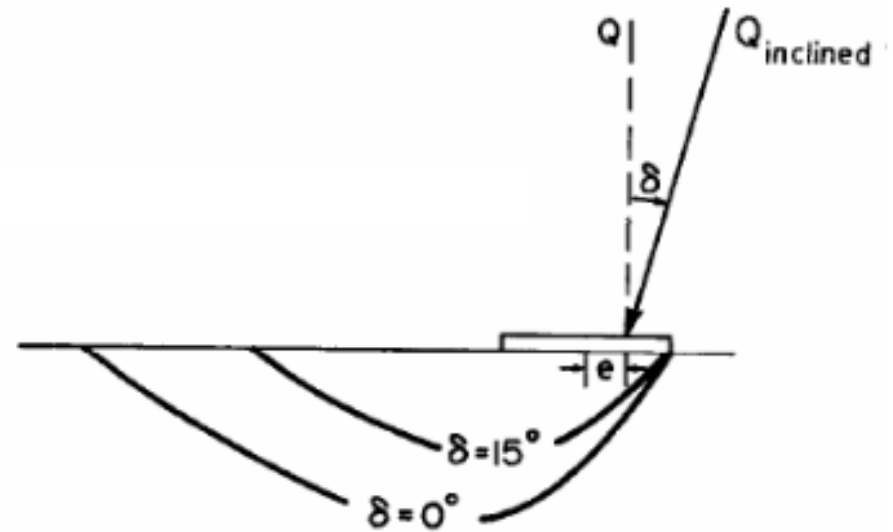
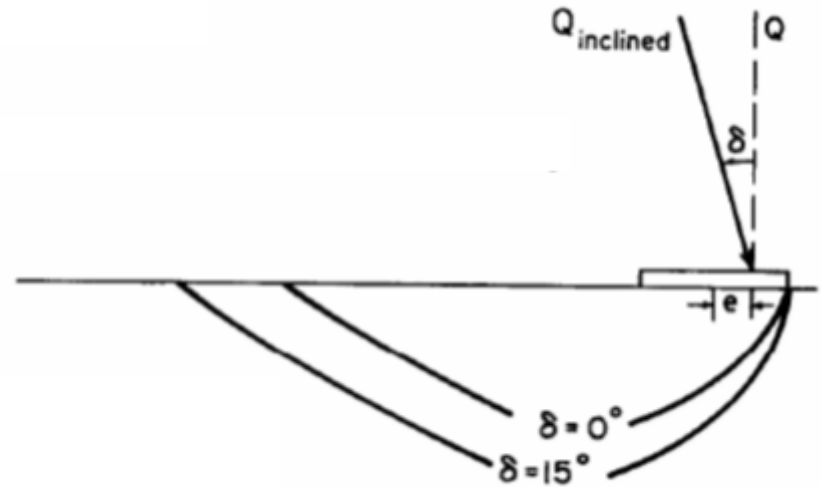
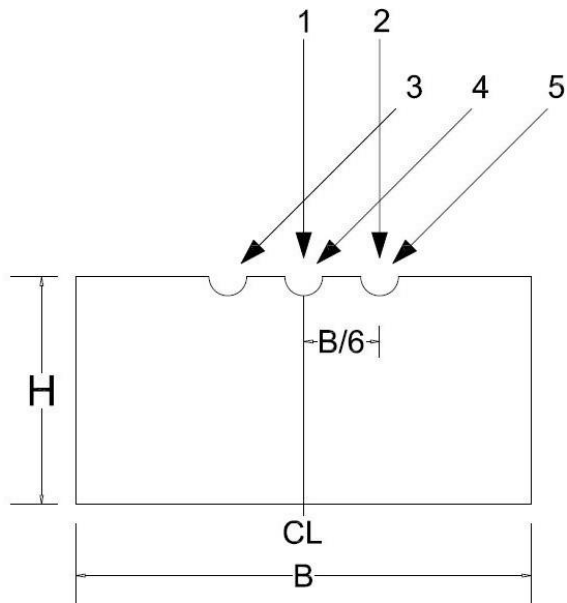
Load Case -5 (LT-28)



Load Case -3 (LT-30)

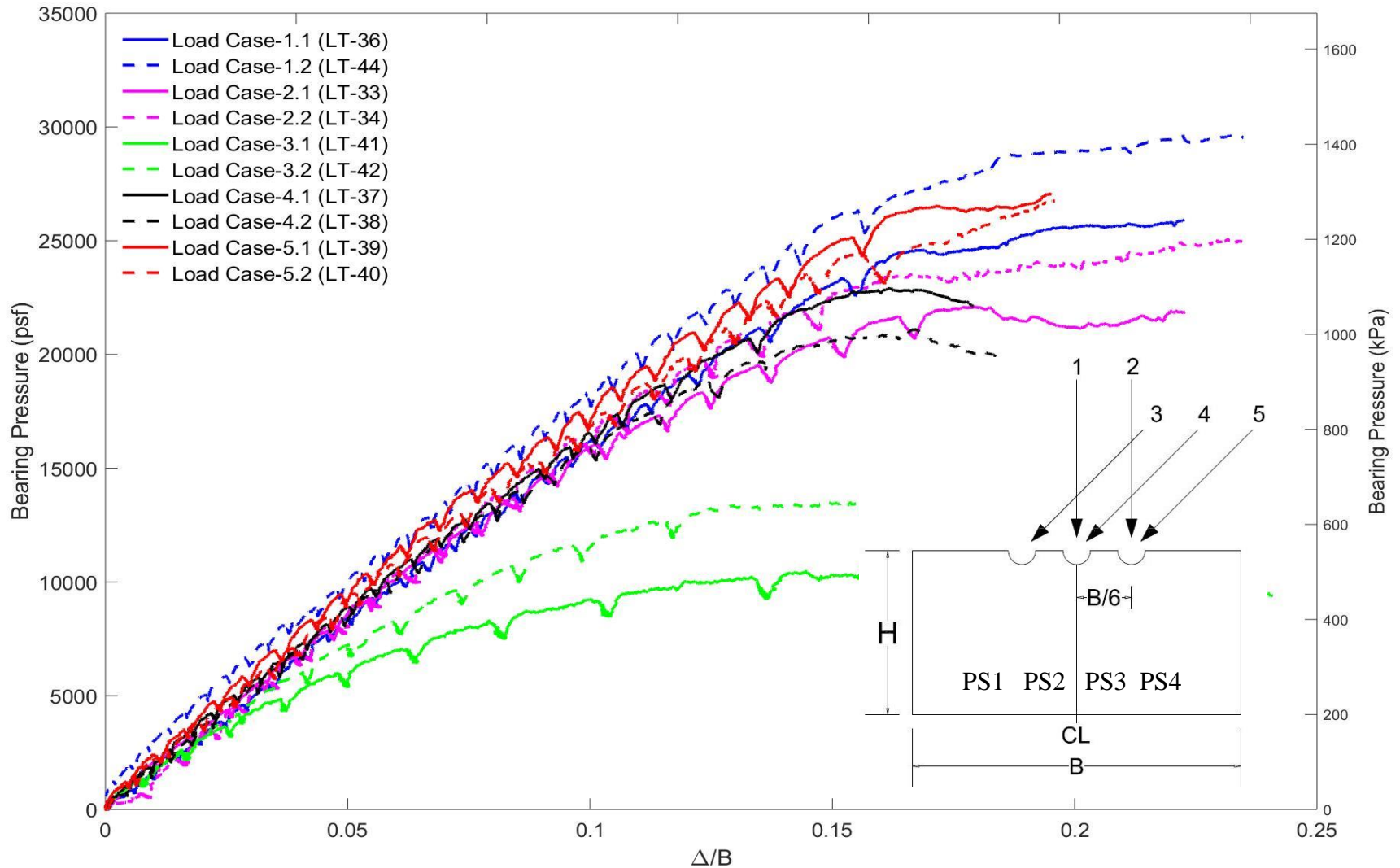


# THEORETICAL FAILURE SURFACE



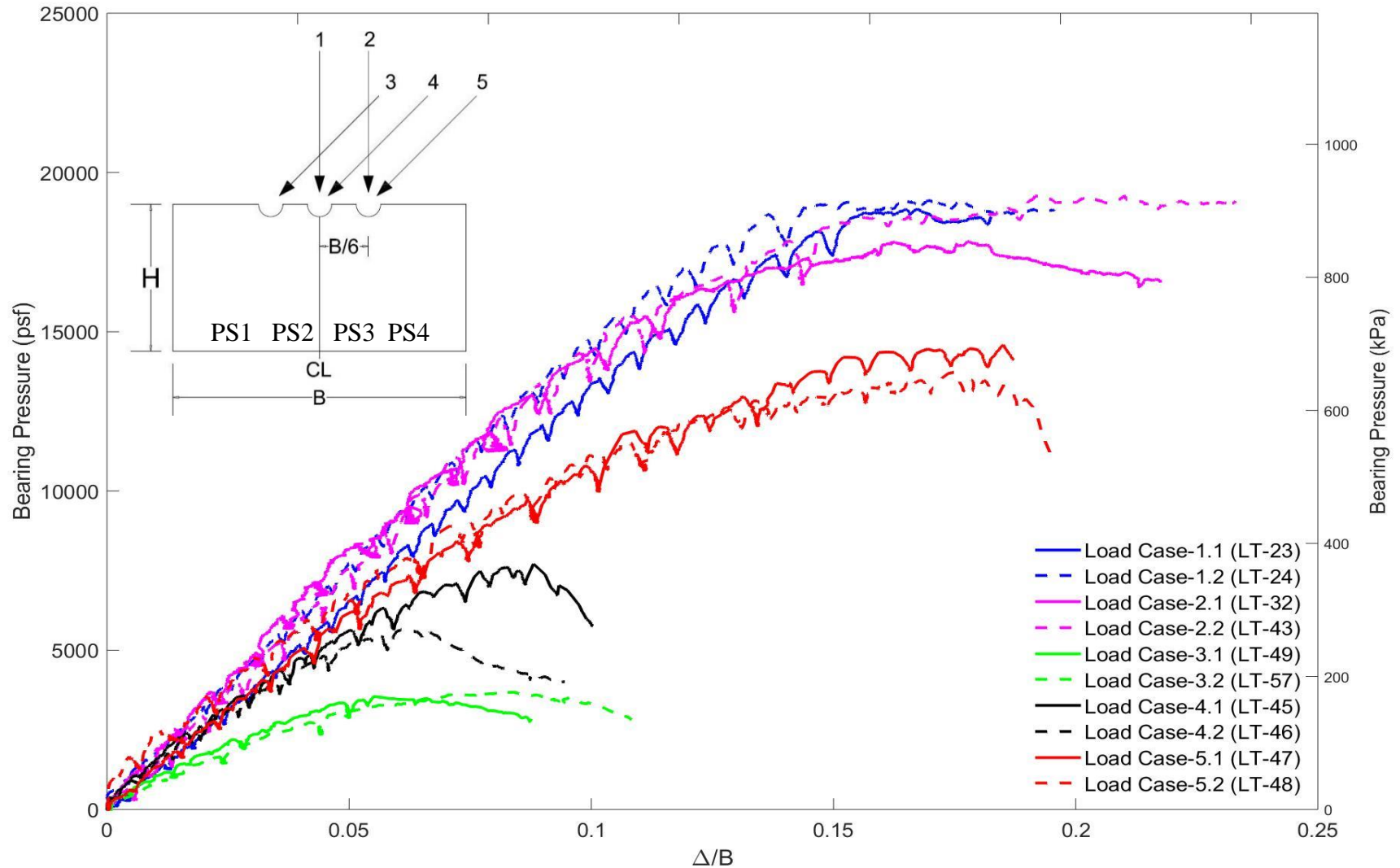
# Pressure vs. Displacement Plot-VD (Df=0.5B and L/A=0.10)

$$q_n = \gamma D_f N_q S_q d_q i_q + 0.5 \gamma B N_\gamma S_\gamma i_\gamma$$



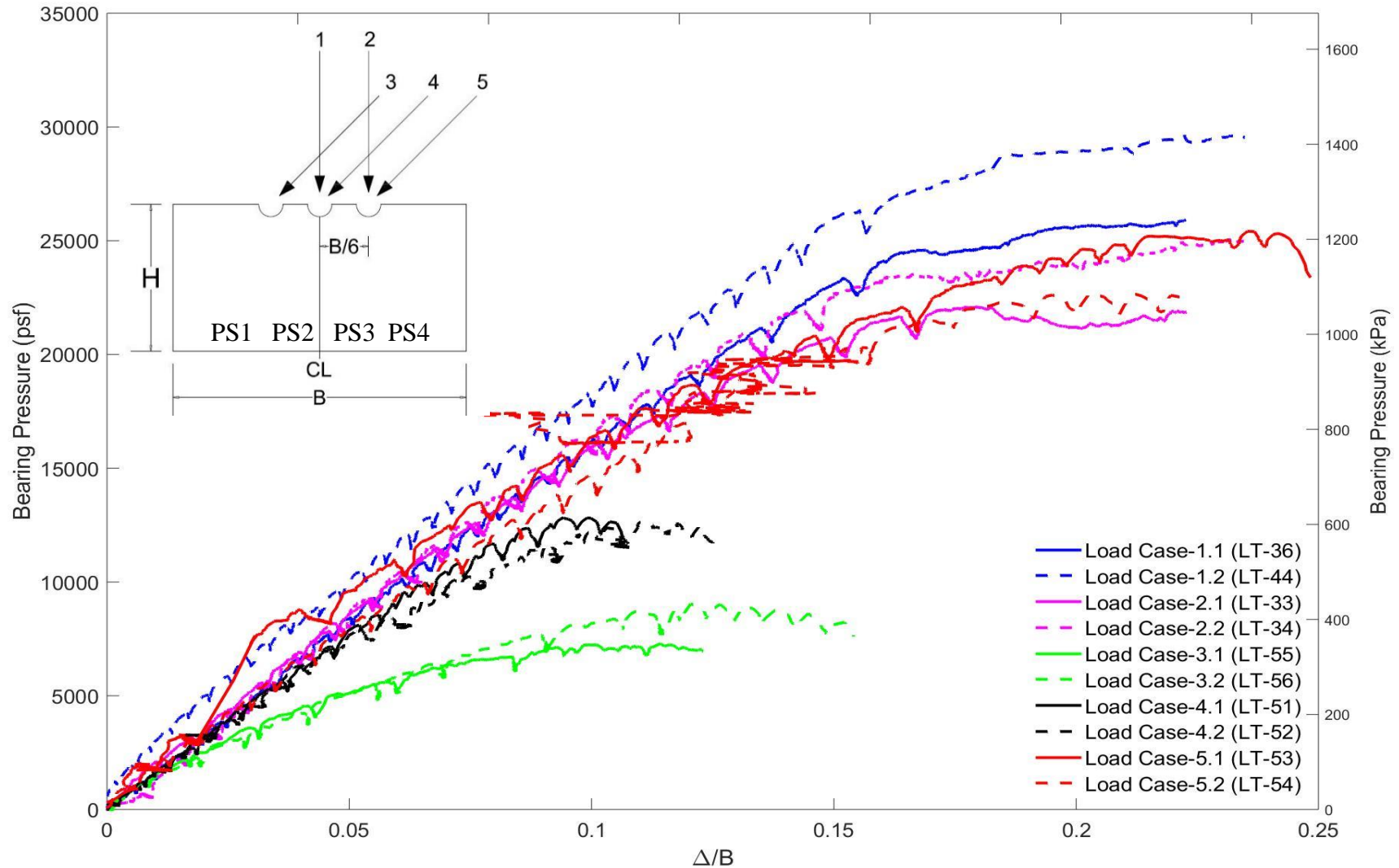
# Pressure vs. Displacement Plot-VD (Df=0 and L/A=0.25)

Bearing Capacity Equation:  $q_n = 0.5\gamma B N_\gamma S_\gamma i_\gamma$



# Pressure vs. Displacement Plot-VD (Df=0.5B and L/A=0.25)

$$q_n = \gamma D_f N_q S_q d_q i_q + 0.5 \gamma B N_\gamma S_\gamma i_\gamma$$



# LOAD TEST ON RECTANGULAR FOUNDATION (L/B=10)-MB



Name	Load Case	$D_r$ (%)	$\gamma$ (pcf)	$\phi$ (degree)	Measured-qu (psf)	Embedment Depth ( $D_f$ )	Eccentricity	Inclination	Series #
LT-58	1	63.65	101.50	31.69	10360	0	0	0	1
LT-59	1	64.08	101.58	31.75	10670	0	0	0	2
LT-60	1	63.79	101.52	31.71	14120	0.5B	0	0	1
LT-61	1	63.40	101.45	31.66	15360	0.5B	0	0	2
LT-62	2	63.80	101.53	31.71	11280	0	B/6	0	1
LT-63	2	64.16	101.59	31.77	11420	0	B/6	0	2
LT-64	2	63.88	101.54	31.73	15780	0.5B	B/6	0	1
LT-65	2	64.37	101.63	31.8	15240	0.5B	B/6	0	2
LT-66	3	64.56	101.67	31.82	6080	0	B/6	0.10	1
LT-67	3	64.26	101.61	31.78	6503	0	B/6	0.10	2
LT-68	3	64.23	101.61	31.78	10050	0.5B	B/6	0.10	1
LT-69	3	63.17	101.41	31.62	8315	0.5B	B/6	0.10	2
LT-70	4	64.25	101.61	31.78	6155	0	0	0.10	1
LT-71	4	63.27	101.42	31.64	6531	0	0	0.10	2
LT-72	4	63.52	101.47	31.68	11070	0.5B	0	0.10	1
LT-73	4	64.03	101.57	31.75	12570	0.5B	0	0.10	2
LT-74	5	64.39	101.64	31.80	11880	0	B/6	-0.10	1
LT-75	5	64.08	101.58	31.76	11380	0	B/6	-0.10	2
LT-76	5	63.85	101.54	31.72	16650	0.5B	B/6	-0.10	1
LT-77	5	63.74	101.51	31.71	17540	0.5B	B/6	-0.10	2

\*\* Load test excluded from analysis due to instrumentation malfunction

# LOAD TEST ON RECTANGULAR FOUNDATION (L/B=10)-MB



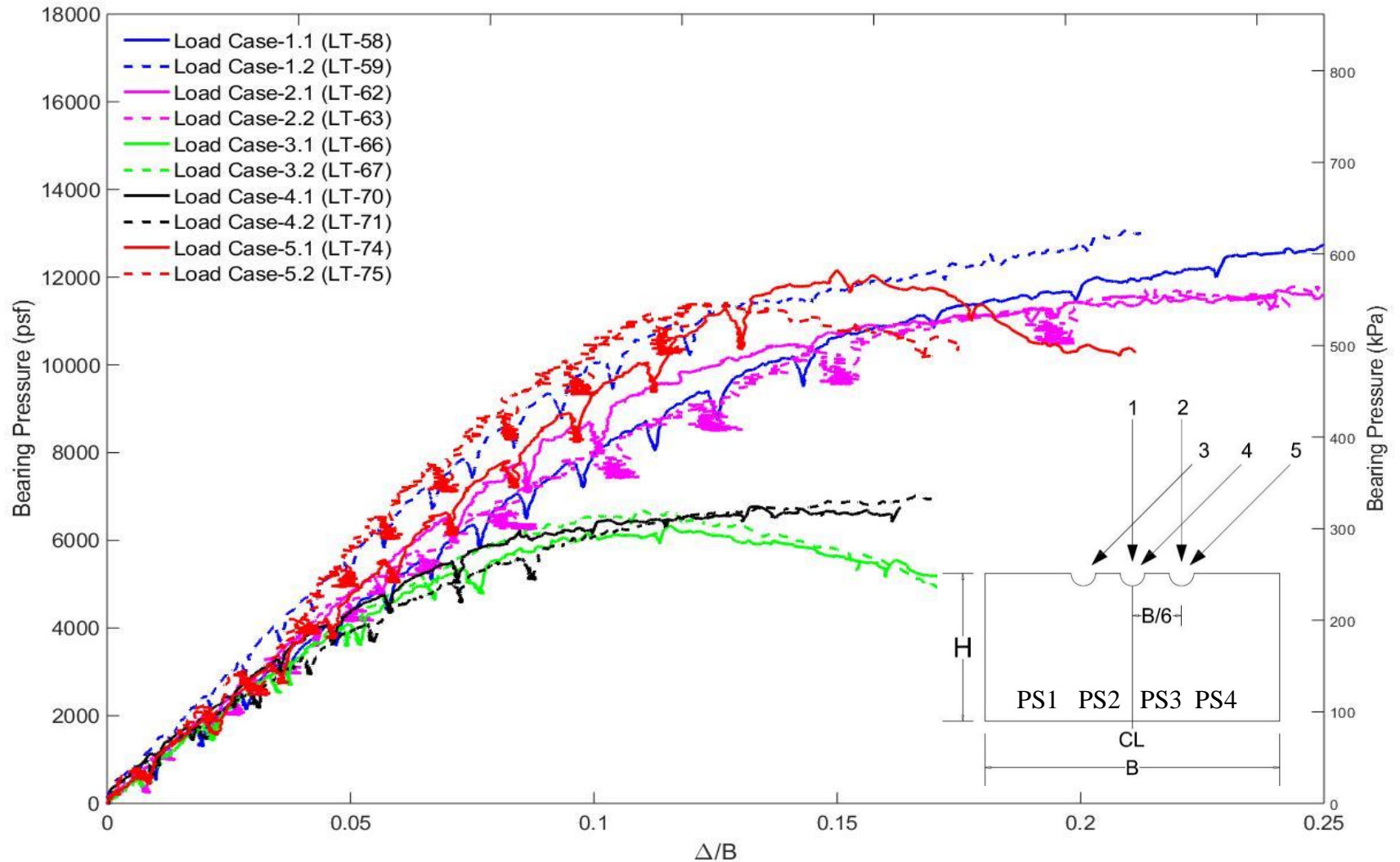
Name	Load Case	$D_r$ (%)	$\gamma$ (pcf)	$\phi$ (degree)	Measured- qu (psf)	Embedment Depth ( $D_f$ )	Eccentricity	Inclination	Series #
LT-78	3	63.53	101.47	31.68	3140	0	B/6	0.25	1
LT-79	3	63.74	101.51	31.71	2124	0	B/6	0.25	2
LT-80	3	64.24	101.61	31.78	8012	0.5B	B/6	0.25	1
LT-81	3	63.59	101.49	31.68	6356	0.5B	B/6	0.25	2
LT-82	4	63.32	101.43	31.65	3023	0	0	0.25	1
LT-83	4	63.69	101.51	31.7	2612	0	0	0.25	2
LT-84	4	64.19	101.6	31.77	9322	0.5B	0	0.25	1
LT-85	4	64.06	101.58	31.75	8969	0.5B	0	0.25	2
LT-86	5	63.74	101.51	31.71	9169	0	B/6	-0.25	1
LT-87	5	63.66	101.5	31.7	9818	0	B/6	-0.25	2
LT-88	5	63.34	101.44	31.65	13210	0.5B	B/6	-0.25	1
LT-89	5	63.92	101.55	31.73	12630	0.5B	B/6	-0.25	2

\*\* Load test excluded from analysis due to instrumentation malfunction



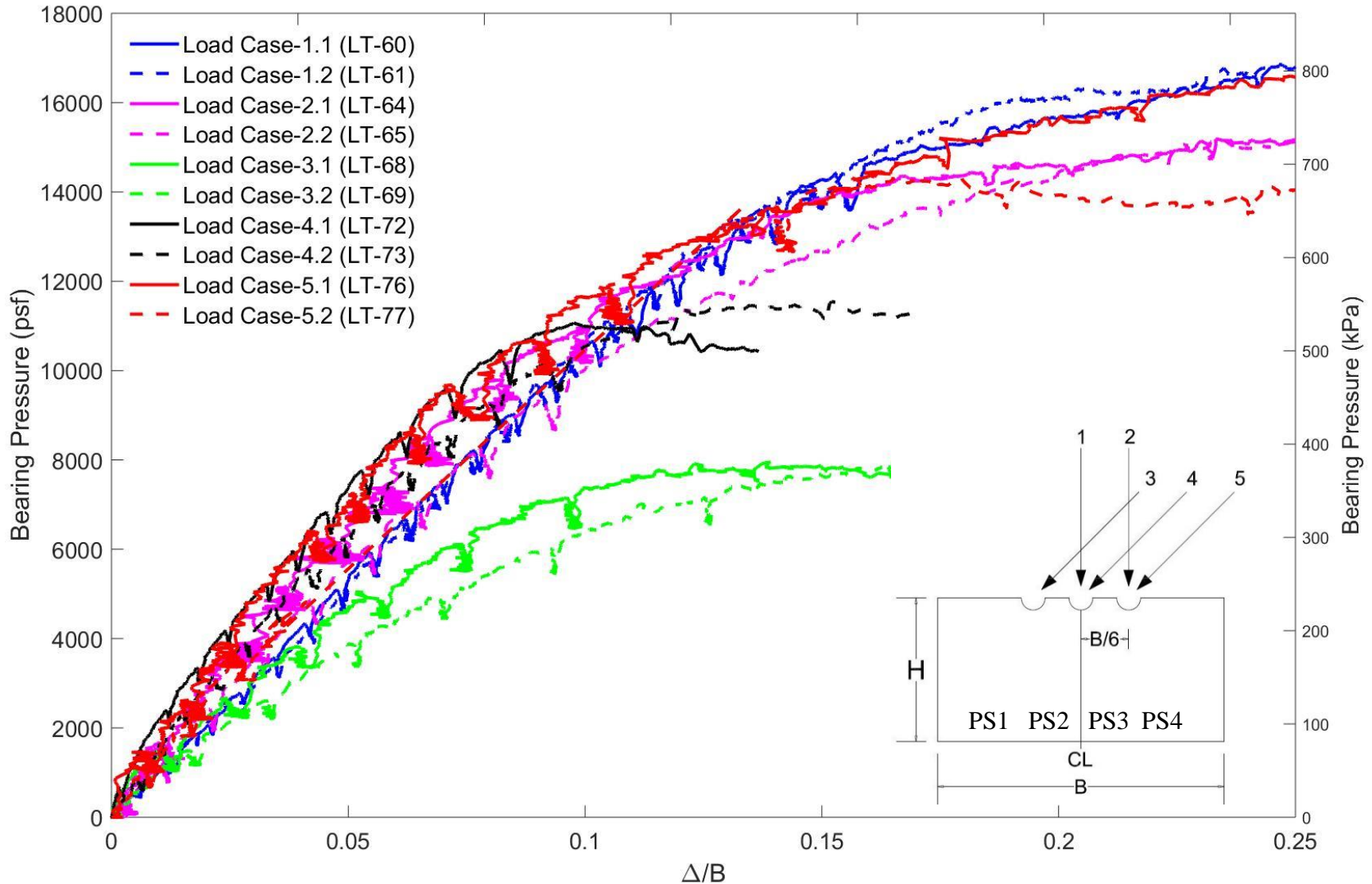
# Pressure vs. Displacement Plot-MD (Df=0 and L/A=0.1)

Bearing Capacity Equation:  $q_n = 0.5\gamma B N_\gamma S_\gamma i_\gamma$



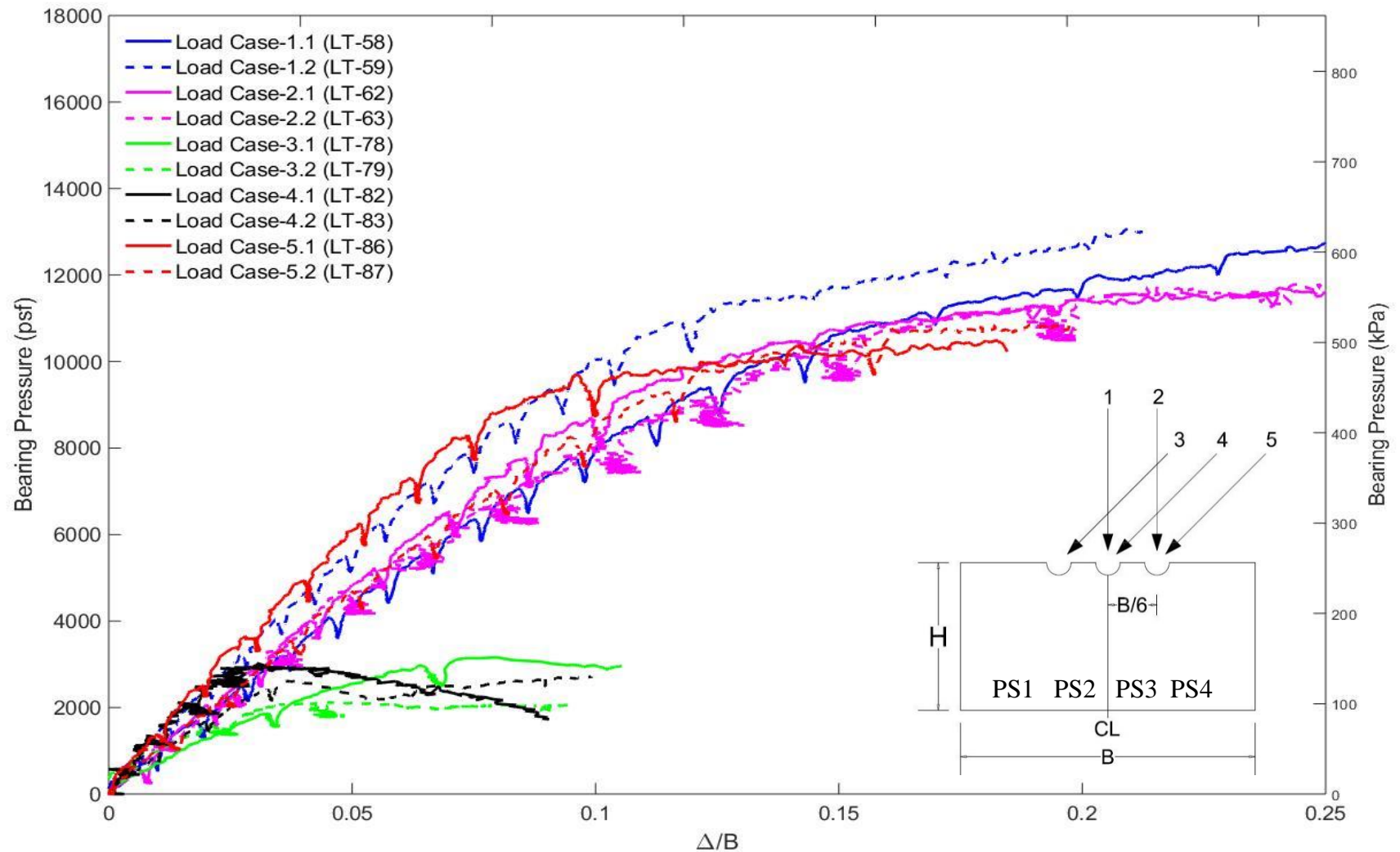
# Pressure vs. Displacement Plot-MD (Df=0.5B and L/A=0.10)

Bearing Capacity Equation:  $q_n = \gamma D_f N_q S_q d_q i_q + 0.5 \gamma B N_\gamma S_\gamma i_\gamma$



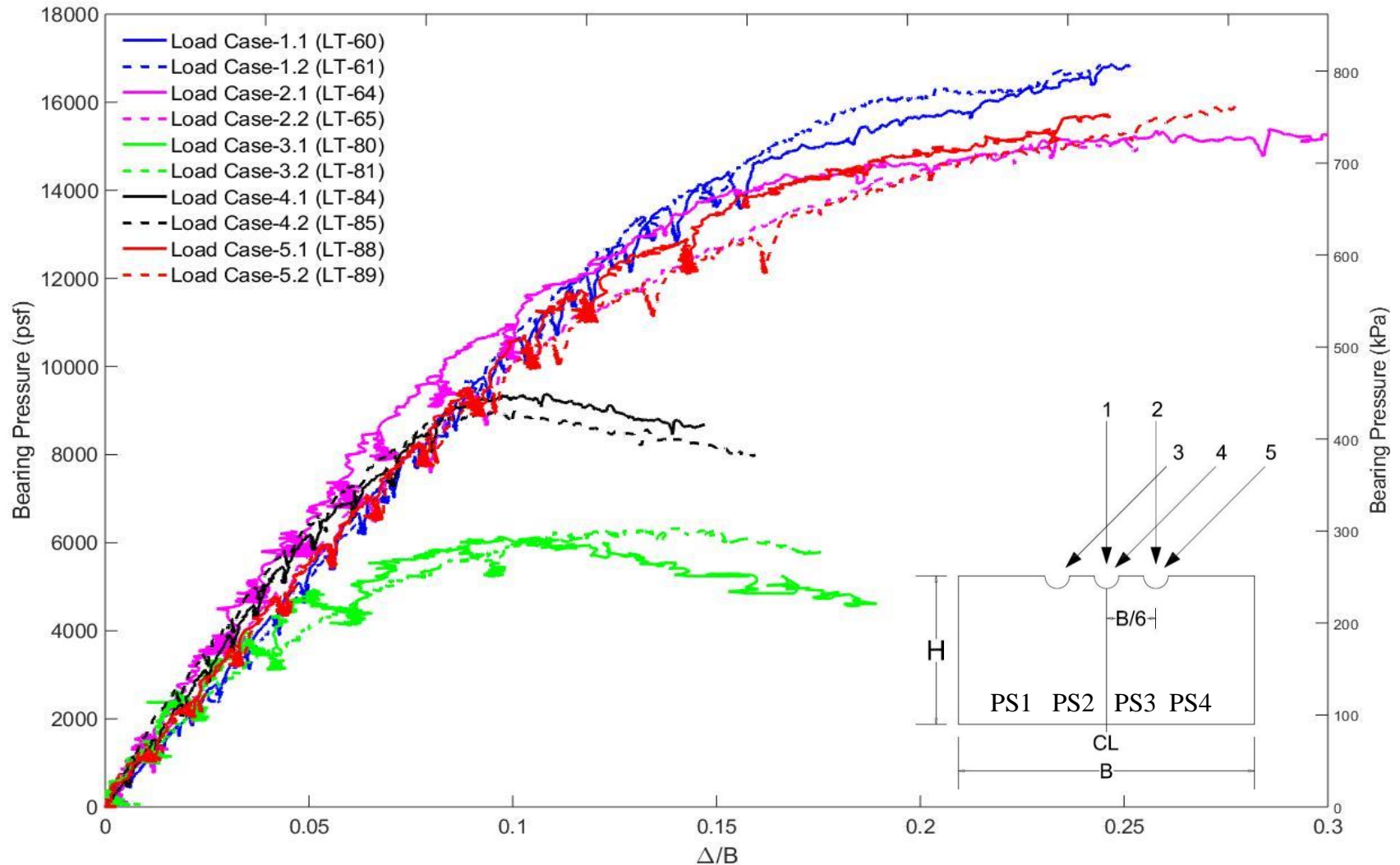
# Pressure vs. Displacement Plot-MD (Df=0 and L/A=0.25)

Bearing Capacity Equation:  $q_n = 0.5\gamma BN_\gamma S_\gamma i_\gamma$



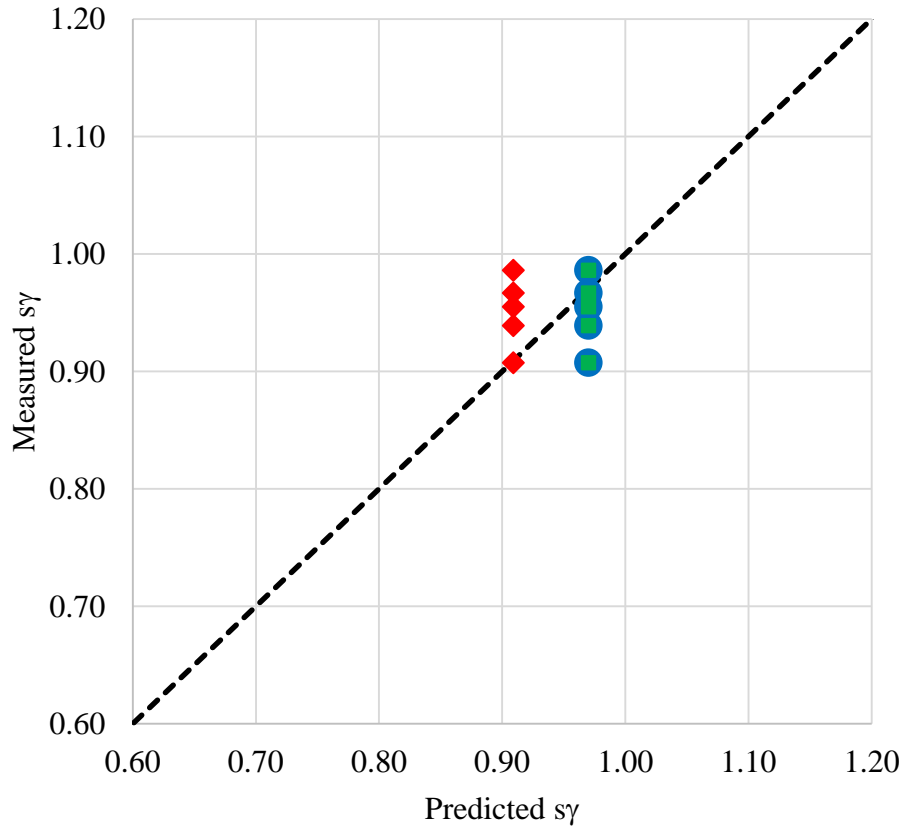
# Pressure vs. Displacement Plot-MD (Df=0.5B and L/A=0.10)

$$q_n = \gamma D_f N_q S_q d_q i_q + 0.5 \gamma B N_\gamma S_\gamma i_\gamma$$

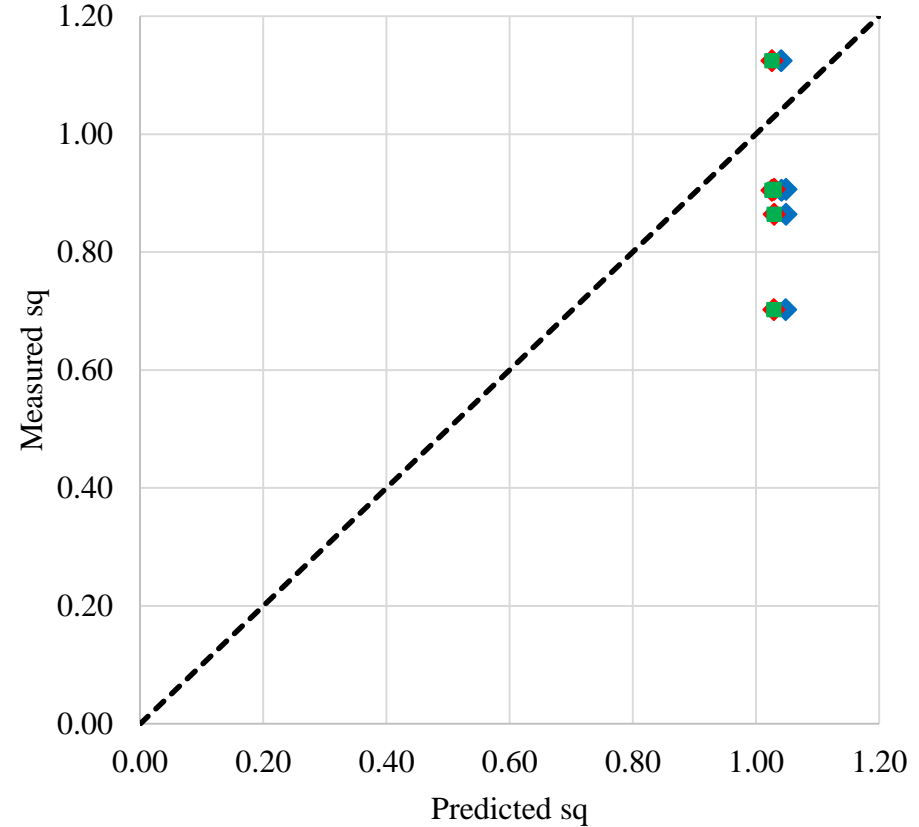


# SHAPE & DEPTH FACTORS (L/B=10)

Bearing Capacity Factor- $s_\gamma$



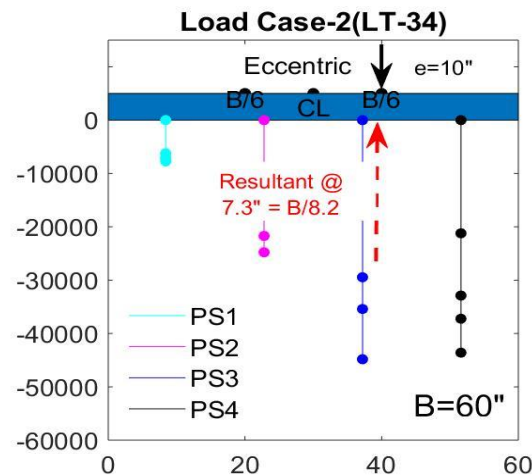
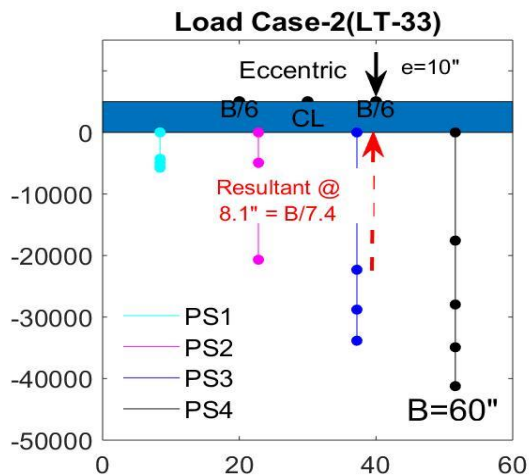
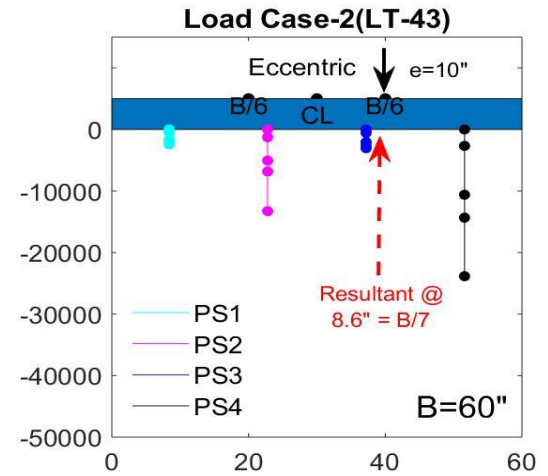
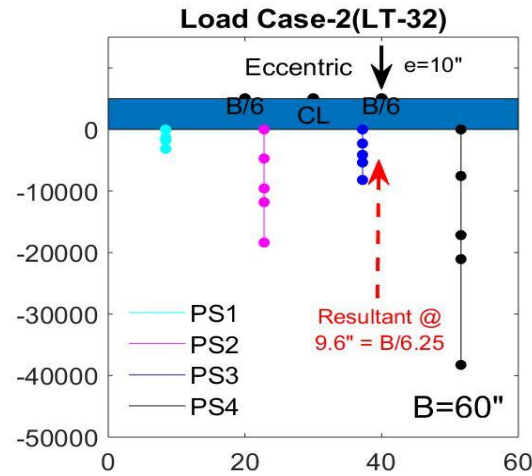
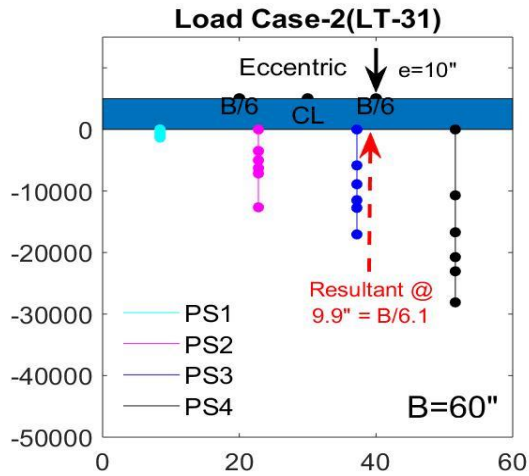
Bearing Capacity Factor- $s_q$



- Vesic'-sg (L/B=10)
- ◆ Meyerhof-sg (L/B=10)
- Paikowsky-sg (L/B=10)
- 45 degree

- ◆ Vesic'-sq (L/B=10)
- ◆ Meyerhof-sq (L/B=10)
- Paikowsky-sq (L/B=10)
- 45 degree

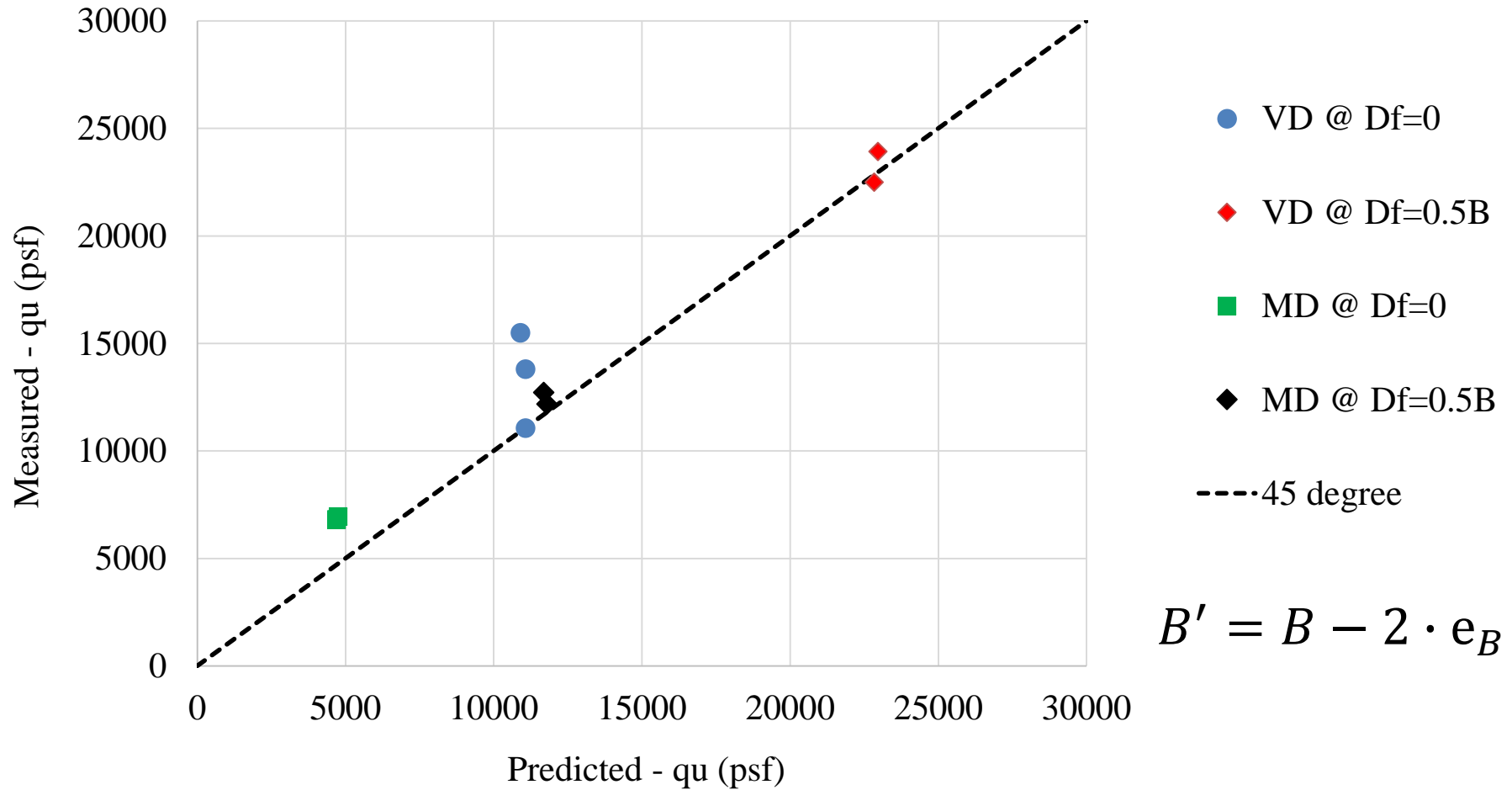
# Pressure Distribution for Eccentric Load Case



$$B' = B - 2 \cdot e_B$$

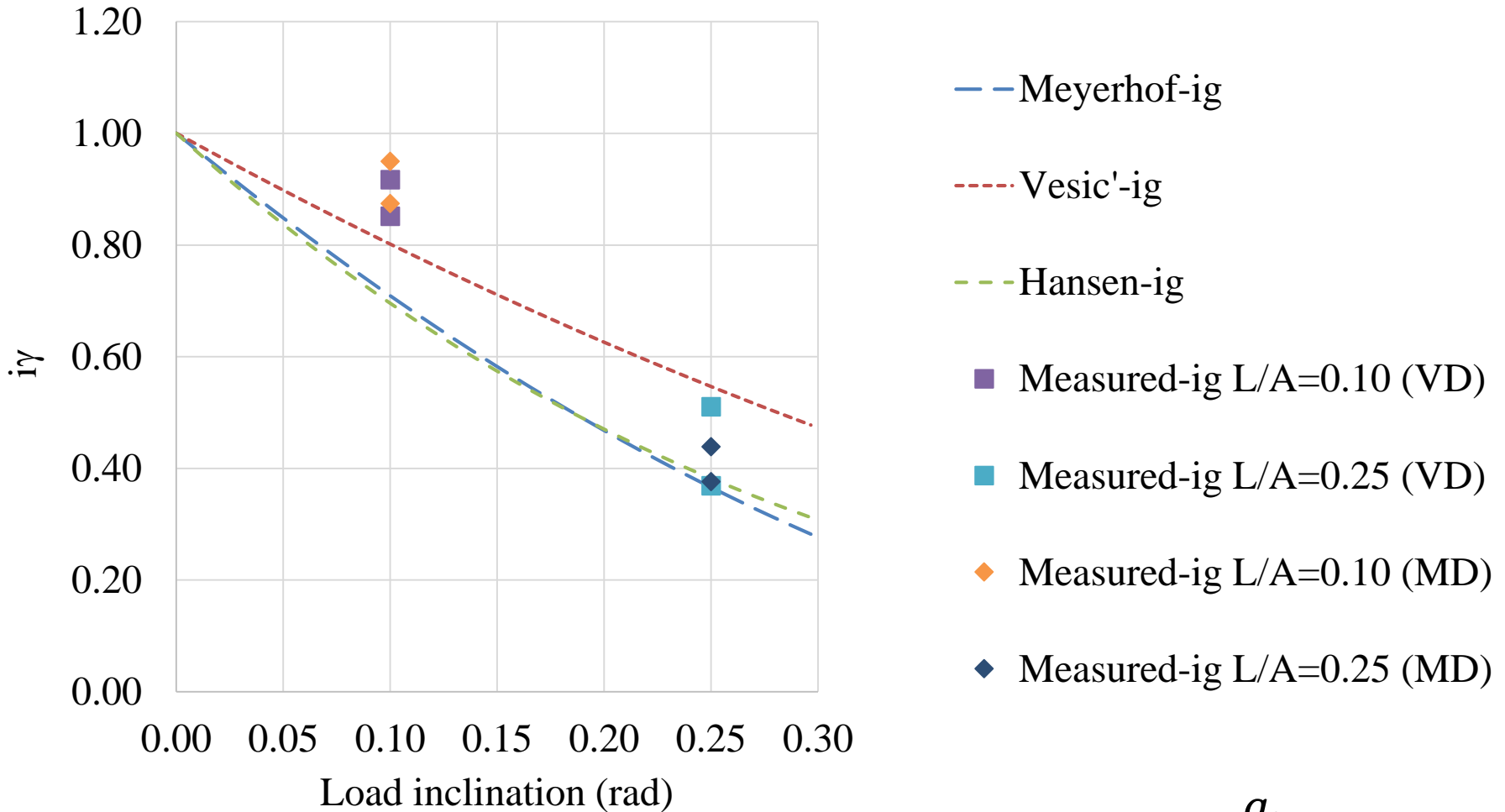
Measured Eccentricity	Design Eccentricity	Foundation Rotation (degree)
B/6.1	B/6	5.65
B/6.25	B/6	4.41
B/7	B/6	4.69
B/7.4	B/6	4.51
B/8.2	B/6	4.60

# Effect of Eccentricity on Surface & Embedded Footing



$$B' = B - 2 \cdot e_B$$

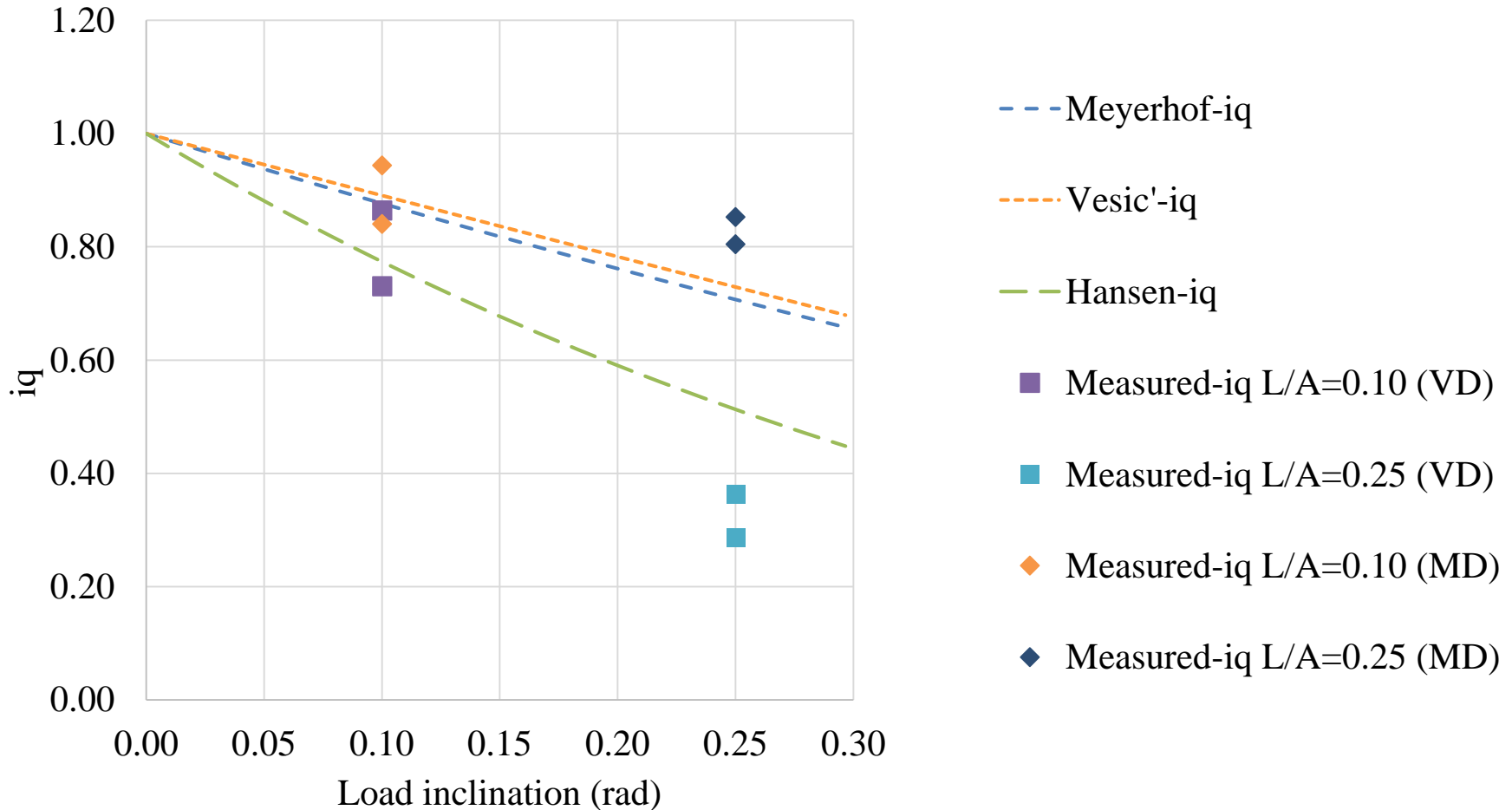
# Effect of Load Inclination on Surface Footing



$$i_\gamma = \frac{q_u}{0.5\gamma B N_\gamma s_\gamma d_\gamma}$$

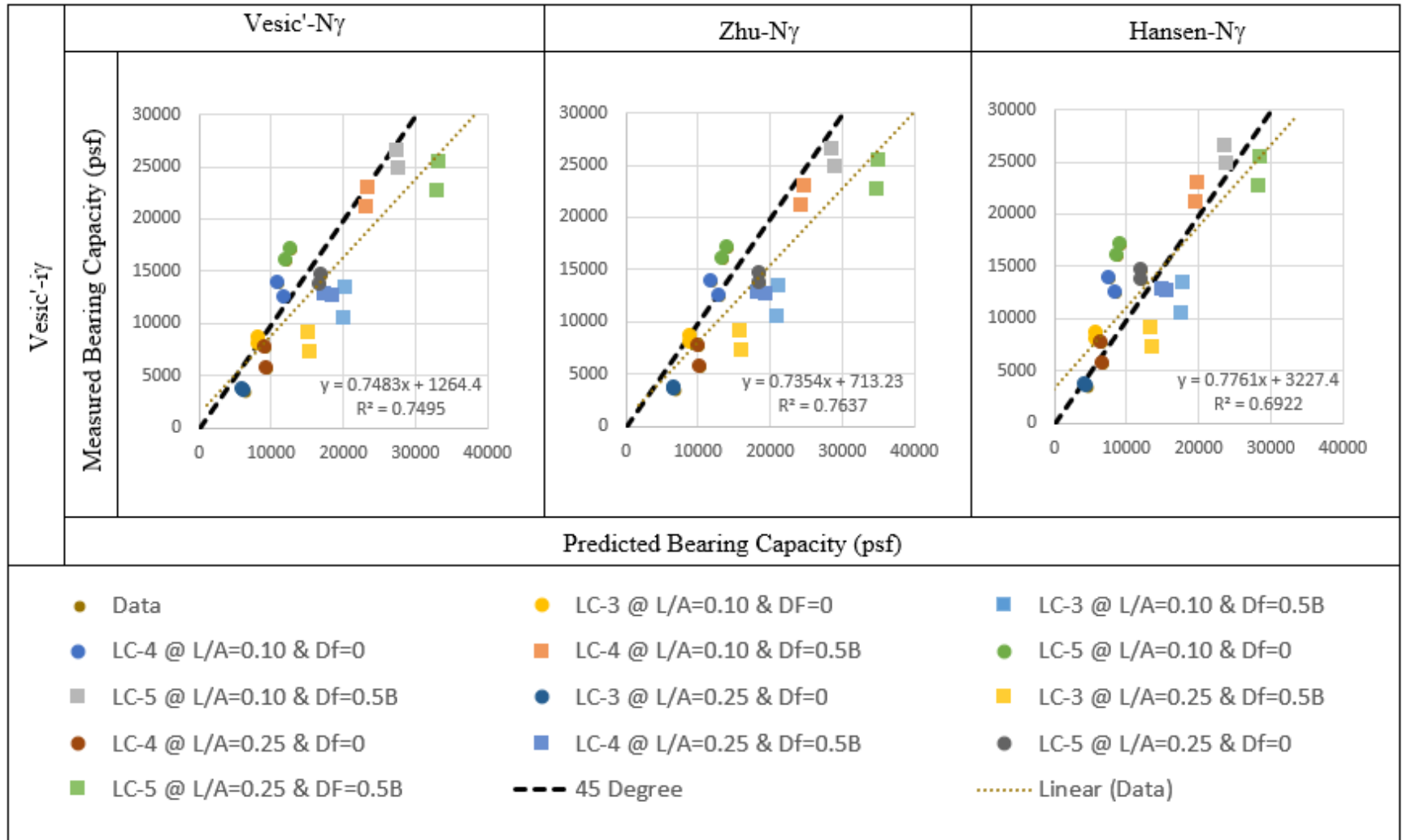


# Effect of Load Inclination on Surface Footing

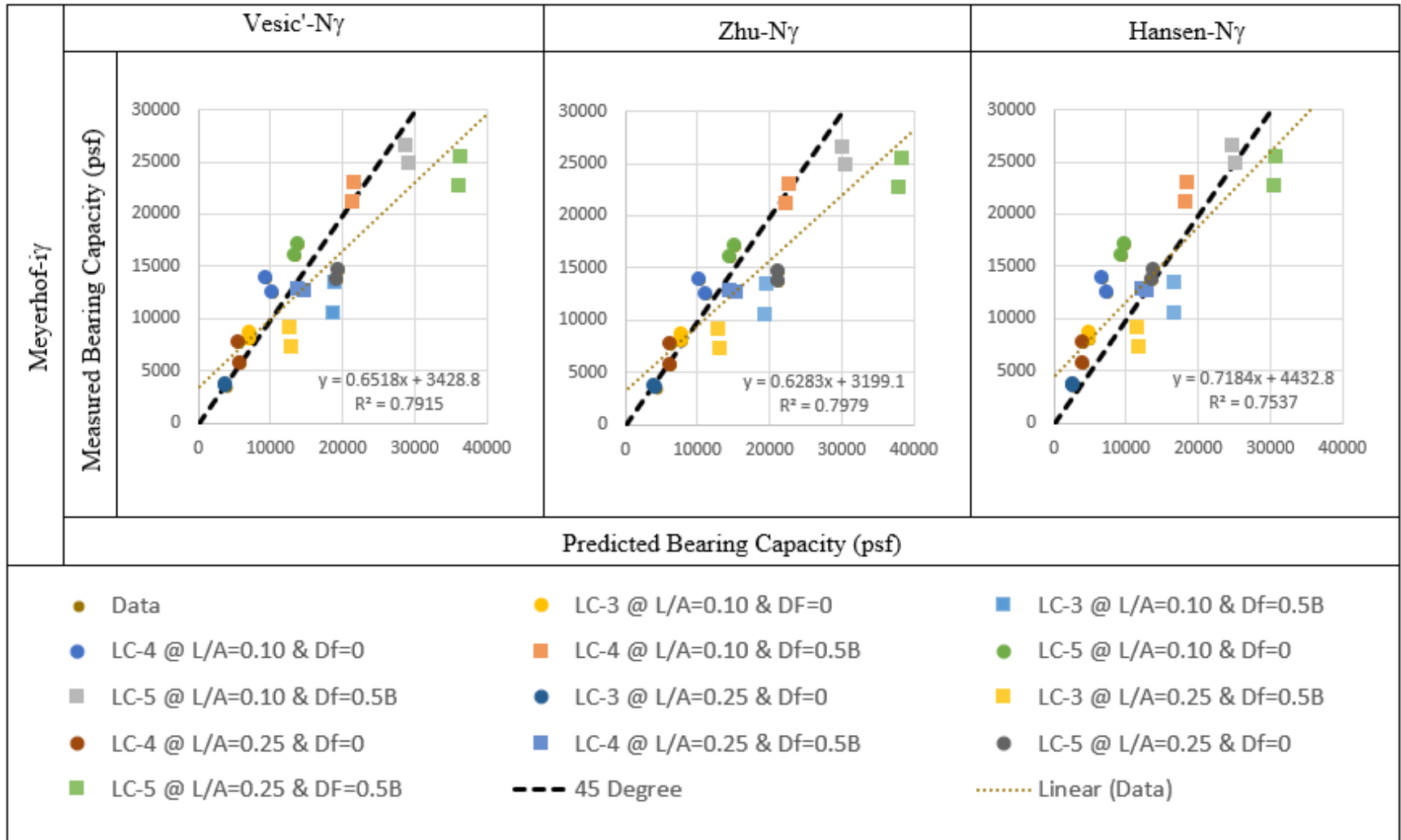


$$i_q = \frac{q_u - 0.5\gamma B N_\gamma s_\gamma d_\gamma i_\gamma}{D_f \gamma N_q s_q d_q}$$

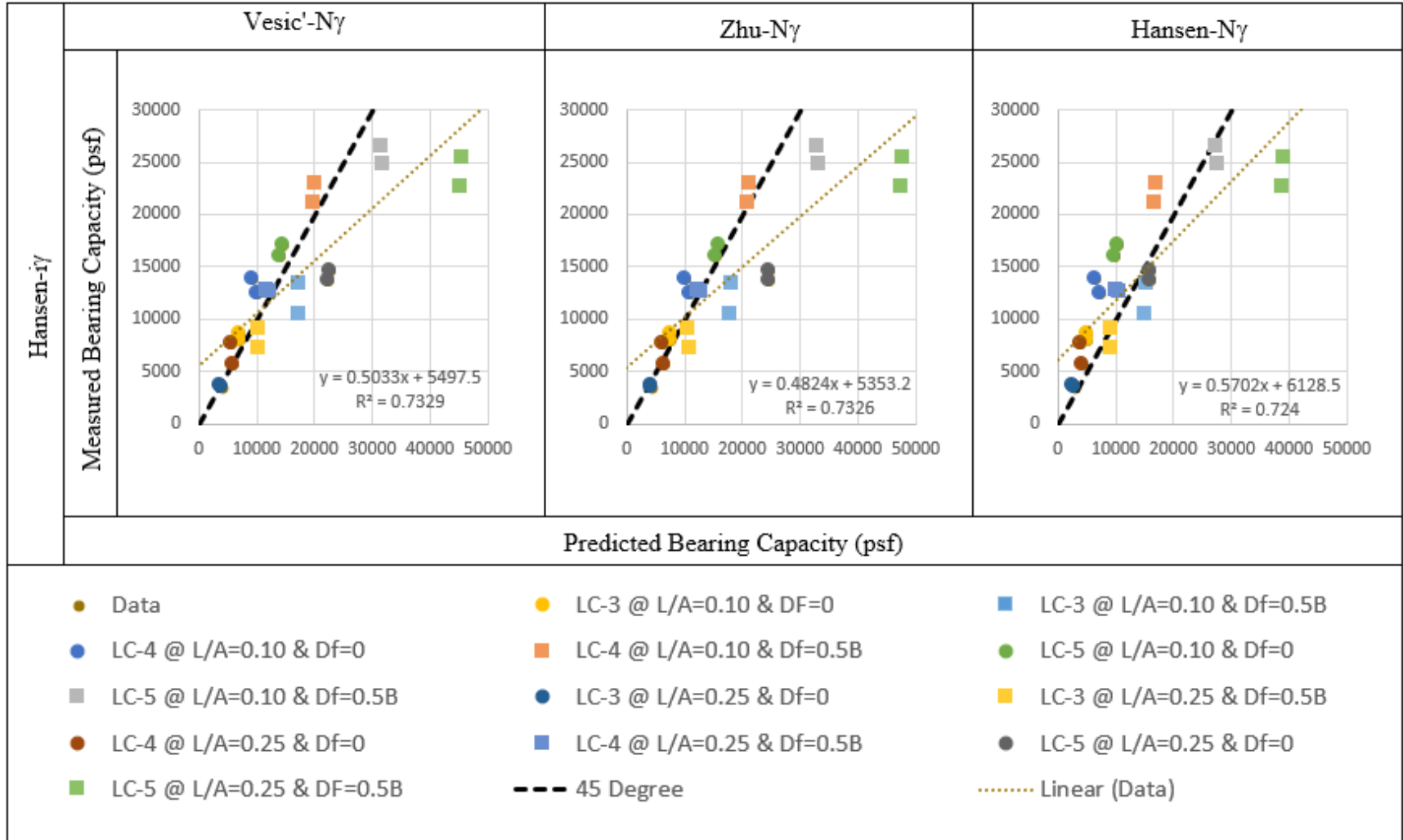
# Bearing Capacity Bias Plot for Vesic' - $i\gamma$ (VD)



# Bearing Capacity Bias Plot for Meyerhof - $i\gamma$ (VD)



# Bearing Capacity Bias Plot for Hansen - $i\gamma$ (VD)



# CONCLUSIONS

## Strip Foundation: (L/B=20)

- Bearing capacity factor- $N_q$  presented by Reissner, AASHTO Recommended is representative (Mean - 13% difference)
- Bearing capacity factor- $N_\gamma$  presented by Vesic' (1973), AASHTO Recommended and Zhu et al.(2001) are representative (Mean - 9.7% and 10.3% difference)
- Shape factors- $s_\gamma$  presented by Vesic' (1973), AASHTO Recommended are representative (< 4% error)
- Depth factors- $d_q$  and  $d_\gamma$  presented by Meyerhof (1963), AASHTO Recommended is representative (Mean - 9.3% difference)

# CONCLUSIONS CONTINUED



## Rectangular Footing L/B=10: (Very Dense)

- Load Case #1-Concentric loading
  - Df=0: **19,000 psf**
  - Df=0.5B: **29,000 psf**
- Load Case#2-Eccentric loading
  - Df=0: **17,800 psf** (93.7% of LC-1)
  - Df=0.5B: **23,400 psf** (80.7% of LC-1)

# CONCLUSIONS CONTINUED



## Rectangular Footing L/B=10: (Very Dense)

Load Case#3-Eccentric-Inclined loading, (+) to the direction of Inclination

- Df=0 & L/A=0.10: **8,150 psf** (42.9% of LC-1)
- Df=0.5B & L/A=0.10: **13,350 psf** (46.0% of LC-1)
- Df=0 & L/A=0.25: **3,500 psf** (18.4% of LC-1)
- Df=0.5B & L/A=0.25: **8,725 psf** (45.9% of LC-1)

• Load Case#4-Inclined loading

- Df=0 & L/A=0.10: **12,500 psf** (65.8% of LC-1)
- Df=0.5B & L/A=0.10: **21,600 psf** (74.5% of LC-1)
- Df=0 & L/A=0.25: **7,500 psf** (39.5% of LC-1)
- Df=0.5B & L/A=0.25: **12,800 psf** (44.1% of LC-1)

• Load Case#5-Eccentric-Inclined loading (-) to the direction of Inclination

- Df=0 & L/A=0.10: **17,000 psf** (90.3% of LC-1)
- Df=0.5B & L/A=0.10: **26,500 psf** (91.4% of LC-1)
- Df=0 & L/A=0.25: **14,000 psf** (73.7% of LC-1)
- Df=0.5B & L/A=0.25: **23,250 psf** (80.2 % of LC-1)

# CONCLUSIONS CONTINUED



## Rectangular Footing L/B=10: (Medium Dense)

- Load Case #1-Concentric loading
  - Df=0: **11,200 psf**
  - Df=0.5B: **14,750 psf**
- Load Case#2-Eccentric loading
  - Df=0: **10,700 psf** (95.5% of LC-1)
  - Df=0.5B: **12,120 psf** (82.2% of LC-1)



# CONCLUSIONS CONTINUED

## Rectangular Footing L/B=10: (Medium Dense)

- Load Case#3-Eccentric-Inclined loading (+) to the direction of Inclination
  - Df=0 & L/A=0.10: **6,300 psf** (54.3% of LC-1)
  - Df=0.5B & L/A=0.10: **9,180 psf** (62.3% of LC-1)
  - Df=0 & L/A=0.25: **2,630 psf** (23.5% of LC-1)
  - Df=0.5B & L/A=0.25: **7,180 psf** (48.7% of LC-1)
- Load Case#4-Inclined loading
  - Df=0 & L/A=0.10: **6,340 psf** (56.6% of LC-1)
  - Df=0.5B & L/A=0.10: **11,000 psf** (74.6% of LC-1)
  - Df=0 & L/A=0.25: **2,820 psf** (25.2% of LC-1)
  - Df=0.5B & L/A=0.25: **9,145 psf** (62.0% of LC-1)
- Load Case#5-Eccentric-Inclined loading (-) to the direction of Inclination
  - Df=0 & L/A=0.10: **11,000 psf (98.2% of LC-1)**
  - Df=0.5B & L/A=0.10: **14,200 psf** (96.3% of LC-1)
  - Df=0 & L/A=0.25: **9,493 psf** (84.8% of LC-1)
  - Df=0.5B & L/A=0.25: **12,920 psf** (87.7 % of LC-1)



**Thank You**