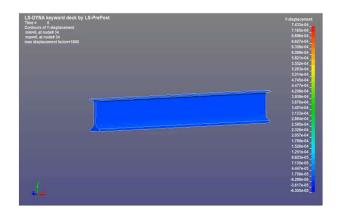


What is it?

The camber of a beam is the upwards deflections of the beam resulting from the eccentric prestressing force (either pretension or post-tension).

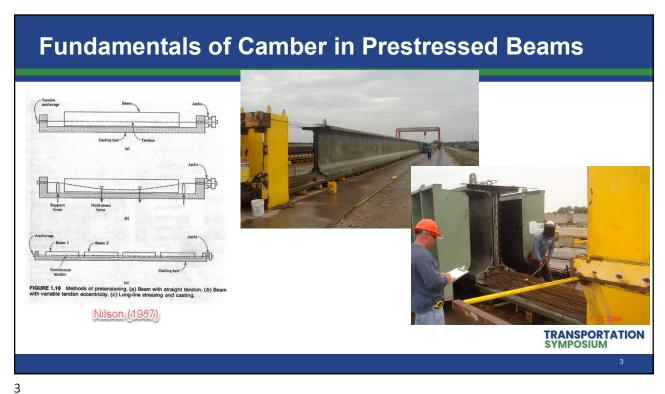
Why is it important?

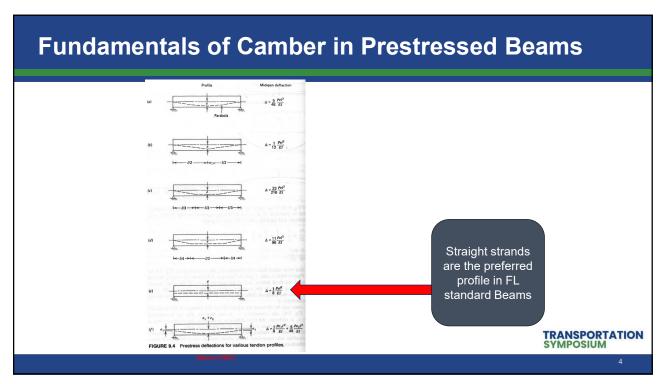
Accurate camber estimates ensure the deck and build-up are placed as designed and ensure the bridge profile is met.



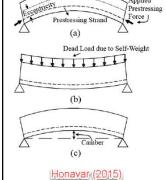
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2





Camber could be calculated as follows:



$$\Delta_{Camber} = \frac{P \cdot e \cdot L^2}{8 \cdot E \cdot I}$$

 $\delta_{SW} = \frac{5 \cdot w \cdot L^4}{384 \cdot E}$

P = Prestressing force (after loss)

e = Eccentricity of prestress force

L = Span length

E = Modulus of elasticity

I = Moment of inertia

w = Uniform load due to self-weight

L = Span length

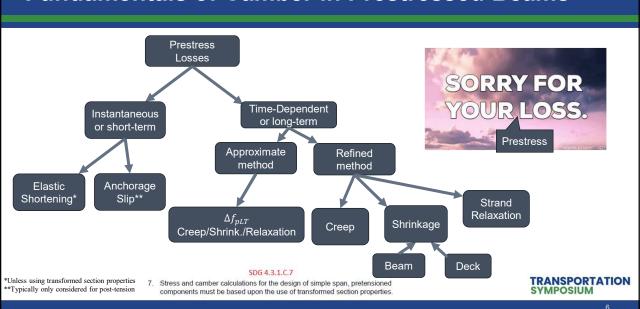
E = Modulus of elasticity

I = Moment of inertia

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 $\Delta_{net} = \Delta_{Camber} - \delta_{SW}$

Fundamentals of Camber in Prestressed Beams



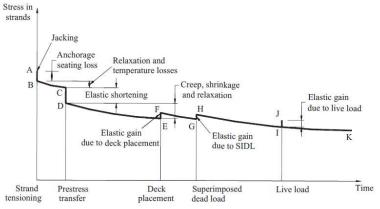


Figure 1. Stress versus time in the strands in a pretensioned concrete girder.

(NCHRP Report 496)

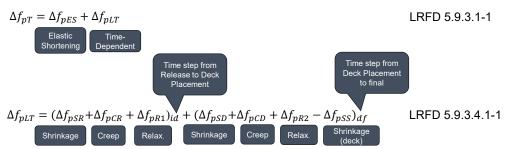
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Fundamentals of Camber in Prestressed Beams

LRFD 5.9.3.4 – Refined Prestress Losses (pretension members)



Shrinkage: Loss of prestress associated with the drying shrinkage of concrete, the reduction of strain in the prestressing steel is equal to the shrinkage strain of concrete.

Creep: Loss of prestress resulting from the gradual, time-dependent deformation of concrete under sustained stress.

Strand Relaxation: Loss of prestress in strands under sustained load while held at constant length.

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LRFD 5.9.3.3 – Approximate Method of time dependent losses

SDG 4.3.1.C.6

6. When calculating the Service Limit State capacity for pretensioned concrete flat slabs and girders, use the transformed section properties as follows: at strand transfer; for calculation of prestress losses; for live load application. For precast, pretensioned, normal weight concrete members designed as simply supported beams, use LRFD 5.9.3.3, Approximate Estimate of Time-Dependent Losses. For all other members use LRFD 5.9.3.4 with a 180-day differential between girder concrete casting and placement of the deck concrete.

Commentary: The FDOT cannot practically control, nor require the Contractor to control, the construction sequence and materials for simple span precast, prestressed beams. To benefit from the use of refined time-dependent analysis, literally every prestressed beam design would have to be re-analyzed using the proper construction times, temperature, humidity, material properties, etc. of both the beam and the yet-to-be-oast composite slab.

$$\Delta f_{pLT} = \frac{10 \cdot f_{pi} \cdot A_{ps}}{A_q} \gamma_h \cdot \gamma_{st} + 12 \cdot \gamma_h \cdot \gamma_{st} + \Delta f_{pR}$$

$$\gamma_h = 1.7 - 0.01 \cdot H$$

$$\gamma_{st} = \frac{5}{(1+f_{ci})}$$

 f_{pi} = prestressing steel stress immediately prior to transfer (ksi)

 γ_h = correction factor for relative humidity of the ambient air

 γ_{st} = correction factor for specified concrete strength at time of prestress transfer to the concrete member

 $\Delta f_{pR} =$ an estimate of relaxation loss taken as 2.4 ksi for low relaxation strand and in accordance with manufacturers recommendation for other types of strand (ksi)

H = average annual ambient relative humidity (percent)

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Fundamentals of Camber in Prestressed Beams

	Spacing (ft)	Span (ft)	D/C for Moment	D/C for Ser III w/ Simplified		
Beam				PS+DL+0.8LL	PS+DL+1.0	
FSB12x53	9.70	40	0.81	0.95	1.03	
FSB15x53	-	50	0.85	0.97	1.05	
FSB18x53	727	60	0.89	0.97	1.06	
Type II	7	60	0.85	0.89	0.99	
FIB36	8	97	0.84	0.96	1.06	
FIB45	8	117	0.83	0.95	1.04	
FIB54	8	132	0.87	0.98	1.07	
FIB63	8	145	0.86	0.97	1.05	
FIB72	8	163	0.85	0.97	1.04	
FIB78	8	172	0.85	0.97	1.03	
FIB84	8	181	0.83	0.95	1.02	
FIB96	8	198	0.84	0.97	1.03	
FIB96	12	178	0.81	0.95	1.02	

Beam	Difference
FSB12x53	-1%
FSB15x53	-5%
FSB18x53	-4%
Type II	-8%
FIB36	6%
FIB45	10%
FIB54	11%
FIB63	11%
FIB72	14%
FIB78	15%
FIB84	15%
FIB96	17%
FIB96	9%

			A			
ating	Time-Dep	endent Lo	ses (ksi)	V	Simplified	Difference
pCD	Δf.pR2	Δf.pSS	Δf.pSS WAI 227	Total	Total	Difference
24	1.56	0.08	0.02	21.48	21.16	-1%
23	1.55	-0.05	-0.01	22.17	20.99	-5%
16	1.53	-0.02	-0.01	22.47	21.63	-4%
54	1.43	-0.96	-0.28	23.66	21.86	-8%
04	1.34	-0.98	-0.28	24.13	25.68	6%
.00	1.31	-0.89	-0.26	24.57	26.99	10%
75	1.36	-0.91	-0.26	23.33	25.88	11%
69	1.38	-0.91	-0.26	22.92	25.51	11%
63	1.36	-0.88	-0.26	23.09	26.30	14%
59	1.37	-0.89	-0.26	22.91	26.25	15%
60	1.36	-0.88	-0.26	22.99	26.45	15%
48	1.38	-0.90	-0.26	22.37	26.09	17%
74	1.30	-0.99	-0.29	24.42	26.58	9%

Suggested Multipliers to be Used as a Guide in
Estimating Long-Term Cambers and Deflections for Typical Members

		Without Composite Topping	With Composite Topping
	At erection:		
(1)	Deflection () component—apply to the elastic deflection due to the member weight at transfer of prestress	1.85	1.85
(2)	Camber (†) component—apply to the elastic camber due to prestress at the time of transfer of prestress	1.80	1.80
	Final:		
(3)	Deflection (1) component—apply to the elastic deflection due to the member weight at transfer of prestress	2.70	2.40
(4)	Camber (†) component—apply to the elastic camber due to prestress at the time of transfer of prestress	2.45	2.20
(5)	Deflection () component—apply to elastic deflection due to superimposed dead load only	3.00	3.00
(6)	Deflection () component—apply to elastic deflection caused by the composite topping	=	2.30

PCI (2023)

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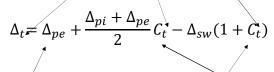
Fundamentals of Camber in Prestressed Beams



FDOT LRFD Prestressed Beam Program v6.2

© 2022 Florida Department of Transportation

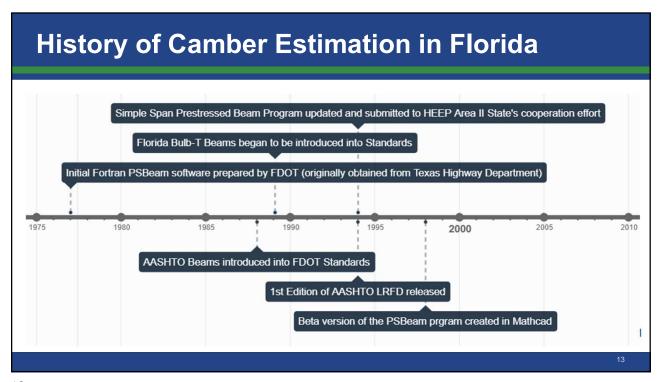
Subscript "t" is a time step e.g. from 0 days to 30 days

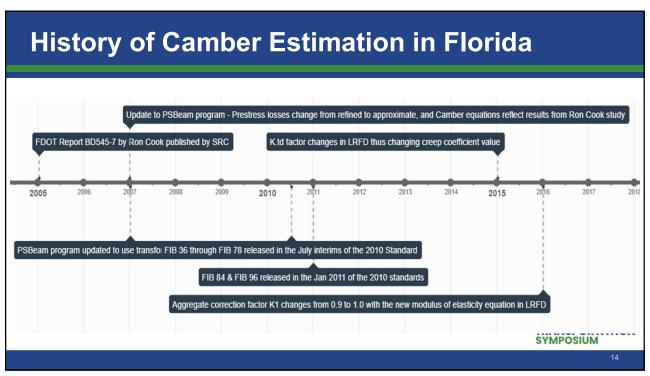


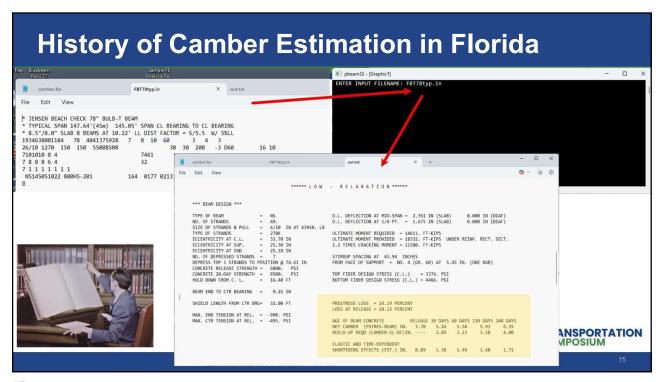
Losses based on Creep Coefficient applied to Approx. method both camber and self-weight deflections

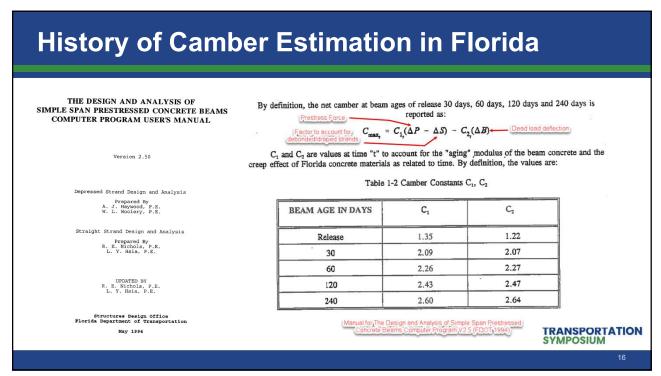
Field Verification of Camber **Estimates for Prestressed Concrete** Bridge Girders (Cook 2005)

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History of Camber Estimation in Florida

For Wires and Strands with f_{pu} = 1620, 1725 or 1680 MPa Rectangular Beams and Solid Slabs Upper Bound 130 + 41 PPR Upper Bound Average Box Girder I-Girder 130 + 41 PPR Average $230\left[1 - 0.15 \frac{f_c' - 41}{41}\right] + 41 PPR$ Single T, Double T, Hollow Core and Voided Slab Upper Bound 270 1.0 -0.15 1/e-41 +41 PPR 210 1.0-0.15 1/c-41 -41 PPR 230 1.0 -0.15 1/6-41 + 41 PPR

Approximate

1st Ed. AASHTO LRFD (1994)

- for pretensioned members:
- $\Delta f_{pSR} = (117 1.03 \text{ H}) \text{ (MPa)}$

Prestress loss due to creep may be taken as:

 $\Delta f_{pCR} = 12.0 f_{cap} - 7.0 \Delta f_{cdp} \ge 0$ (5.9.5.4.3-1)

change in concrete stress at center of gravity of prestressing steel due to permanent loads, except the load acting at the time the prestressing force is applied. Values of Af_{cop} should be calculated at the same section or sections for which f_{cop} is calculated (MPa).

5.9.5.4.4a General

The total relaxation at any time after transfer shall be taken as the sum of the losses specified in Articles 5.9.5.4.4b and 5.9.5.4.4c.

5.9.5.4.4b At Transfer

In pretensioned members, the relaxation loss in prestressing steel, initially stressed in excess of 0.50 $\rm f_{p,\nu}$ may be taken as:

 $\Delta f_{pRI} = \frac{\log(24.0t)}{10.0} \left[\frac{f_{pI}}{f_{py}} - 0.55 \right] f_{pI}$ (5.9.5.4.4b-1)

for low-relaxation strand:

 $\Delta f_{pRt} = \frac{\log(24.0t)}{40.0} \left[\frac{f_{pl}}{f_{ml}} - 0.55 \right] f_{pl}$ (5.9.5.4.4b-2)

- t = time estimated in days from stressing to transfer (DAYS)

Refined

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Fundamentals of Camber in Prestressed Beams

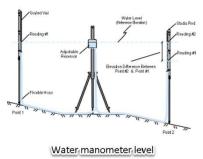
How and when is it measured?





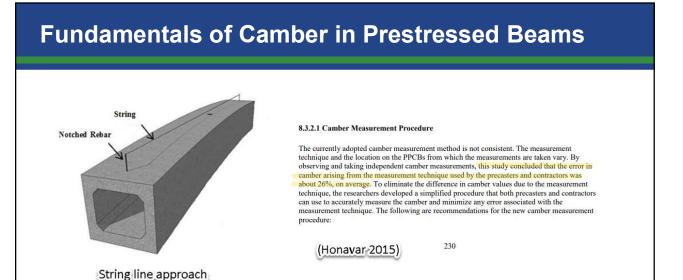






(Cook-2005)

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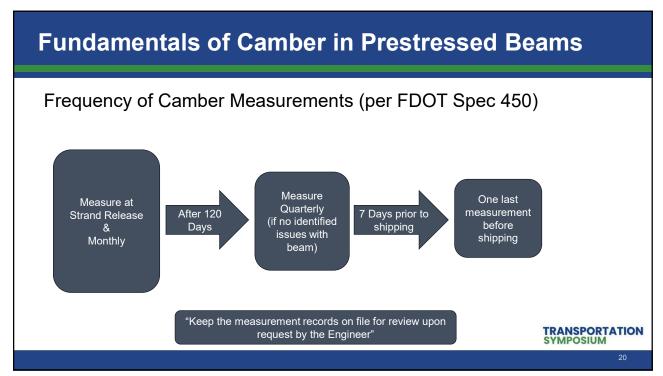


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(Rizkalla 2011)





4.3.2 Beam Camber/Build-Up over Beams

A. Unless otherwise required as a design parameter, beam camber for computing the build-up shown on the plans must be based on 120-day old beam concrete.

Modification for Non-Conventional Projects:

Delete SDG 4.3.2.A.

- B. On the build-up detail, show the age of beam concrete used for camber calculations as well as the value of camber due to prestressing minus the dead load deflection of the beam.
- C. Consider the effects of horizontal curvature with bridge deck cross slope when determining the minimum buildup over the tip of the inside flange.
- Commentary: In the past, the FDOT has experienced significant deck construction problems associated with excessive prestressed, pretensioned beam camber. The use of straight strand beam designs, higher strength materials permitting longer spans, stage construction, long storage periods, improperly placed dunnage, and construction delays are some of the factors that have contributed to camber growth. Actual camber at the time of casting the deck equal to 2 to 3 times the initial camber at release is not uncommon.
- D. Design pretensioned beams so that the theoretical design camber at the end of construction is positive (upward) after all non-composite and composite dead loads are applied.

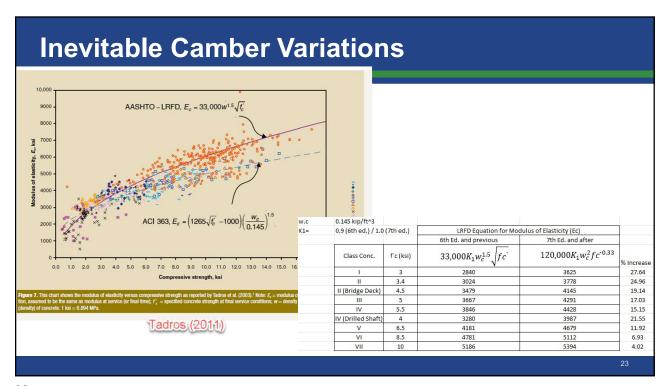


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Inevitable Camber Variations Indirect Porosity Influence through Aggregate indicators of Ec Friction the Modulus of Type Elasticity (Ec) of Bean Unit weight Moisture Size/Shape (wc) Stiffness W/C Ratio affecting Camber "In early-age concrete, the strength of the cement Time at Transfer paste is the primary contributor to the strength while Temperature the stiffness of the coarse aggregates is the primary contributor to the modulus of elasticity." NCHRP RPT 496 (2003) TRANSPORTATION SYMPOSIUM



Inevitable Camber Variations

FDOT Standard Specifications

346-9.7 Structural Adequacy: The Engineer will evaluate the structural adequacy for verified concrete that does not meet the minimum specified compressive strength of Table 346-3. For structural adequacy, with standard molded and cured compressive strength

For structural adequacy, with standard molded and cured compressive strength cylinders, the compressive strength of concrete is satisfactory provided that the two following criteria are met:

1. The average compressive strength does not fall below the specified minimum compressive strength by more than:

a. $500 \ \mathrm{psi}$ if the specified minimum compressive strength is equal to or less than $5{,}000 \ \mathrm{psi}$.

b. 10% of the specified minimum compressive strength if the specified minimum compressive strength is greater than 5,000 psi.

The average compressive strength with the previous two LOTs is equal to or exceeds the specified minimum compressive strength. This condition only applies if there are two or more previous LOTs to calculate the average.

The Engineer will consider the concrete for a given LOT as structurally adequate and coring will not be allowed when a concrete compressive strength test result falls below the specified minimum strength but has met the above conditions.

Class VI (f'c = 8,500)

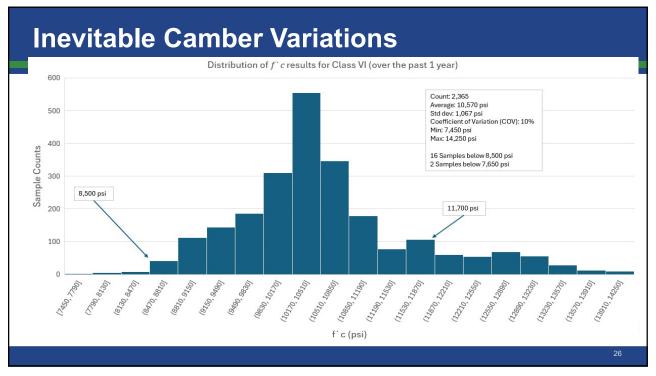
 $8,500 - 0.10 \cdot 8,500 = 7,650 \ psi$

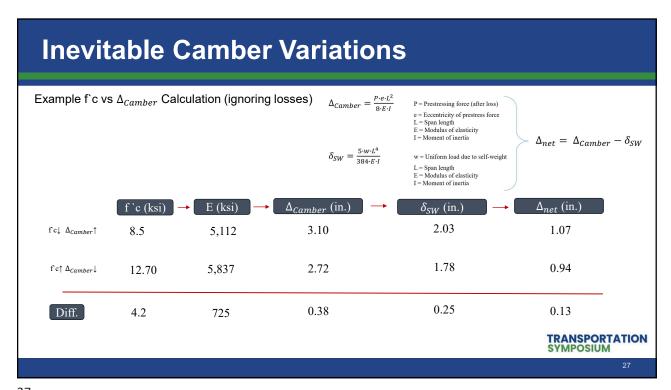
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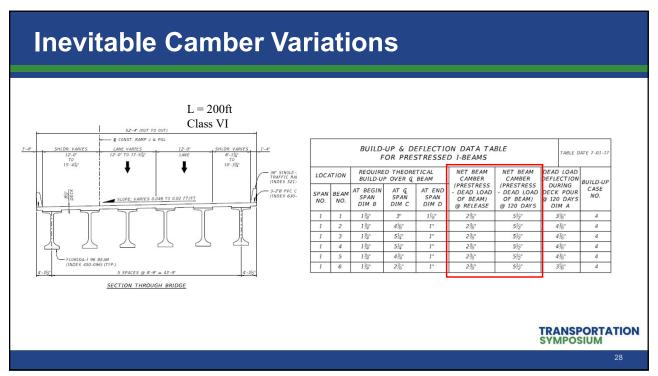
24

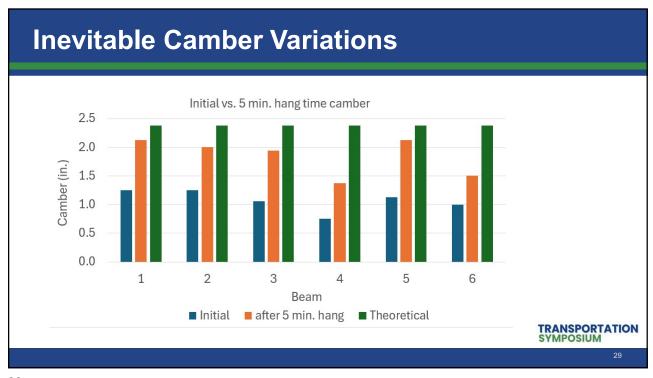
Inevitable Camber Variations FDOT Materials Manual 9.2.7 MIX DESIGNS FDOT Materials Manual 9.2.7.1 Concrete mix designs shall meet the requirements of **Specification Section 346**. Plants may follow ACI 301 Section 4, and ACI 211 as guidelines to design concrete mixes. TABLE 1 – Overdesign requirements for establishing f'cr when data is not available at 28-day or 56-day whichever is applicable When the Engineer determines that unsatisfactory results are obtained during production, the mix design approval will be rescinded. Class of Overdesign fcr (psi) f'c (psi) Compressive Design a concrete mix to provide a required compressive strength (*f'cr*) that exceeds the specified minimum compressive strength (*f'c*) by the overdesion value. (psi) Strength (psi) I Seal 3,000 1,200 4,200 f'cr = f'c + OverdesignNot Not 5.200 I Pavement 3,000 Specified Specified Proceed as follows to select the overdesign value in concrete mixes: 3,400 5,700 4,600 (1) For a class of concrete, submit compressive strength field test data for the past 24 months and spanning no less than 45 calendar days, to determine the standard deviation. The 7c is required to be within 1,000 psi. The strength test data represents either a group of at least 30 consecutive tests or a statistical average for two groups totaling 30 or more tests. Determine the overdesign as follow: 1,200 II Bridge Deck 1,200 5,700 4,500 6,750 5,000 6,200 1,200 6,750 IV 5,500 1,250 6,750 7,850 IV Drilled Shaft 4,000 1,200 5,200 6.200 a. When fc is equal to or less than 5,000 psi. 7,850 6,500 1,350 10,050 Overdesian = 2.33 x Standard Deviation - 500 psi 1,550 10,050 11,700 8,500 b. When Fc is greater than 5,000 psi. 11,700 $Overdesign = 2.33\ x\ Standard\ Deviation - 0.10xf'c$ (2) Use Table 1 at the concrete producer's option, or when the concrete producer has no records of field strength tests performed within the past 24 months and spanning no less than 45 calendar days for a class of concrete within 1,000 psi of that *fc. TRANSPORTATION SYMPOSIUM

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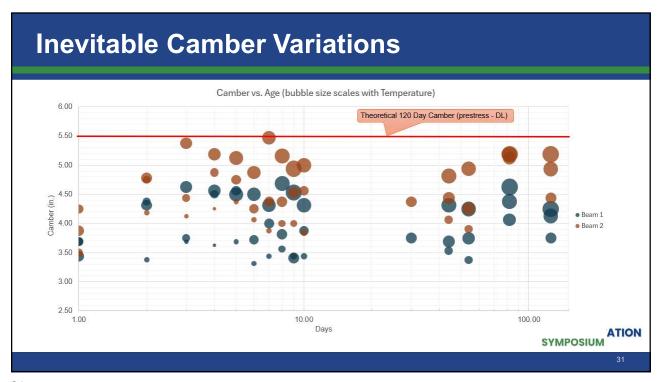


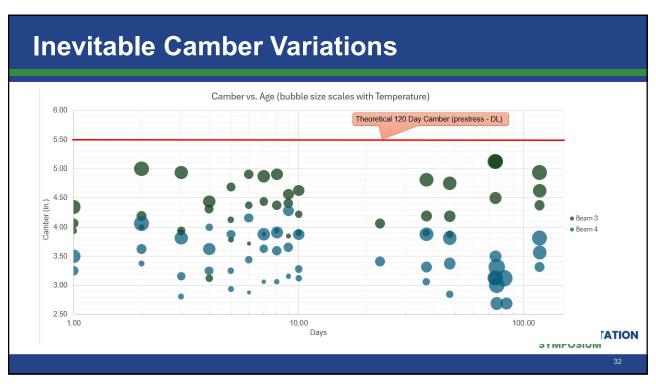


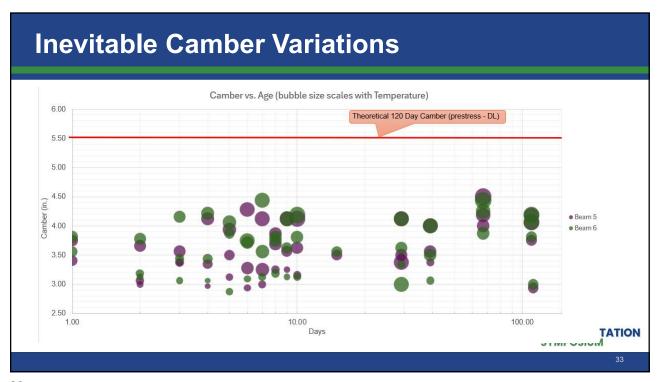


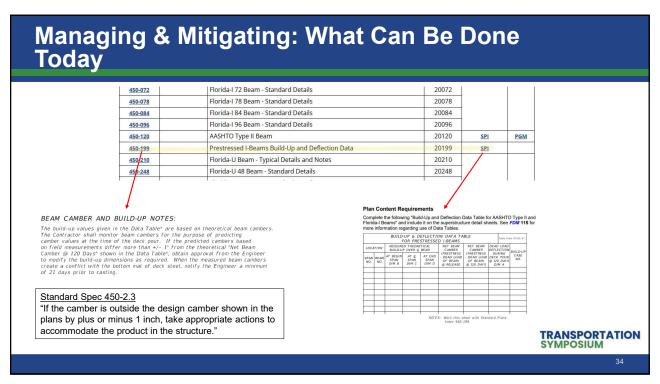


Inevitable Camber Variations Max dif. in Camber Beam Tem Beam Tem Temp at time of Check 67°F 67°F 61°F Temp at time of CAMBER at time of Check DATE at time of Check DATE CAMBER DATE CAMBER at time of Check DATE measurements (in.) 89°F 89°F 84°F 4.313 5.469 4.875 95.6°F 90.6°F 80.9°F 75.2°F 4-17-243:30PM 4-17-243:30PM 4-24-243:30PM 4-24-243:30PM 3.563 4.000 3.938 77.6°F 77.9°F 73.5°F 4-18-245:30AM 4-18-245:30AM 4-25-245:30AM 76.2°F 75.6°F 73.2°F 4.688 5.156 4.906 95.7°F 90.6°F 83.9°F 4-18-243:30PM 4-18-243:30PM 4-25-243:00PM 1.125 1.156 4.375 4.375 4-25-243:00PM 0.968 4-25-243:00PM 0.843 5-4-245:30AM 0.625 5-4-245:30AM 0.625 4-25-2411:00AM 3.875 TRANSPORTATION SYMPOSIUM









Managing & Mitigating: What Can Be Done Today

- Camber too Low
 - Per spec 450, if camber is less than 50% of predicted camber at release. Adjust dunnage inwards to induce camber. (Ask the precaster when did they measure the release camber, did they pick it up and set it back down? did they move it to storage before measuring?)
 - (For Negative Camber Beams) Does the beam still meet stress limits? Will it still load rate? does it meet vertical clearance?
 - Have the beam seats been cast already? Can they be raised?
 - Can we adjust the roadway profile?

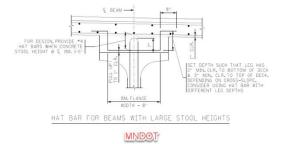
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Managing & Mitigating: What Can Be Done Today

- Camber too High
 - Have the beam seats been cast already? Can they be lowered?
 - Is the beam interfering with the bottom mat of deck reinforcing?
 - Build-up at the end spans maybe too large for beam shear stirrups to embed in deck, consider 'hat' bars to bridge the gap.



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Managing & Mitigating: What Can Be Done Today

- The time of day which the precaster could take camber measurements to eliminate effect of temperature/solar radiation.
- Ask for the Cylinder breaks for your beams, Remember f`c↑ Δ_{Camber}↓
- Ask the precaster for camber data on previous beams they've cast.

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Managing & Mitigating: What Can Be Done Today

Reach out to your district structural materials engineer.

Staff Directory

District Materials Office Contacts

D1-7 Materials | D2 Materials | D3 Materials | D4-6 Materials | D5 Materials | Turnpike Materials

District Materials Engineers (DMREs)

Additional Information

Florida Center for Pavement Excellence Contacts

MAC Primary Contacts (DACs, Development, etc.)

Research Management Team



https://www.fdot.gov/materials/administration/resources/contacts/staffdirectory.shtm (https://tinyurl.com/muweb9em)

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Managing & Mitigating: What Can Be Done Today

FDOT Standard Specs 450-14.2

Support prestressed products that are stacked by dunnage placed across the full width of each bearing point and aligned vertically over lower supports. Move dunnage points in accordance with 450-2.3 with the approval of the QC Manager. Do not use stored products as a storage area for either shorter or longer products or heavy equipment.

Where feasible, base the selection of storage sites, storage conditions and

Where feasible, base the selection of storage sites, storage conditions and orientation upon consideration of minimizing the thermal and time-dependent creep and shrinkage effects on the camber and/or sweep of the precast pretensioned products.

Continuous application of water during the initial 72 hour moist curing period may be interrupted for a maximum of one hour to allow relocation of precast prestressed concrete elements within the manufacturing facility. Keep the moist burlap in place during relocation of the element.

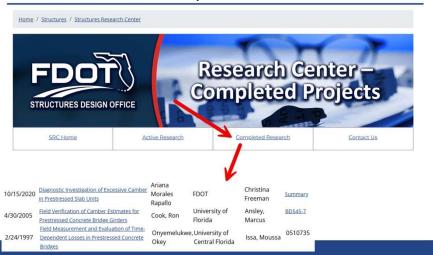
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Managing & Mitigating: What Can Be Done, Moving Forward

What research can accomplish



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Managing & Mitigating: What Can Be Done, Moving Forward

From Tadros (2011)

"In design, allow for variability of camber by 50%."

"Allowance in design should include flexibility in adjusting the horizontal shear reinforcement and the girder-seat elevations"

From Cook (2005)

"For the influence of the thermal gradient on camber, there was little difference between the empirically corrected camber measurements and the analytically corrected camber measurements in the majority of cases. Either method is suitable for the correction of camber due to thermal gradient effects."

"Guidelines for storage of the girders with instruction of the amount of clearance necessary between the ground and bottom flange should be implemented in order to reduce the effect of differential shrinkage in the field."

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Managing & Mitigating: What Can Be Done, Moving Forward

From Rizkalla (2011)

"Whenever practical, camber should be measured before dawn before the sun induces thermal gradients within the girders."

"Girders should be stored with the supports as close to possible to their design bearing locations to minimize camber variability."

From Almohammedi (2019)

"The contractor should update camber, deflection and the road longitudinal profile based on the measured concrete strength to decrease the discrepancy between the design and the actual cambers..."

"...More effectively, the fabricators can provide the contractor with the average camber values for the girders in the storage yard and update the road profile accordingly."

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Managing & Mitigating: What Can Be Done, Moving Forward

From Almohammedi (2019)

"Girders should be cast based on a scheduled erection plan to minimize storage time and to reduce the effect of creep and shrinkage on camber prediction."

"The initial camber and the elastic shortening losses should be measured after moving the girder to the storage yard to eliminate the effect of the friction from the prestressing bed on camber."

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Managing & Mitigating: What Can Be Done, **Moving Forward** CAST DATE WEST # JOB# SDO In-house Cambe DESIGN MIX/REL./28 DAYS LENGTH POUR DATE SAMPLE # REL. DATE REL. PSI 28 DAYS PSI SHIP PSI/DAYS SHIP DATE SPECIAL NOTES 03-2084/8000/10000 1-5 SWEEP CAMBER SWEEP 03-2084/8000/10000 5.190 0.7688888 2.211578947 0.250 2.137368421 0.87686 03-2084/8000/10000 2.053157895 2.094210526 0.84232118 1-3 0.85916329 0.125 2.110 112 2.196842105 86 1.004651163 0.250 0.500 0.90126855 30 LID 86 0.823255814 1.31720930 96" FIB 1.29894291 1.28195569 0.250 09/29/18 6.81038961 96" FIB 4.370 0.750 6.981818182 KB KB 4.220 4.480 0.500 KB KB 2.370 KB 2.290 0.500 2.170 0.500 2.040 0.500 SYMPOSIUM



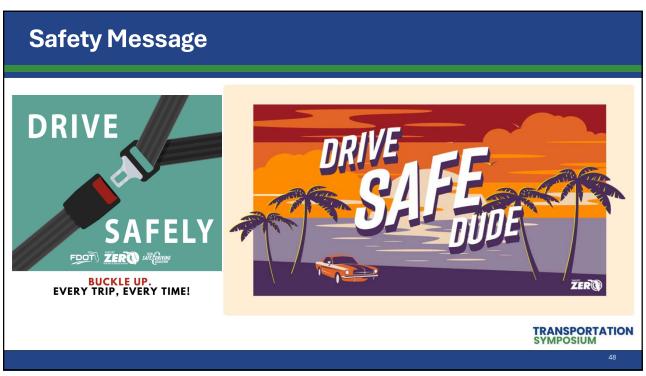
References

- Design of Prestressed Concrete (Nilson 1987)
- Field Verification of Camber Estimates for Prestressed Concrete Bridge Girders (Cook 2005)
- Improving the Accuracy of Camber Predictions for Precast Pretensions Concrete Beams (Honarvar 2015)
- Prestress Losses in Pretensioned High-Strength Concrete Bridge Girders, NCHRP rpt 496 (Tadros, Al-Omaishi 2003)
- · Predicting Camber, Deflection, and Prestress Losses in Prestressed Concrete Members (Rizkalla 2011)
- Precast, prestressed girder camber variability (Tadros 2011)
- Estimating Camber, Deflection, and Prestress Losses in Precast, Prestressed Bridge Girders (Almohammedi 2019)
- PCI Bridge Design Manual (4th Edition 2023)
- The Design and Analysis of Simple Span Prestressed Concrete Beams Computer Program User's Manual (1994)
- AASHTO LRFD Bridge Design Specifications (1st Edition 1994)

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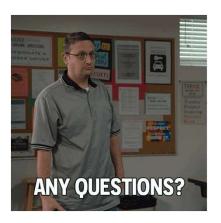
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