

STATE OF FLORIDA



ANALYSIS OF BACK CALCULATION METHOD FOR DETERMINATION OF BULK SPECIFIC GRAVITY AT N_{DESIGN} AND N_{INITIAL} LEVELS OF GYRATION

**Research Report
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INTRODUCTION

The current Superpave mix design procedure requires that specimens be compacted to the maximum number of gyrations, N_{\max} , for the specified traffic level. Volumetric data for the design number of gyrations, N_{des} , and the initial number of gyrations, N_{ini} , are then back calculated based on the bulk specific gravity, G_{mb} , of the N_{\max} specimens and the height data generated during the compaction process of those same specimens.

When computing volumes using the height data and cross sectional area of the mold, the calculated volume is always higher than the actual volume of the sample because the sample contains surface voids. The volume of the surface voids are mostly excluded in the determination of the volume of the specimen by the saturated surface dry method (such as AASHTO T 166 specification). This happens because the water in the pores either runs out of the pores upon removal of the specimen from the water bath or the water is removed from the pores as the specimen is rolled on the towel prior to determining the saturated surface dry weight.. Therefore, a correction factor is determined for the N_{\max} specimens. The correction factor is computed as:

$$C.F. = \frac{G_{mb,measured}}{G_{mb,estimated}}$$

where: C.F. = correction factor

$G_{\text{mb,measured}}$ = measured bulk specific gravity at N_{\max}
 $G_{\text{mb,estimated}}$ = estimated bulk specific gravity at N_{\max}

The correction factor is then applied to the estimated G_{mb} values for the specimens compacted to

N_{des} and N_{ini} compaction levels using the following formula:

$$G_{mb,corrected} = C.F. \times G_{mb,estimated}$$

where: $G_{mb,corrected}$ = corrected bulk specific gravity at N_{des} or N_{ini}

The issue in question is whether the correction factor calculated at N_{max} is applicable or accurate for the N_{des} and N_{ini} levels of gyration. One might reason that the correction factor might increase as the number of gyrations decreased due to the increasing size and number of voids present on the surfaces of a specimen. If the correction factor were not constant throughout the gyration process, then the back calculated values for G_{mb} and other volumetric properties such as air voids would be incorrect. One possible solution would be to actually gyrate samples to the N_{des} and N_{ini} levels during the mix design process, eliminating the need for a correction factor.

PURPOSE AND SCOPE OF EXPERIMENT

The purpose of this research study was to determine the error, if any, that occurs by back calculating volumetric properties based on a correction factor determined at N_{max} .

Six different coarse graded Superpave mix designs were tested. The mixes consisted of three Florida limestone mixes and three Georgia granite mixes. None of the mixes contained reclaimed asphalt pavement. Within each aggregate type, there was a 9.5, 12.5 and 19.0 mm mix type. See **Table 1** for a summary of the six mixes used.

For each mix type, four samples were gyrated to the N_{max} , N_{des} , and N_{ini} compaction

levels. This amounted to 12 samples per mix type for a total of 72 samples for the study. All mixes were designed for traffic level five (10 - 30 million ESAL's) and were compacted to the following number of gyrations: N_{max} - 152; N_{des} - 96; N_{ini} - 8.

The G_{mb} 's of all specimens were determined in accordance with Florida Method FM 1-T 166 Method B (non-destructive). This Florida Method is the same as AASHTO Method T 166 Method A for determination of bulk specific gravity. In addition the G_{mb} 's of the N_{ini} specimens were also determined using a granular medium method for comparison. The granular medium used was glass beads conforming to AASHTO M 247-81 Type I. Basically, the glass beads replace the water in the above referenced methods. The procedure for determining the G_{mb} using glass beads was obtained from an article in March 1998 Asphalt Contractor Periodical (1).

RESULTS

The raw data for G_{mb} , G_{mm} , % air voids, outlier determination, etc. is included in the **Appendix**. The variability in the G_{mb} values, as determined by FM 1-T 166, within a few of the mixes was high (see **Table 2**). The variability in this study is being defined as the range between the highest and lowest G_{mb} values for a set of four specimens. AASHTO T 166 states a maximum allowable range of 0.02 between two specimens (2). Since this study is using four specimens, the allowable range would be higher. ASTM D 2726-93a states a maximum allowable range of 0.045 for four specimens for single-operator precision (3). The multi-laboratory precision for four specimens is 0.097. As will be discussed later, the specimens made in this study were all prepared with the same equipment but with different operators. Therefore, a precision value somewhere in between single-operator and multi-laboratory would be appropriate. A precision statement for

the glass bead method of G_{mb} determination was not available.

The source(s) of the variability is difficult to determine, but is most likely due to operator error with some variability due to natural variation in materials and variability in the gyratory compaction process. The following conditions occurred during the study:

1. The aggregate gradations were fabricated by several lab technicians.
2. The same technician performed all mixing duties.
3. All mixes were aged for two hours prior to compaction, therefore compaction temperatures were most likely consistent.
4. Three technicians performed gyration duties.
5. Bulk specific gravity measurements were performed by several technicians.

The G_{mb} data was then analyzed for outliers using the FDOT method for outlier determination

(4). Excluding the outliers, the variability within each mix improved, as expected (see **Table 3**).

With respect to air voids, the data was analyzed with and without the outliers. Both methods of analysis resulted in the same trends with slightly different magnitudes. For the four N_{des} specimens of each mix type, the average air voids were determined and subtracted from the average air voids back calculated from the N_{max} specimens. Therefore, a positive difference would indicate that the back calculation method was overestimating air voids at N_{des} , whereas a negative difference would indicate that the back calculation method was underestimating air voids at N_{des} . The same procedure was used at N_{ini} except that two methods for determining the G_{mb} of the N_{ini} specimens were used, FM 1-T 166 Method B (water bath method) and glass

beads. The results including the outliers are displayed in **Table 4** and **Figures 1 and 2** and the results excluding the outliers are displayed in **Table 5** and **Figure 3 and 4**.

For the N_{des} specimens, the results show three mixes with positive differences and three mixes with negative differences, whether including the outliers or not. The magnitude of the differences is larger with the limestone mixes compared to the granite mixes.

For the N_{ini} specimens, the results show all of the mixes having a positive difference, indicating that the back calculation method is overestimating air voids at the N_{ini} level. The magnitude of the difference also increases as the nominal maximum aggregate size increases. This is logical due to the larger void spaces present on the surfaces of specimens containing larger size aggregates. The differences calculated do not vary greatly between the water bath method and glass bead method for the 9.5 and 12.5 mm mixes. However, for the 19 mm mixes, the differences are more pronounced. The differences are higher for the water bath method. This is because, at high air void levels, water will flow out of the specimen as it is lifted out of the water bath, affecting the accuracy of the results. This results in a lower saturated surface dry weight and therefore a calculated higher bulk density and lower air void content. Therefore, for the N_{ini} specimens, it is more appropriate to use the values calculated by the glass bead method for the 19.0 mm mixes.

CONCLUSIONS / RECOMMENDATIONS

The N_{des} data can be interpreted in at least two ways. First, it can be argued that because there were three mixes with positive differences and three mixes with negative differences, that no

firm conclusions can be drawn from the data and therefore, the current method of back calculation should continue to be used. One could also interpret the data by recognizing that because there is variability between mix types, that this is justification that one should gyrate to N_{des} instead of N_{max} . After a design aggregate blend and binder content is determined, then specimens could be compacted to N_{max} to verify the criteria that the percent of the maximum density is $\leq 98\%$. This would be an after the design check just as moisture sensitivity is currently done. However, the ramifications of failing the N_{max} criteria would likely result in a time consuming redesign of the mix.

The N_{ini} data is more conclusive. The back calculation method overestimates the air voids at this level. This effect is most pronounced for 19.0 mm mixes. This could result in a mix passing the N_{ini} requirements when in reality it should not. One solution is to compact specimens to N_{ini} as a check similar to the N_{max} specimens mentioned above. Another solution is to require N_{ini} specimens to be made for only those mix designs where the back calculated $\%G_{mm}$ at N_{ini} is $\geq 86\%$. This would provide a 3% G_{mm} margin of error. If the back calculated $\%G_{mm}$ was less than 86%, then even with a 3% error in the back calculation method, the $\%G_{mm}$ would be $\leq 89\%$.

The findings in this report agree with the findings from Report 98-5 from the National Center for Asphalt Technology (NCAT) (5). That study also recommended that specimens be compacted to N_{des} at mix design. The study examined dense graded and stone matrix asphalt (SMA) mixes. The data showed both positive and negative air void differences at higher gyration levels and larger positive values at lower gyration values (both results similar to the findings in this report).

It should be noted that the current Superpave specifications for $\%G_{mm}$, VMA, VFA, etc. may have been based on the current back calculation method. These specification values may need to be reexamined and possibly adjusted if a if specimens at design are to be gyrated to N_{des} and possibly N_{ini} levels .

REFERENCES

1. Crockford, Bill. *More Tailgate Tips - Estimating Bulk Specific Gravity without Water*. The Asphalt Contractor, Independence, MO, June, 1998.
2. *Bulk Specific Gravity of Compacted Bituminous Mixtures Using Saturated Surface-Dry Specimens, AASHTO Standard Method of Test T 166-93*. 1993.
3. *Standard Test Method for Bulk Specific Gravity and Density of Compacted Bituminous Mixtures Using Saturated Surface-Dry Specimens, ASTM D 2726-93a*. 1993.
4. *Asphalt Paving Technician Manual, English Version*. Pages 9-9 thru 9-12. Florida Department of Transportation, Gainesville, FL, 1996.
5. Mallick, Rajib B., S. Buchanan, E. R. Brown, M. Huner. *An Evaluation of Superpave Gyrotory Compaction of Hot Mix Asphalt*. Report 98-5, National Center for Asphalt Technology, Auburn, AL, January, 1998.

Table 1 - Composite Gradation Summary of Mixes Used in Study

Mix #	SP98-0176A	SP98-0177A	SP98-0178A	SP98-0108A	SP97-0071A	SP96-0017B
Nom. Max. Agg. Size, mm	9.5	12.5	19.0	9.5	12.5	19.0
Agg. Type	Fl. Limestone	Fl. Limestone	Fl. Limestone	Ga. Granite	Ga. Granite	Ga. Granite
Gradation % Passing						
19.0 mm	100	100	99	100	100	99
12.5 mm	100	96	91*	100	100	63
9.5 mm	99	90	84	100	78	45
4.75 mm	72	61	53	75	43	35
2.36 mm	46	39	33	47	29	25
1.18 mm	28	22	18	32	18	20
600µm	15	11	9.5	23	12	14
300µm	8.1	6.0	5.5	16	8.6	11
150µm	4.9	4.1	4.2	11	5.9	7.2
75µm	3.9	3.6	3.7	6.4	3.7	4.5

* By definition, this composition gradation does not meet the Superpave requirements for a 19.0 mm mix because the % passing the 12.5 mm sieve is 91 %. This is 1% greater than that of the FDOT approved mix design.

Table 2 - Maximum Range in G_{mb} Values of Four Specimens for Each Mix Type and Gyration Level (Including Outliers)

Mix ID	Nmax	Ndes	Nini (SSD)	Nini (Beads)
176A-9.5 LS	0.053	0.026	0.038	0.056
177A-12.5 LS	0.013	0.089	0.018	0.045
	3 samples			
178A-19.0 LS	0.045	0.040	0.027	0.063
108A-9.5 GR	0.029	0.005	0.046	0.039
71A-12.5 GR	0.051	0.074	0.025	0.018
17B-19.0 GR	0.016	0.030	0.007	0.049

Table 3 - Maximum Range in G_{mb} Values of Three or Four Specimens for Each Mix Type and Gyration Level (Excluding Outliers)

Mix ID	Nmax	Ndes	Nini (SSD)	Nini (Beads)
176A-9.5 LS	0.009	0.026	0.038	0.056
	3 samples	4 samples	4 samples	4 samples
177A-12.5 LS	0.013	0.023	0.018	0.045
	4 samples	3 samples	4 samples	4 samples
178A-19.0 LS	0.022	0.015	0.027	0.030
	3 samples	3 samples	4 samples	3 samples
108A-9.5 GR	0.007	0.005	0.046	0.011
	3 samples	4 samples	4 samples	3 samples
71A-12.5 GR	0.012	0.042	0.006	0.018
	3 samples	3 samples	3 samples	4 samples
17B-19.0 GR	0.004	0.030	0.007	0.049
	3 samples	4 samples	4 samples	4 samples

Table 4 - Air Void Data Including Outliers

Summary, 176A - 9.5 Limerock	N _{des}	N _{ini}	
Average air voids, back calculated	5.23	16.28	16.28
Average air voids actual, SSD	5.43	15.73	NA
Average air voids actual, beads	NA	NA	15.16
Difference (Back calculated - actual)	-0.20	0.54	1.12

Summary, 177A - 12.5 Limerock	N _{des}	N _{ini}	
Average air voids, back calculated	4.37	15.65	15.65
Average air voids actual, SSD	5.65	14.36	NA
Average air voids actual, beads	NA	NA	14.51
Difference (Back calculated - actual)	-1.28	1.29	1.14

Summary, 178A - 19.0 Limerock	N _{des}	N _{ini}	
Average air voids, back calculated	6.89	17.75	17.75
Average air voids actual, SSD	6.45	15.06	NA
Average air voids actual, beads	NA	NA	15.74
Difference (Back calculated - actual)	0.43	2.69	2.01

Summary, 108A - 9.5 Granite	N _{des}	N _{ini}	
Average air voids, back calculated	4.11	13.26	13.26
Average air voids actual, SSD	3.54	11.66	NA
Average air voids actual, beads	NA	NA	11.21
Difference (Back calculated - actual)	0.56	1.60	2.04

Summary, 71A - 12.5 Granite	N _{des}	N _{ini}	
Average air voids, back calculated	5.58	15.37	15.37
Average air voids actual, SSD	5.76	12.81	NA
Average air voids actual, beads	NA	NA	13.17
Difference (Back calculated - actual)	-0.18	2.56	2.19

Summary, 17B - 19.0 Granite	N _{des}	N _{ini}	
Average air voids, back calculated	4.26	13.68	13.68
Average air voids actual, SSD	4.11	9.43	NA
Average air voids actual, beads	NA	NA	10.36
Difference (Back calculated - actual)	0.16	4.26	3.32

Table 5 - Air Void Data Excluding Outliers

Summary, 176A - 9.5 Limerock	N_{des}	N_{ini}	
Average air voids, back calculated	4.68	15.66	15.66
Average air voids actual, SSD	5.43	15.73	NA
Average air voids actual, beads	NA	NA	15.16
Difference (Back calculated - actual)	-0.75	-0.07	0.50

Summary, 177A - 12.5 Limerock	N_{des}	N_{ini}	
Average air voids, back calculated	4.37	15.65	15.65
Average air voids actual, SSD	6.46	14.36	NA
Average air voids actual, beads	NA	NA	14.51
Difference (Back calculated - actual)	-2.09	1.29	1.14

Summary, 178A - 19.0 Limerock	N_{des}	N_{ini}	
Average air voids, back calculated	7.22	18.14	18.14
Average air voids actual, SSD	6.09	15.06	NA
Average air voids actual, beads	NA	NA	16.24
Difference (Back calculated - actual)	1.13	3.09	1.90

Summary, 108A - 9.5 Granite	N_{des}	N_{ini}	
Average air voids, back calculated	3.84	13.02	13.02
Average air voids actual, SSD	3.54	11.66	NA
Average air voids actual, beads	NA	NA	11.55
Difference (Back calculated - actual)	0.30	1.37	1.48

Summary, 71A - 12.5 Granite	N_{des}	N_{ini}	
Average air voids, back calculated	5.16	15.05	15.05
Average air voids actual, SSD	5.20	12.59	NA
Average air voids actual, beads	NA	NA	13.17
Difference (Back calculated - actual)	-0.04	2.46	1.87

Summary, 17B - 19.0 Granite	N_{des}	N_{ini}	
Average air voids, back calculated	4.40	13.90	13.90
Average air voids actual, SSD	4.11	9.43	NA
Average air voids actual, beads	NA	NA	10.36
Difference (Back calculated - actual)	0.29	4.47	3.54

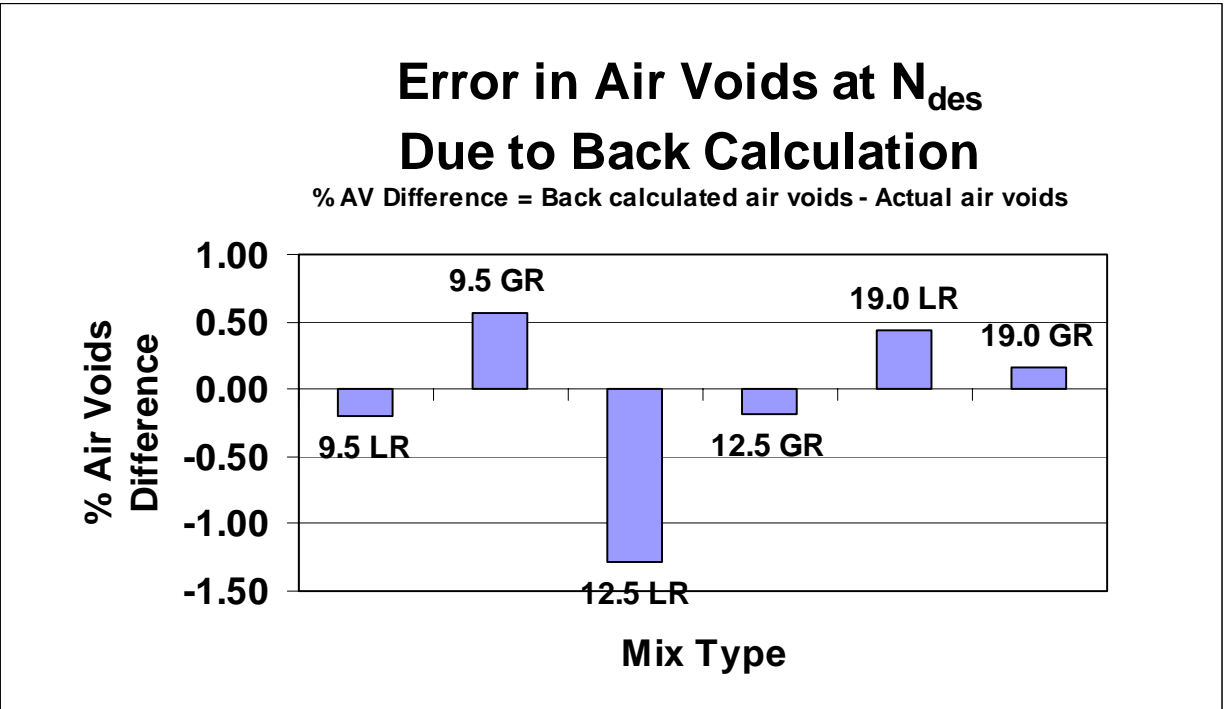


Figure 1 - N_{des} Air Void Data Including Outliers

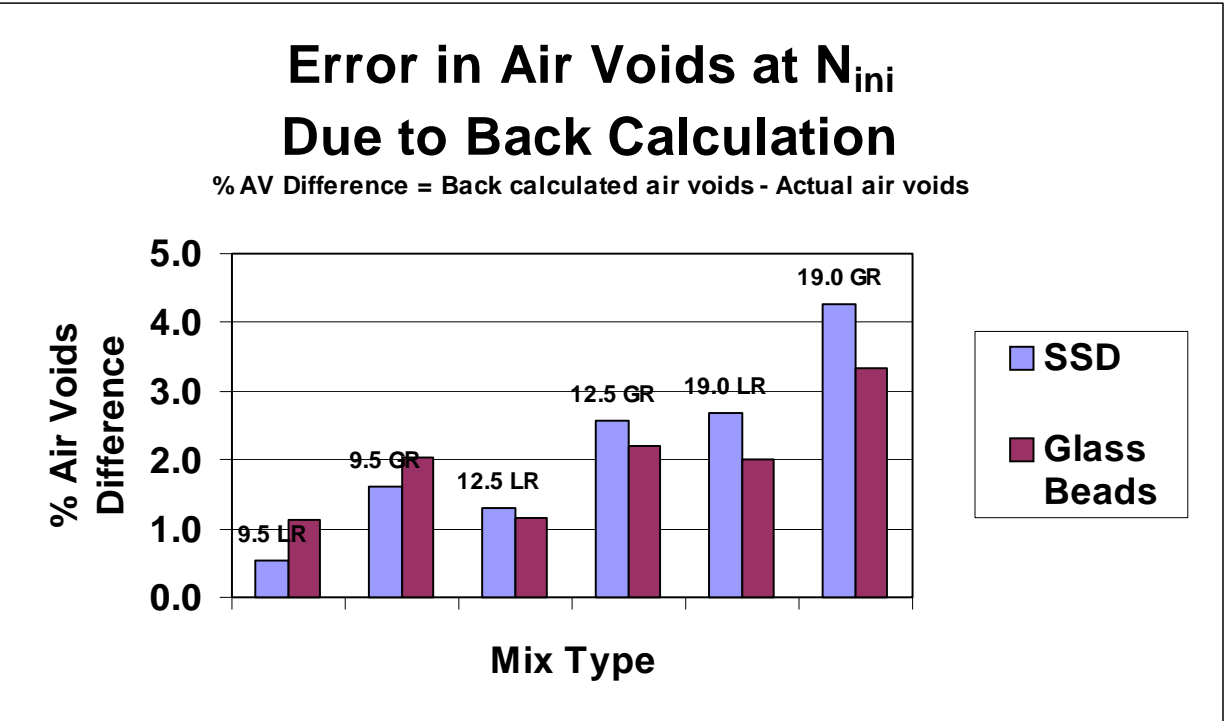


Figure 2 - N_{ini} Air Void Data Including Outliers

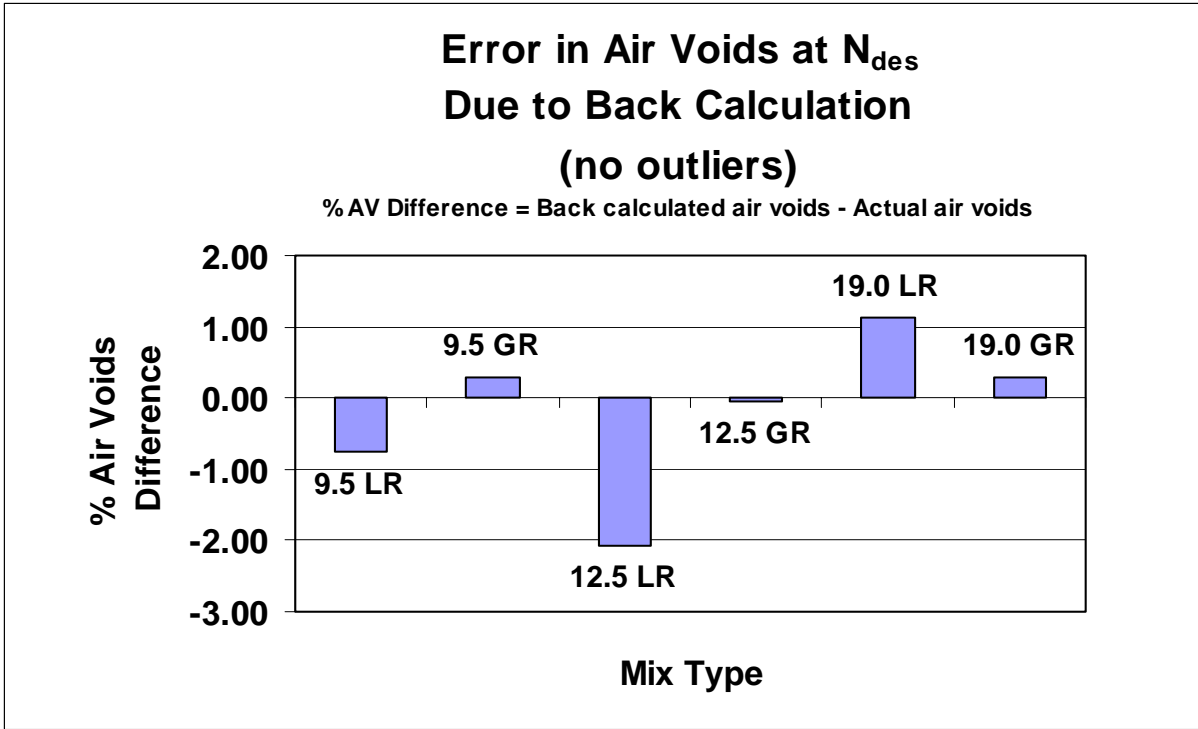


Figure 3 - N_{des} Air Void Data Excluding Outliers

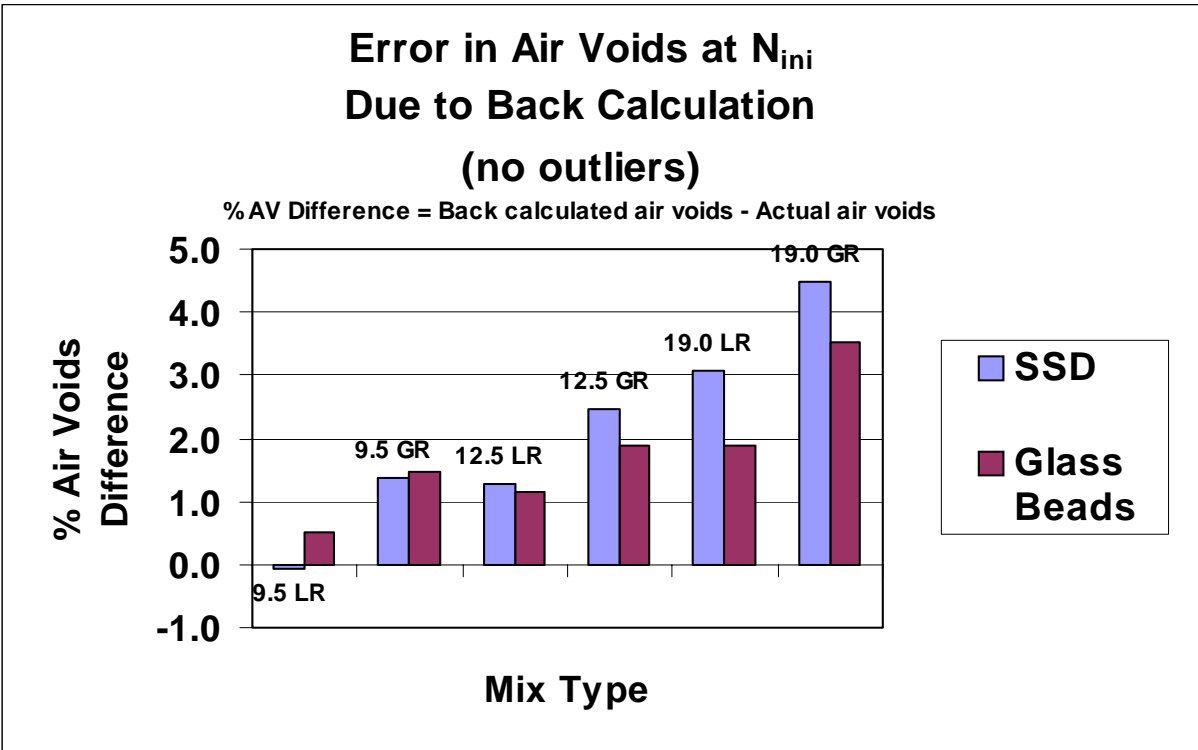


Figure 4 - N_{ini} Air Void Data Excluding Outliers

APPENDIX

Calculations for Mix 177A-12.5 LR (Including Outliers)

N _{max} SSD method					N _{des} SSD method					N _{ni} SSD method					N _{ni} - Glass Beads tested by Bryan Cawley									
Sample ID	A	B	C	D	Range	Sample ID	E	F	G	H	Range	Sample ID	I	J	K	L	Range	Sample ID	I	J	K	L		
Dry Wt.	4538.5	v	4549.7	4546.1	11.2	Dry Wt.	4554.7	4554.0	4546.5	4540.5	14.2	Dry Wt.	4550.0	4545.8	4555.2	4547.7	9.4	Dry Wt.	4550.0	4545.8	4555.2	4547.7		
Wt. In H ₂ O	2544.9	o	2547.6	2537.4		Wt. In H ₂ O	2480.0	2531.8	2458.3	2470.9		Wt. In H ₂ O	2459.4	2456.9	2452.1	2452.3		Wt. partial wet	4594.8	4593.1	4601.1	4587.5		
SSD Wt.	4543.5	l	4553.7	4551.1		SSD Wt.	4570.7	4568.8	4565.7	4553.4		SSD Wt.	4736.3	4752.4	4735.4	4748.8		Wt.w/ beads & bkt (1) kg	32.77	32.66	32.72	32.74		
Volume	1998.6	d	2006.1	2013.7	0.013	Volume	2090.7	2027.0	2107.4	2082.5	0.007	Volume	2276.9	2295.5	2283.3	2296.5	0.018	Wt.w/ beads & bkt (2) kg	32.74	32.69	32.74	32.70		
G _{mb}	2.271		2.268	2.258		G _{mb}	2.179	2.247	2.157	2.180	0.089	G _{mb}	1.998	1.980	1.995	1.980	0.010	Wt.w/ beads & bkt (3) kg	32.77	32.68	32.73	32.71		
G _{mm}	2.322		2.322	2.322		G _{mm}	2.322	2.322	2.322	2.322		G _{mm}	2.322	2.322	2.322	2.322		Wt.w/ beads & bkt (avg)	32.76	32.68	32.73	32.72		
Air Voids	2.20		2.33	2.77	0.6	Air Voids	6.18	3.24	7.09	6.10	3.8	Air Voids	13.94	14.72	14.08	14.72	0.8	Bucket wt.	8.7041	8.7041	8.7041	8.7041		
			Avg air voids	2.44					Avg air voids	5.65						Avg air voids	14.36							
N_{max} dimensional method						Summary, 177A - 12.5 Limerock					N_{des}					N_{ni}								
Ht @ N _{max} , mm	114.8	v	115.2	115.9		Average air voids, back calculated	4.37	15.65	15.65		Average air voids actual, SSD	5.65	14.36	NA		Average air voids actual, beads	NA	NA	14.51		Difference (back calculated-actual)	-1.28	1.29	1.14
Area, cm ²	176.7	o	176.7	176.7		Average air voids actual, SSD	5.65	14.36	NA		Average air voids actual, beads	NA	NA	14.51		Difference (back calculated-actual)	-1.28	1.29	1.14					
Volume, cm ³	2028.7	l	2035.8	2048.1																				
Dry wt.	4538.5	d	4549.7	4546.1																				
G _{mb}	2.237		2.235	2.220																				
G _{mb} corr. fact.	1.015		1.015	1.017																				
N_{des} dimensional method																								
Ht @ N _{des} , mm	117.2	v	117.5	118.2																				
Area, cm ²	176.7	o	176.7	176.7																				
Volume, cm ³	2071.1	l	2076.4	2088.8																				
Dry wt.	4538.5	d	4549.7	4546.1																				
G _{mb}	2.191		2.191	2.176	Range																			
G _{mb} * CF	2.224		2.224	2.214	0.011																			
G _{mm}	2.322		2.322	2.322																				
Air Voids (corr)	4.21		4.24	4.67	0.5																			
			Avg air voids, corr	4.37																				
N_{ni} dimensional method																								
Ht @ N _{ni} , mm	132.8	v	133.6	133.7																				
Area, cm ²	176.7	o	176.7	176.7																				
Volume, cm ³	2346.8	l	2360.9	2362.7																				
Dry wt.	4538.5	d	4549.7	4546.1																				
G _{mb}	1.934		1.927	1.924	Range																			
G _{mb} * CF	1.963		1.956	1.957	0.007																			
G _{mm}	2.322		2.322	2.322																				
Air Voids (corr)	15.46		15.78	15.72	0.3																			
			Avg air voids corr.	15.65																				

Calculations for Mix 178A-19.0 LR (Including Outliers)

N_{max} SSD method

Sample ID	A	B	C	D	Range	St. Dev.
Dry Wt.	4579.5	4572.1	4578.7	4581.6	9.5	
Wt. In H ₂ O	2554.2	2531.0	2517.7	2532.8		
SSD Wt.	4590.7	4585.2	4595.0	4597.5		
Volume	2036.5	2054.2	2077.3	2064.7		
G _{mb}	2.249	2.226	2.204	2.219	0.045	0.019
G _{mm}	2.341	2.341	2.341	2.341		
Air Voids	3.94	4.92	5.85	5.21	1.9	
		Avg air voids	4.98			

N_{max} dimensional method

Ht @ N _{max} , mm	Area, cm ²	Volume, cm ³	Dry wt.	G _{mb}	G _{mb} corr. fact.
117.0	176.7	2067.6	4579.5	2.215	1.015
118.1	176.7	2087.0	4572.1	2.191	1.016
119.6	176.7	2113.5	4578.7	2.166	1.017
119.2	176.7	2106.4	4581.6	2.175	1.020

N₉₅ dimensional method

Ht @ N ₉₅ , mm	Area, cm ²	Volume, cm ³	Dry wt.	G _{mb}	G _{mb} * CF	G _{mm}	Air Voids (corr)
119.4	176.7	2110.0	4579.5	2.170	2.204	2.341	5.87
120.5	176.7	2129.4	4572.1	2.147	2.181	2.341	6.82
122.1	176.7	2157.7	4578.7	2.122	2.159	2.341	7.77
121.6	176.7	2148.8	4581.6	2.132	2.175	2.341	7.08
				Range			1.9
							Avg air voids, corr
							6.89

N₉₅ dimensional method

Ht @ N ₉₅ , mm	Area, cm ²	Volume, cm ³	Dry wt.	G _{mb}	G _{mb} * CF	G _{mm}	Air Voids (corr)
134.7	176.7	2390.3	4579.5	1.924	1.953	2.341	16.56
135.9	176.7	2401.6	4572.1	1.904	1.934	2.341	17.38
138.9	176.7	2454.6	4578.7	1.865	1.898	2.341	18.93
138.0	176.7	2438.7	4581.6	1.879	1.917	2.341	18.12
				Range			2.4
							Avg air voids corr.
							17.75

N₉₅ SSD method

Sample ID	E	F	G	H	Range	St. Dev.
Dry Wt.	4580.2	4588.8	4583.1	4586.7	8.6	
Wt. In H ₂ O	2493.6	2524.6	2522.6	2515.9		
SSD Wt.	4609.7	4609.7	4601.3	4610.5		
Volume	2116.1	2085.1	2078.7	2094.6		
G _{mb}	2.164	2.201	2.205	2.190	0.040	0.018
G _{mm}	2.341	2.341	2.341	2.341		
Air Voids	7.54	5.99	5.82	6.46	1.7	
		Avg air voids	6.45			

G _{mb} , N _{max}	Dens(pcf)	Ht, N _{max}	Mass	Dens(pcf)
2.249	140.3	117.0	4579.5	140.3
2.226	138.9	118.1	4572.1	138.9
2.204	137.5	119.6	4578.7	137.5
2.219	138.5	119.2	4581.6	138.5

Summary, 178A - 19.0 Limerock		N ₉₅	N ₉₅
Average air voids, back calculated		6.89	17.75
Average air voids actual, SSD		6.45	15.06
Average air voids actual, beads		NA	15.74
Difference (back calculated-actual)		0.43	2.69

N₉₅ SSD method

Sample ID	I	J	K	L	Range	St. Dev.
Dry Wt.	4588.3	4588.2	4591.4	4589.9	3.2	
Wt. In H ₂ O	2497.4	2512.2	2504.1	2511.8		
SSD Wt.	4790.5	4837.2	4815.2	4814.8		
Volume	2293.1	2325.0	2311.1	2303.0		
G _{mb}	2.001	1.973	1.987	1.993	0.027	0.012
G _{mm}	2.341	2.341	2.341	2.341		
Air Voids	14.53	15.70	15.14	14.87	1.2	
		Avg air voids	15.06			

N₉₅ - Glass Beads tested by Bryan Cawley

Sample ID	I	J	K	L	Range
Dry Wt.	4588.3	4588.2	4591.4	4589.9	
Wt. partial wet	4645.3	4660.8	4652.0	4654.0	
Wt.w/ beads & bkt.(1) kg	32.76	32.68	32.72	32.70	
Wt.w/ beads & bkt.(2) kg	32.82	32.68	32.72	32.72	
Wt.w/ beads & bkt.(3) kg	32.78	32.68	32.74	32.70	
Wt.w/ beads & bkt.(avg)	32.79	32.68	32.73	32.71	
Bucket wt.	8.7041	8.7041	8.7041	8.7041	
Wt. of beads, g	19437.3	19315.1	19370.6	19348.6	
Volume of beads, cm ³	11794.7	11720.6	11754.2	11740.9	
Pill vol = bkt vol - bead vol	2284.8	2358.9	2325.3	2338.6	Range
G _{mb} pill	2.008	1.945	1.975	1.963	0.063
G _{mm}	2.341	2.341	2.341	2.341	
Air Voids	14.22	16.91	15.65	16.16	2.7
		Avg air voids	15.74		

Bucket Wt. (Empty)	8.7041	kg
Bucket Volume	14079.5	cm ³
Beads and Bucket	1	2
	31.84	31.92
	31.96	31.96
		kg
Avg. (beads and bucket)	31.91	kg
Avg. minus bucket wt.	23.20	kg
G _{mb} of beads	1.648	

Calculations for Mix 108A-9.5 GR (Including Outliers)

N _{max} SSD method						N _{sef} SSD method						N _{ni} SSD method						N _{ni} - Glass Beads tested by Greg Sholar						
Sample ID	A	B	C	D	Range	Sample ID	E	F	G	H	Range	Sample ID	I	J	K	L	Range	Sample ID	I	J	K	L		
Dry Wt.	4993.5	5001.3	4997.4	4981.5	19.8	Dry Wt.	4978.9	4979.1	4975.1	4976.3	4.0	Dry Wt.	4978.9	4977.4	4976.7	4976.3	2.6	Dry Wt.	4978.9	4977.4	4976.7	4976.3		
Wt. In H ₂ O	2938.4	2960.2	2958.1	2954.6		Wt. In H ₂ O	2929.2	2927.4	2928.0	2930.5		Wt. In H ₂ O	2808.5	2806.1	2822.7	2801.7		Wt. partial wet	5029.1	5030.7	5026.5	5005.4		
SSD Wt.	4996.6	5003.2	4999.8	4983.9		SSD Wt.	4982.3	4982.2	4978.2	4979.5		SSD Wt.	5062.7	5068.7	5038.9	5030.0		Wt.w/ beads & bkt.(1) kg	33.24	33.24	33.30	33.26		
Volume	2058.2	2043.0	2041.7	2029.3		Volume	2053.1	2054.8	2050.2	2049.0		Volume	2254.2	2262.6	2216.2	2228.3		Wt.w/ beads & bkt.(2) kg	33.26	33.26	33.30	33.26		
G _{mb}	2.426	2.448	2.448	2.455	0.029	G _{mb}	2.425	2.423	2.427	2.429	0.005	G _{mb}	2.209	2.200	2.246	2.233	0.046	Wt.w/ beads & bkt.(3) kg	33.26	33.24	33.32	33.20		
G _{mm}	2.515	2.515	2.515	2.515		G _{mm}	2.515	2.515	2.515	2.515		G _{mm}	2.515	2.515	2.515	2.515		Wt.w/ beads & bkt.(avg)	33.25	33.25	33.31	33.24		
Air Voids	3.53	2.66	2.68	2.39	1.1	Air Voids	3.58	3.65	3.51	3.43	0.2	Air Voids	12.18	12.53	10.71	11.20	1.8	Bucket wt.	8.7041	8.7041	8.7041	8.7041		
		Avg air voids	2.82					Avg air voids			3.54			Avg air voids			11.66							
N _{max} dimensional method						N _{sef} dimensional method						N _{ni} dimensional method						N _{ni} - Glass Beads tested by Greg Sholar						
Ht @ N _{max} , mm	118.0	117.1	117.1	116.4		Gmb, Nmax	Dens(pcf)	Ht, Nmax	Mass	Dens(pcf)								Volume of beads, g	19520.1	19511.9	19576.1	19530.5		
Area, cm ²	176.7	176.7	176.7	176.7			2.426	151.4	118.0	4993.5	151.4							Volume of beads, cm ³	11841.6	11836.6	11875.5	11847.9		
Volume, cm ³	2065.2	2069.3	2069.3	2057.0			2.448	152.8	117.1	5001.3	152.8							Pill vol = bkt vol - bead vol	2237.9	2242.9	2204.0	2231.6	Range	
Dry wt.	4993.5	5001.3	4997.4	4981.5			2.448	152.7	117.1	4997.4	152.7							G _{mb} pill	2.225	2.219	2.258	2.230	0.039	
G _{mb}	2.395	2.417	2.415	2.422			2.455	153.2	116.4	4981.5	153.2							G _{mm}	2.515	2.515	2.515	2.515		
G _{mb} corr. fact.	1.013	1.013	1.014	1.014														Air Voids	11.54	11.76	10.22	11.34	1.5	
																			Avg air voids		11.21			
N _{sef} dimensional method						Summary, 108A - 9.5 Granite						N _{ni} dimensional method						N _{ni} - Glass Beads tested by Greg Sholar						
Ht @ N _{sef} , mm	119.7	118.7	118.6	117.9		Average air voids, back calculated	4.11	13.26	13.26									Bucket Wt. (Empty)	8.7041		kg			
Area, cm ²	176.7	176.7	176.7	176.7		Average air voids actual, SSD	3.54	11.66	NA									Bucket Volume	14079.5		cm ³			
Volume, cm ³	2115.3	2097.6	2095.8	2083.5		Average air voids actual, beads	NA	NA	11.21									Beads and Bucket	1	2	3			
Dry wt.	4993.5	5001.3	4997.4	4981.5		Difference (back calculated-actual)	0.56	1.60	2.04															
G _{mb}	2.361	2.384	2.384	2.391	Range																			
G _{mb} * CF	2.392	2.415	2.417	2.424	0.032																			
G _{mm}	2.515	2.515	2.515	2.515																				
Air Voids (corr)	4.90	3.98	3.91	3.64	1.3																			
		Avg air voids, corr		4.11																				
N _{ni} dimensional method																								
Ht @ N _{ni} , mm	132.3	131.3	131.1	130.3																				
Area, cm ²	176.7	176.7	176.7	176.7																				
Volume, cm ³	2337.9	2320.3	2316.7	2302.6																				
Dry wt.	4993.5	5001.3	4997.4	4981.5																				
G _{mb}	2.136	2.155	2.157	2.163	Range																			
G _{mb} * CF	2.164	2.183	2.186	2.193	0.029																			
G _{mm}	2.515	2.515	2.515	2.515																				
Air Voids (corr)	13.96	13.19	13.07	12.81	1.2																			
		Avg air voids, corr		13.26																				

Calculations for Mix 176A-9.5 LR (Excluding Outliers)

N _{max} SSD method						N _{des} SSD method						N _{inj} SSD method						N _{inj} - Glass Beads tested by Brian Cawley					
Sample ID	A	B	C	D	Range	Sample ID	E	F	G	H	Range	Sample ID	I	J	K	L	Range	Sample ID	I	J	K	L	
Dry Wt.	4509.1	4499.7	4506.8		9.4	Dry Wt.	4503.7	4506.5	4501.7	4500.2	6.3	Dry Wt.	4510.2	4502.1	4508.0	4516.4	14.3	Dry Wt.	4510.2	4502.1	4508.0	4516.4	
Wt. In H ₂ O	2499.8	2501.6	2502.7			Wt. In H ₂ O	2440.4	2446.4	2460.9	2454.2		Wt. In H ₂ O	2380.2	2396.5	2389.7	2392.1		Wt. partial wet	4557.5	4556.5	4565.2	4575.4	
SSD Wt.	4513.2	4502.6	4508.8			SSD Wt.	4514.3	4512.3	4508.9	4508.5		SSD Wt.	4679.2	4727.4	4681.1	4733.4		Wt w/ beads & bkt (1) kg	32.80	32.70	32.84	32.76	
Volume	2013.4	2001.0	2006.1			Volume	2073.9	2065.9	2048.0	2054.3		Volume	2299.0	2330.9	2291.4	2341.3		Wt w/ beads & bkt (2) kg	32.80	32.72	32.80	32.74	
G _{mb}	2.240	2.249	2.247		0.009	G _{mb}	2.172	2.181	2.198	2.191	0.026	G _{mb}	1.962	1.931	1.967	1.929	0.038	Wt w/ beads & bkt (3) kg	32.80	32.70	32.82	32.68	
G _{mm}	2.311	2.311	2.311			G _{mm}	2.311	2.311	2.311	2.311		G _{mm}	2.311	2.311	2.311	2.311		Wt w/ beads & bkt (avg)	32.80	32.71	32.82	32.73	
Air Voids	3.09	2.69	2.79		0.4	Air Voids	6.03	5.61	4.89	5.21	1.1	Air Voids	15.11	16.42	14.87	16.53	1.7	Bucket wt.	8.7041	8.7041	8.7041	8.7041	
		Avg air voids		2.86				Avg air voids		5.43				Avg air voids		15.73		Wt. of beads, g	19538.4	19446.1	19550.7	19447.2	
N _{max} dimensional method						N _{des} dimensional method						N _{inj} dimensional method						N _{inj} - Glass Beads tested by Brian Cawley					
Ht @ N _{max} , mm	115.4	114.4	114.8			G _{mb} , N _{max}	Dens(pct)	Ht, N _{max}	Mass	Dens(pct)	Ht @ N _{inj} , mm	133.1	131.4	132.4			Pill vol = bkt vol - bead vol	2274.3	2330.1	2266.9	2329.4	Range	
Area, cm ²	176.7	176.7	176.7				2.240	139.7	115.4	4509.1	139.7	Area, cm ²	176.7	176.7	176.7			G _{mb} pill	1.983	1.932	1.989	1.939	0.056
Volume, cm ³	2039.3	2021.6	2028.7				2.249	140.3	114.4	4499.7	140.3	Volume, cm ³	2078.2	2060.5	2067.6			G _{mm}	2.311	2.311	2.311	2.311	
Dry wt.	4509.1	4499.7	4506.8				2.247	140.2	114.8	4506.8	140.2	Dry wt.	4509.1	4499.7	4506.8			Air Voids	14.19	16.39	13.95	16.10	2.4
G _{mb}	2.211	2.226	2.222									G _{mb}	2.170	2.184	2.180		Range			Avg air voids		15.16	
G _{mb} corr. fact.	1.013	1.010	1.011									G _{mb} * CF	2.198	2.206	2.204		0.009	Bucket Wt. (Empty)		8.7041	kg		
N _{des} dimensional method						Summary, 176A - 9.5 Limerock						N _{inj} dimensional method						N _{inj} - Glass Beads tested by Brian Cawley					
Ht @ N _{des} , mm	117.6	116.6	117.0			Average air voids, back calculated	N _{des}		N _{inj}		Ht @ N _{inj} , mm	133.1	131.4	132.4			Bucket Volume		14079.5	cm ³			
Area, cm ²	176.7	176.7	176.7			Average air voids actual, SSD	4.68	15.66	15.66		Area, cm ²	176.7	176.7	176.7			Beads and Bucket		1	2	3		
Volume, cm ³	2078.2	2060.5	2067.6			Average air voids actual, beads	5.43	15.73	NA		Volume, cm ³	2352.1	2322.0	2339.7					32.02	32.02	31.98	kg	
Dry wt.	4509.1	4499.7	4506.8			Difference (back calculated-actual)	-0.75	-0.07	0.50		Dry wt.	4509.1	4499.7	4506.8			Avg. (beads and bucket)		32.01	kg			
G _{mb}	2.170	2.184	2.180		Range						G _{mb}	1.917	1.938	1.926		0.016	Avg. minus bucket wt.		23.30	kg			
G _{mb} * CF	2.198	2.206	2.204		0.009						G _{mb} * CF	1.942	1.958	1.948			G _{mb} of beads		1.655				
G _{mm}	2.311	2.311	2.311								G _{mm}	2.311	2.311	2.311									
Air Voids (corr)	4.90	4.53	4.62		0.4						Air Voids (corr)	15.98	15.28	15.71		0.7							
		Avg air voids, corr		4.68									Avg air voids corr.		15.66								
N _{inj} dimensional method																							
Ht @ N _{inj} , mm	133.1	131.4	132.4																				
Area, cm ²	176.7	176.7	176.7																				
Volume, cm ³	2352.1	2322.0	2339.7																				
Dry wt.	4509.1	4499.7	4506.8																				
G _{mb}	1.917	1.938	1.926		Range																		
G _{mb} * CF	1.942	1.958	1.948		0.016																		
G _{mm}	2.311	2.311	2.311																				
Air Voids (corr)	15.98	15.28	15.71		0.7																		
		Avg air voids corr.		15.66																			

Calculations for Mix 177A-12.5 LR (Excluding Outliers)

N _{max} SSD method						N _{des} SSD method						N _{inj} SSD method						N _{inj} - Glass Beads tested by Bryan Cawley										
Sample ID	A	B	C	D	Range	Sample ID	E	F	G	H	Range	Sample ID	I	J	K	L	Range	Sample ID	I	J	K	L						
Dry Wt.	4538.5	v	4549.7	4546.1	11.2	Dry Wt.	4554.7		4546.5	4540.5	14.2	Dry Wt.	4550.0	4545.8	4555.2	4547.7	9.4	Dry Wt.	4550.0	4545.8	4555.2	4547.7						
Wt. In H ₂ O	2544.9	o	2547.6	2537.4		Wt. In H ₂ O	2480.0		2458.3	2470.9		Wt. In H ₂ O	2459.4	2456.9	2452.1	2452.3		Wt. partial wet	4594.8	4593.1	4601.1	4587.5						
SSD Wt.	4543.5	l	4553.7	4551.1		SSD Wt.	4570.7		4565.7	4553.4		SSD Wt.	4736.3	4752.4	4735.4	4748.8		Wt w/ beads & bkt (1) kg	32.77	32.66	32.72	32.74						
Volume	1998.6	d	2006.1	2013.7		Volume	2090.7		2107.4	2082.5		Volume	2276.9	2295.5	2283.3	2296.5		Wt w/ beads & bkt (2) kg	32.74	32.69	32.74	32.70						
G _{mb}	2.271		2.268	2.258	0.013	G _{mb}	2.179		2.157	2.180	0.023	G _{mb}	1.998	1.980	1.995	1.980	0.018	Wt w/ beads & bkt (3) kg	32.77	32.68	32.73	32.71						
G _{mm}	2.322			2.322		G _{mm}	2.322		2.322	2.322		G _{mm}	2.322	2.322	2.322	2.322		Wt w/ beads & bkt (avg)	32.76	32.68	32.73	32.72						
Air Voids	2.20		2.33	2.77	0.6	Air Voids	6.18		7.09	6.10	1.0	Air Voids	13.94	14.72	14.08	14.72	0.8	Bucket wt.	8.7041	8.7041	8.7041	8.7041						
			Avg air voids	2.44					Avg air voids	6.46						Avg air voids	14.36											
N _{max} dimensional method						N _{des} dimensional method						N _{inj} dimensional method						N _{inj} - Glass Beads tested by Bryan Cawley										
Ht @ N _{max} , mm	114.8	v	115.2	115.9		G _{mb} , N _{max}	Dens(pcf)	Ht, N _{max}	Mass	Dens(pcf)		Ht @ N _{inj} , mm	117.2	v	117.5	118.2		Pill vol = bkt vol - bead vol	2268.7	2318.2	2290.7	2290.5	Range					
Area, cm ²	176.7	o	176.7	176.7			2.271	141.7	114.8	4538.5	141.7		Area, cm ²	176.7	o	176.7	176.7		G _{mb} pill	2.006	1.961	1.989	1.985	0.045				
Volume, cm ³	2028.7	l	2035.8	2048.1			2.268	141.5	115.2	4549.7	141.5		Volume, cm ³	2071.1	l	2076.4	2088.8		G _{mm}	2.322	2.322	2.322	2.322					
Dry wt.	4538.5	d	4549.7	4546.1			2.258	140.9	115.9	4546.1	140.9		Dry wt.	4538.5	d	4549.7	4546.1		Air Voids	13.63	15.55	14.36	14.49	1.9				
G _{mb}	2.237			2.220									G _{mb}	2.191		2.191	2.176	Range										
G _{mb} corr. fact.	1.015		1.015	1.017									G _{mb} * CF	2.224		2.224	2.214	0.011										
													G _{mm}	2.322		2.322	2.322											
													Air Voids (corr)	4.21		4.24	4.67	0.5										
			Avg air voids, corr	4.37												Avg air voids, corr	4.37											
N _{inj} dimensional method						Summary, 177A - 12.5 Limerock						N _{des}						N _{inj}										
Ht @ N _{inj} , mm	132.8	v	133.6	133.7		Average air voids, back calculated		4.37	15.65	15.65		Average air voids actual, SSD		6.46	14.36	NA		Average air voids actual, beads		NA	NA	14.51		Difference (back calculated-actual)		-2.09	1.29	1.14
Area, cm ²	176.7	o	176.7	176.7		Average air voids actual, beads		NA	NA	14.51		Difference (back calculated-actual)		-2.09	1.29	1.14		Avg. (beads and bucket)		31.90	kg		Avg. minus bucket wt.		23.20	kg		
Volume, cm ³	2346.8	l	2360.9	2362.7		G _{mb} of beads		1.648				Avg. of beads		1.648				Bucket Wt. (Empty)		8.7041	kg		Bucket Volume		14079.5	cm ³		
Dry wt.	4538.5	d	4549.7	4546.1		Beads and Bucket		31.89	31.93	31.89	kg	Bucket Wt. (Empty)		8.7041	kg			Bucket Volume		14079.5	cm ³		Beads and Bucket		31.89	31.93	31.89	kg
G _{mb}	1.934		1.927	1.924	Range	Avg. (beads and bucket)		31.90	kg			Avg. minus bucket wt.		23.20	kg			G _{mb} of beads		1.648			Avg. (beads and bucket)		31.90	kg		
G _{mb} * CF	1.963		1.956	1.957	0.007	Avg. minus bucket wt.		23.20	kg			G _{mb} of beads		1.648				Avg. (beads and bucket)		31.90	kg		Avg. minus bucket wt.		23.20	kg		
G _{mm}	2.322		2.322	2.322		G _{mb} of beads		1.648				Avg. (beads and bucket)		31.90	kg			Avg. minus bucket wt.		23.20	kg		G _{mb} of beads		1.648			
Air Voids (corr)	15.46		15.78	15.72	0.3	Avg. minus bucket wt.		23.20	kg			G _{mb} of beads		1.648				Avg. (beads and bucket)		31.90	kg		Avg. minus bucket wt.		23.20	kg		
			Avg air voids corr.	15.65		G _{mb} of beads		1.648				Avg. (beads and bucket)		31.90	kg			Avg. minus bucket wt.		23.20	kg		G _{mb} of beads		1.648			

Calculations for Mix 178A-19.0 LR (Excluding Outliers)

N_{max} SSD method

Sample ID	A	B	C	D	Range
Dry Wt.	4572.1	4578.7	4581.6		9.5
Wt. In H ₂ O	2531.0	2517.7	2532.8		
SSD Wt.	4585.2	4595.0	4597.5		
Volume	2054.2	2077.3	2064.7		
G _{mb}	2.226	2.204	2.219	0.022	
G _{mm}	2.341	2.341	2.341		
Air Voids	4.92	5.85	5.21	0.9	
	Avg air voids		5.33		

N_{des} SSD method

Sample ID	E	F	G	H	Range
Dry Wt.	4588.8	4583.1	4586.7		5.7
Wt. In H ₂ O	2524.6	2522.6	2515.9		
SSD Wt.	4609.7	4601.3	4610.5		
Volume	2085.1	2078.7	2094.6		
G _{mb}	2.201	2.205	2.190	0.015	
G _{mm}	2.341	2.341	2.341		
Air Voids	5.99	5.82	6.46	0.6	
	Avg air voids		6.09		

N_{inj} SSD method

Sample ID	I	J	K	L	Range
Dry Wt.	4588.3	4588.2	4591.4	4589.9	3.2
Wt. In H ₂ O	2497.4	2512.2	2504.1	2511.8	
SSD Wt.	4790.5	4837.2	4815.2	4814.8	
Volume	2293.1	2325.0	2311.1	2303.0	
G _{mb}	2.001	1.973	1.967	1.993	0.027
G _{mm}	2.341	2.341	2.341	2.341	
Air Voids	14.53	15.70	15.14	14.87	1.2
	Avg air voids		15.06		

N_{inj} - Glass Beads tested by Bryan Cawley

Sample ID	I	J	K	L
Dry Wt.	4588.2	4591.4	4589.9	
Wt. partial wet	4660.8	4652.0	4654.0	
Wt w/ beads & bkt (1) kg	32.68	32.72	32.70	
Wt w/ beads & bkt (2) kg	32.68	32.72	32.72	
Wt w/ beads & bkt (3) kg	32.68	32.74	32.70	
Wt w/ beads & bkt (avg)	32.68	32.73	32.71	
Bucket wt.	8.7041	8.7041	8.7041	
Wt. of beads, g	19315.1	19370.6	19348.6	
Volume of beads, cm ³	11720.6	11754.2	11740.9	
Pill vol = bkt vol - bead vol	2358.9	2325.3	2338.6	Range
G _{mb} pill	1.945	1.975	1.963	0.030
G _{mm}	2.341	2.341	2.341	
Air Voids	16.91	15.65	16.16	1.3
	Avg air voids		16.24	

N_{max} dimensional method

Ht @ N _{max} , mm	A	B	C
	118.1	119.6	119.2
Area, cm ²	176.7	176.7	176.7
Volume, cm ³	2087.0	2113.5	2106.4
Dry wt.	4572.1	4578.7	4581.6
G _{mb}	2.191	2.166	2.175
G _{mb} corr. fact.	1.016	1.017	1.020

G _{mb} , N _{max}	Dens(pcf)	Ht, N _{max}	Mass	Dens(pcf)
0.000	0.0	0.0	0.0	0.0
2.226	138.9	118.1	4572.1	138.9
2.204	137.5	119.6	4578.7	137.5
2.219	138.5	119.2	4581.6	138.5

N_{des} dimensional method

Ht @ N _{des} , mm	A	B	C
	120.5	122.1	121.6
Area, cm ²	176.7	176.7	176.7
Volume, cm ³	2129.4	2157.7	2148.8
Dry wt.	4572.1	4578.7	4581.6
G _{mb}	2.147	2.122	2.132
G _{mb} * CF	2.181	2.159	2.175
G _{mm}	2.341	2.341	2.341
Air Voids (corr)	6.62	7.77	7.08
	Avg air voids, corr		7.22

Summary, 178A - 19.0 Limerock		N _{des}	N _{inj}	
Average air voids, back calculated		7.22	18.14	18.14
Average air voids actual, SSD		6.09	15.06	NA
Average air voids actual, beads		NA	NA	16.24
Difference (back calculated-actual)		1.13	3.09	1.90

Bucket Wt. (Empty)	8.7041	kg		
Bucket Volume	14079.5	cm ³		
Beads and Bucket	1	2	3	
	31.84	31.92	31.96	kg
Avg. (beads and bucket)	31.91	kg		
Avg. minus bucket wt.	23.20	kg		
G _{mb} of beads	1.648			

N_{inj} dimensional method

Ht @ N _{inj} , mm	A	B	C
	135.9	138.9	138.0
Area, cm ²	176.7	176.7	176.7
Volume, cm ³	2401.6	2454.6	2438.7
Dry wt.	4572.1	4578.7	4581.6
G _{mb}	1.904	1.865	1.879
G _{mb} * CF	1.934	1.898	1.917
G _{mm}	2.341	2.341	2.341
Air Voids (corr)	17.38	18.93	18.12
	Avg air voids corr.		18.14

Calculations for Mix 108A-9.5 GR (Excluding Outliers)

N_{max} SSD method

Sample ID	A	B	C	D	Range
Dry Wt.	5001.3	4997.4	4981.5		19.8
Wt. In H ₂ O	2960.2	2958.1	2954.6		
SSD Wt.	5003.2	4999.8	4983.9		
Volume	2043.0	2041.7	2029.3		
G _{mb}	2.448	2.448	2.455	0.007	
G _{mm}	2.515	2.515	2.515		
Air Voids	2.66	2.68	2.39	0.3	
Avg air voids	2.58				

N_{des} SSD method

Sample ID	E	F	G	H	Range
Dry Wt.	4978.9	4979.1	4975.1	4976.3	4.0
Wt. In H ₂ O	2929.2	2927.4	2928.0	2930.5	
SSD Wt.	4982.3	4982.2	4978.2	4979.5	
Volume	2053.1	2054.8	2050.2	2049.0	
G _{mb}	2.425	2.423	2.427	2.429	0.005
G _{mm}	2.515	2.515	2.515	2.515	
Air Voids	3.58	3.65	3.51	3.43	0.2
Avg air voids	3.54				

N_{ij} SSD method

Sample ID	I	J	K	L	Range
Dry Wt.	4978.9	4977.4	4976.7	4976.3	2.6
Wt. In H ₂ O	2808.5	2806.1	2822.7	2801.7	
SSD Wt.	5062.7	5068.7	5038.9	5030.0	
Volume	2254.2	2262.6	2216.2	2228.3	
G _{mb}	2.209	2.200	2.246	2.233	0.046
G _{mm}	2.515	2.515	2.515	2.515	
Air Voids	12.18	12.53	10.71	11.20	1.8
Avg air voids	11.66				

N_{ij} - Glass Beads tested by Greg Sholar

Sample ID	I	J	K	L
Dry Wt.	4978.9	4977.4		4976.3
Wt. partial wet	5029.1	5030.7		5005.4
Wt w/ beads & bkt (1) kg	33.24	33.24		33.26
Wt w/ beads & bkt (2) kg	33.26	33.26		33.26
Wt w/ beads & bkt (3) kg	33.26	33.24		33.20
Wt w/ beads & bkt (avg)	33.25	33.25		33.24
Bucket wt.	8.7041	8.7041		8.7041
Wt. of beads, g	19520.1	19511.9		19530.5
Volume of beads, cm ³	11841.6	11836.6		11847.9
Pill vol = bkt vol - bead vol	2237.9	2242.9		2231.6
G _{mb} pill	2.225	2.219		2.230
G _{mm}	2.515	2.515		2.515
Air Voids	11.54	11.76		11.34
Avg air voids	11.55			

N_{max} dimensional method

Ht @ N _{max} , mm	A	B	C
Area, cm ²	117.1	117.1	116.4
Volume, cm ³	2069.3	2069.3	2057.0
Dry wt.	5001.3	4997.4	4981.5
G _{mb}	2.417	2.415	2.422
G _{mb} corr. fact.	1.013	1.014	1.014

G _{mb} , Nmax	Dens(pcf)	Ht, Nmax	Mass	Dens(pcf)
0.000	0.0	0.0	0.0	0.0
2.448	152.8	117.1	5001.3	152.8
2.448	152.7	117.1	4997.4	152.7
2.455	153.2	116.4	4981.5	153.2

Summary, 108A - 9.5 Granite	N _{des}	N _{ij}
Average air voids, back calculated	3.84	13.02
Average air voids actual, SSD	3.54	11.66
Average air voids actual, beads	NA	NA
Difference (back calculated-actual)	0.30	1.37

Bucket Wt. (Empty)	8.7041	kg
Bucket Volume	14079.5	cm ³
Beads and Bucket	1	2
	31.86	31.94
	31.94	31.94
	kg	
Avg. (beads and bucket)	31.91	kg
Avg. minus bucket wt.	23.21	kg
G _{mb} of beads	1.648	

N_{des} dimensional method

Ht @ N _{des} , mm	A	B	C
Area, cm ²	118.7	118.6	117.9
Volume, cm ³	2097.6	2095.8	2083.5
Dry wt.	5001.3	4997.4	4981.5
G _{mb}	2.384	2.384	2.391
G _{mb} * CF	2.415	2.417	2.424
G _{mm}	2.515	2.515	2.515
Air Voids (corr)	3.98	3.91	3.64
Avg air voids, corr	3.84		

N_{ij} dimensional method

Ht @ N _{ij} , mm	A	B	C
Area, cm ²	131.3	131.1	130.3
Volume, cm ³	2320.3	2316.7	2302.6
Dry wt.	5001.3	4997.4	4981.5
G _{mb}	2.155	2.157	2.163
G _{mb} * CF	2.183	2.186	2.193
G _{mm}	2.515	2.515	2.515
Air Voids (corr)	13.19	13.07	12.81
Avg air voids, corr	13.02		

Outlier Determination; FDOT method

Mix ID	Gmb @ Nmax			D	Avg.	Range	Avg + R/2	Avg - R/2	Outlier
	A	B	C						
176A-9.5 LR	2.240	2.249	2.247	2.196	2.233	0.053	2.259	2.206	D
177A-12.5 LR	2.271		2.268	2.258	2.265	0.013	2.272	2.259	None
178A-19.0 LR	2.249	2.226	2.204	2.219	2.224	0.045	2.247	2.202	A
108A-9.5 GR	2.426	2.448	2.448	2.455	2.444	0.029	2.458	2.430	A
71A-12.5 GR	2.461	2.410	2.449	2.455	2.444	0.051	2.469	2.418	B
17B-19.0 GR	2.461	2.446	2.450	2.446	2.451	0.016	2.458	2.443	A

Mix ID	Gmb @ Ndes			H	Avg.	Range	Avg + R/2	Avg - R/2	Outlier
	E	F	G						
176A-9.5 LR	2.172	2.181	2.198	2.191	2.185	0.026	2.199	2.172	None
177A-12.5 LR	2.179	2.247	2.157	2.180	2.191	0.089	2.235	2.146	F
178A-19.0 LR	2.164	2.201	2.205	2.190	2.190	0.040	2.210	2.170	E
108A-9.5 GR	2.425	2.423	2.427	2.429	2.426	0.005	2.429	2.423	None
71A-12.5 GR	2.359	2.433	2.427	2.390	2.402	0.074	2.439	2.365	E
17B-19.0 GR	2.407	2.437	2.425	2.417	2.421	0.030	2.436	2.406	None*

*Include 2.437 even though 0.001 high

Mix ID	Gmb @ Nini (SSD method)				Avg.	Range	Avg + R/2	Avg - R/2	Outlier
	I	J	K	L					
176A-9.5 LR	1.962	1.931	1.967	1.929	1.947	0.038	1.967	1.928	None
177A-12.5 LR	1.998	1.980	1.995	1.980	1.988	0.018	1.998	1.979	None
178A-19.0 LR	2.001	1.973	1.987	1.993	1.989	0.027	2.002	1.975	None
108A-9.5 GR	2.209	2.200	2.246	2.233	2.222	0.046	2.245	2.199	None
71A-12.5 GR	2.225	2.229	2.231	2.206	2.223	0.025	2.235	2.210	L
17B-19.0 GR	2.287	2.286	2.284	2.291	2.287	0.007	2.290	2.284	None

Mix ID	Gmb @ Nini (Glass Beads method)				Avg.	Range	Avg + R/2	Avg - R/2	Outlier
	I	J	K	L					
176A-9.5 LR	1.983	1.932	1.989	1.939	1.961	0.056	1.989	1.932	None
177A-12.5 LR	2.006	1.961	1.989	1.985	1.985	0.045	2.007	1.963	None
178A-19.0 LR	2.008	1.945	1.975	1.963	1.973	0.063	2.004	1.941	I
108A-9.5 GR	2.225	2.219	2.258	2.230	2.233	0.039	2.252	2.214	K
71A-12.5 GR	2.215	2.221	2.204	2.213	2.213	0.018	2.222	2.204	None
17B-19.0 GR	2.252	2.285	2.280	2.237	2.263	0.049	2.288	2.239	None